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FORM: The FORTRAN Object Recovery Model. A Methodology to Extract Object-Oriented Designs From Imperative Code.

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FORM: THE FORTRAN OBJECT RECOVERY MODEL – A METHODOLOGY TO EXTRACT OBJECT-ORIENTED DESIGNS FROM IMPERATIVE CODE

A Dissertation

Submitted to the Graduate Faculty of the Louisiana State University an Agricultural and Mechanical College in partial fulfillment of the requirements for the degree of Doctor of Philosophy

in

The Department of Computer Science

by

Bonnie Lynn Achee
B.S. Southeastern Louisiana University, 1990
May 1998
in memory of my parents,
Acknowledgements

I would like to begin by thanking God for His presence in my life. Throughout the course of my studies at LSU, I have experienced some of the most joyous and most devastating moments of my personal life. He has walked beside me to guide me and carried me through the times when I felt I could not go on. I am truly grateful for His unconditional love and its manifestation in the many friends I have made during my graduate career.

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Abstract

A majority of legacy systems in use in the scientific and engineering application domains are coded in imperative languages, specifically, COBOL or FORTRAN-77. These systems have an average age of 15 years or more and have undergone years of extensive maintenance. They suffer from either poor documentation or no documentation, and antiquated coding practices and paradigms [Chik 94] [Osbo 90]. The purpose of this research is to develop a reverse-engineering methodology to extract an object-oriented design from legacy systems written in imperative languages. This research defines a three-phase methodology that inputs source code and outputs an object-oriented design.

The three phases of the methodology include: Object Extraction, Class Abstraction, and Formation of the Inheritance Hierarchy. Additionally, there is a pre-processing phase that involves code structuring, alias resolution, and resolution of the COMMON block. Object Extraction is divided into two stages: Attribute Identification and Method Identification. The output of phase one is a set of candidate objects that will serve as input for phase two, Class Abstraction. The Class Abstraction phase uses clustering techniques to form classes and define the concept of identical objects. The output of phase two is a set of classes that will serve as input to the third phase, Formation of the Inheritance Hierarchy. The Formation of the Inheritance Hierarchy phase defines a similarity measure which determines class similarity and further refines the clustering performed in phase two, Class Abstraction. The result of the methodology is an object-oriented design including hierarchy diagrams and interaction diagrams. Additionally, the results of applying the methodology in two case studies are presented.
The research has resulted in the development of a unique methodology to extract object-oriented designs from imperative legacy systems. The benefits of using the methodology include: the ability to capture system functionality which may not be apparent due to poor system structure, and the reduction of future maintenance costs of the system as a direct effect of accurate system documentation and updated programming technologies.
Chapter 1

Introduction

In recent years, much progress has been made in the area of software development. Specifically, the introduction and acceptance of the object-oriented paradigm has resulted in software systems exhibiting such desirable properties as code reuse, modularity, deferred commitment and a model that closely resembles the real world. However, "much of the software we depend on today is, on average, 10 to 15 years old" and written primarily in imperative languages, specifically COBOL or FORTRAN-77. Thus, the above benefits are not realized in these systems. Moreover, years of "patching" has resulted in systems that are poorly structured, coded and documented. It is clear that these systems will have to be "cleaned-up", however, the cost-factor makes it unlikely that these working systems will be simply discarded. Therefore, another approach must be taken [Osbo 90].

Reverse-engineering is recognized as a way to migrate old systems to new and improved technologies [Ulri 90]. By reverse-engineering a legacy system to take advantage of new technologies, the resulting system enjoys increased flexibility, increased productivity, and accurate system documentation. Additionally, it provides a better methodology for maintenance, allows rapid adaptation to changing requirements, and utilizes the benefits of new technologies and architectures [Roch 90]. The importance of this can be fully appreciated when it is realized that software maintenance consumes over 50% of the budget in most data processing.
shops [Your 89]. Therefore, the objective of this research is to develop a methodology to reverse-engineer such systems into the object-oriented paradigm, thereby aiding the migration of the system to newer coding practices and paradigms while utilizing system requirement information contained in the source code itself, but not appearing in any other documentation source. This research defines a reverse-engineering methodology to extract an object-oriented design representation from an imperative legacy system.

The remainder of this chapter presents an overview of the problem of software maintenance, introduces the relevant concepts and motivations, presents the objectives of the research and describes the organization of this dissertation.

1.1 Overview

The traditional forward-engineering software lifecycle of imperative systems includes several distinguishable stages: requirements analysis and definition, system design, implementation and testing, and operation and maintenance. Legacy systems are systems that are, on an average, over 10 years old. They were developed under the forward-engineering lifecycle model just described and currently exist in the operation and maintenance phase [Somm 89].

Software maintenance not only involves error-correction but also includes such activities as modification of requirements and design, thereby requiring further implementation. Moreover, what occurs, is that the entire development process is repeated many times during system maintenance as system modifications are made to the software. Maintenance costs are known to be the greatest cost incurred in
software development, averaging two to four times the development costs for large
embedded systems. It is noted that "maintenance costs tend to rise with program
age." Although maintenance costs tend to be less for systems that are well
documented, as maintenance activities continue, the quality and accuracy of system
documentation drops sharply. Therefore, systems that were well documented at
release time may be poorly documented 10 years later due to excessive maintenance
activities [Somm 89]. Rather than continue to nurse an antiquated system,
frequently the decision is made to extract the functionality of the system to utilize
new technologies while making the changes at a higher level of abstraction (i.e.,
system design or specification). The goal is to improve overall system quality,
decrease future maintenance costs, and satisfy current user needs. Reverse-
engineering is the mechanism by which the system functionality is extracted.
Specifically, it is the part of software maintenance "that helps you understand the
system so you can make appropriate changes." [Chik 90]

The purpose of reverse-engineering a system is to increase system
understanding or comprehensibility for maintenance and development. In addition,
research in the area of reverse-engineering addresses at least one of the following six
key objectives: cope with complexity, generate alternate views, recover lost
information, detect side-effects, synthesize higher abstractions, and facilitate reuse.
Reverse-engineering involves analyzing a system to "identify the system's
components and their interrelationships" and to "create a representation of the
system in another form or at a higher level of abstraction [Chik 90]." As the
connotations of reverse-engineering have changed from negative to necessary, there has been a concentration of research in the area. No longer is reverse-engineering clouded by the idea that it is an admission of failure because of the "get it right the first time" mentality. Today it is realized, and widely accepted that a software system is dynamic. "It is not possible to predict what you will want a system to do five, or even two years from now [Wate 94]." Therefore, by using the techniques of reverse-engineering to achieve an object-oriented design, the benefits of current software technologies can be realized without discarding a working system. [Chik 90]

Object-orientation is the amalgamation of three concepts: encapsulation, polymorphism and inheritance. Of these, only inheritance is unique to the paradigm. Encapsulation is realized as a "class" which is the implementation of an abstract data type. Classes are instantiated to give "objects" of the type, which form the basic run-time entity of the system. The object, which is the primitive element, can be viewed as an abstract data type, encapsulating a set of data (i.e. attributes) and a corresponding set of permissible actions on the data (i.e. methods). Each object is an autonomous entity which interacts with other objects during the execution of the system. Polymorphism is a property that permits a single message to refer, at run-time, to instances of different classes. Inheritance defines a relation between classes whereby the definition of a class is based on the definition of existing classes. It encourages the reuse of classes that are similar to what the programmer wants by allowing the programmer to tailor the inherited class(es) to meet the needs of the
inheriting class in a way that will not affect the inherited class(es). Thus, the combination of inheritance, polymorphism and dynamic binding localize required changes, thereby minimizing the amount of code that must be modified during software maintenance [Somm 89]. Other benefits of the object-oriented paradigm include code reuse, modularity, deferred commitment, and a model that closely resembles the real world [Pokk 89].

The research detailed in this dissertation is motivated by the following:

- The majority of scientific and engineering software systems currently in use are coded in imperative languages, specifically, FORTRAN-77.
- The object-oriented paradigm is well-suited for large-scale programming systems such as scientific and engineering systems, and provides a great opportunity for software reuse.
- The reverse-engineering of software systems allows the utilization of desirable system functionality for use in reengineering.

The goal of this research is to develop a methodology that facilitates system migration of legacy systems coded in FORTRAN-77 to the object-oriented paradigm. Additionally, the objectives of the research are as follows:

- Issues specific to FORTRAN-77, such as the COMMON block, should be addressed.
- Algorithms for each phase of the methodology should be detailed.
• A collection of design documents should be developed to represent the extracted design, such that the characteristics specific to reverse-engineering are addressed.

1.2 Outline of the Dissertation

The outline of the dissertation is as follows:

Chapter 2 presents related research in the area of reverse-engineering, specifically, object recovery. The relevance of the related work to the dissertation, as well as the distinction of the related work from the dissertation is presented.

Chapter 3 details the FORTRAN Object Recovery Methodology (FORM). It discusses each phase: pre-processing, object extraction, class abstraction and abstraction of the inheritance hierarchy. All necessary algorithms, definitions, and lemmas are presented. The representation of the object model is explained and the template for each diagram is given. The chapter concludes with a section on the validation and evaluation of FORM.

Chapter 4 presents the results of two case studies. Using two subject systems, one small-scale (less than 500 lines of code) and one medium-scale (1000 - 5000 lines of code) the FORTRAN Object Recovery Methodology (FORM) is demonstrated. Results from each phase of the methodology are presented.

Chapter 5 offers some concluding remarks and discusses possible future research directions.
Chapter 2

Related Research

In the context of software-engineering, reverse-engineering describes “the process of discovering how your own system works.” It involves many activities that all relate to the understanding and modification of existing software systems including creating high-level descriptions of a system. Because software systems are dynamic, it is not possible for a system to be permanently correct. This is evidenced in such factors as changing user needs and rapidly advancing hardware technologies. The rapid decrease in computer cost is making it possible for great advancements in both hardware and software technologies. For this reason, it is impossible to predict what users will expect from systems in the distant, and not-so-distant, future. For all of these considerations, reverse-engineering has been called “one of the most important areas of software engineering, rather than being a peripheral concern.” It is this realization that has sparked interest in the area and fueled the flame of research, which has resulted in conferences, such as the Working Conference on Reverse Engineering, which are devoted solely to reverse-engineering. The widespread appeal of object-oriented programming and the realization of the necessity of reverse-engineering as a software maintenance activity have motivated research in various aspects of the field [Wate 94].

Research in the area of reverse-engineering, specifically object recovery, is classified into five areas: code restructuring, program understanding, structure
identification, design & specification recovery, and system migration [Wate 94]. The remainder of this chapter will present the related research in each of these five areas and discuss the relevance of the related research to this research.

2.1 Code Restructuring

Code restructuring marks the beginning of research in the area of reverse-engineering. The purpose of code restructuring and the central theme of all reverse-engineering activity is program improvement. Code restructuring seeks to improve existing code by improving its understandability. Because unstructured program logic results in increased program complexity, code restructuring improves intellectual control over programs and makes reliable modification and software evolution feasible [Haus 90; Water 94].

The beginning of research in the area is marked by [Haus 90] and [Zimm 90] which detail the restructuring of COBOL and FORTRAN code, respectively. Hausler discusses the structuring of COBOL code to improve maintainability. By eliminating the constructs of Alter and Goto, a “top-down hierarchy of structured, single-entry, single-exit, procedures” is produced [Haus 90]. Zimmer presents a method for restructuring FORTRAN code into an object-oriented style. Zimmer’s research seeks to increase program clarity by establishing global invariants, reducing data cobwebs, and designing single objects. By emphasizing program invariants, the program structure is altered towards program function to create object modules. The resulting programs are written in object-module style and contain three kinds of modules: main, traditional, and object. The main module is the main program,
traditional modules contain only a single subprogram, and object modules contain one or more subprograms with an interface which may contain one or more variables. Thus, the object module style implements a particular object as a set of subprograms, and are, therefore, less general than data abstractions (which provide parameterization or object oriented programming (which provides inheritance). Although this method results in code which is not truly object-oriented, it marks the beginning of research along that path [Zimm 90].

2.2 Program Understanding

Program understanding, a key issue in reverse engineering, seeks to comprehend the underlying functional and data concepts of a system. Program understanding involves both syntactic and semantic analysis. Syntactic analysis in the most basic level of program understanding. It involves analyzing syntactic units such as variables, reserved words, strings and consonants as well as generating syntax trees. Semantic analysis provides a much deeper insight into program behavior detailing such information as control-flow and data-flow dependencies [Baum 93].

Research in the area of programming understanding has resulted in such projects as AMES [Baum 93], the Recognizer [Rich 93], COBOL/SRE [Engb 93], and DESIRE [Bigg 94]. An Extensible Maintenance Engineering System (AMES) was developed as a prototype of a semantics-based program understanding system for COBOL 74 programs. AMES uses denotational semantics and static program analysis techniques to develop tools that aid in semantic program understanding.
Semantic based tools provide a much deeper level of program understanding than syntactic based tools by supporting semantic level understanding through control-flow analyzers, data flow analyzers, and program slicers as opposed to parse trees and token lists. AMES designs and implements a prototype of a COBOL 74 software maintenance environment. It is composed of three parts: the maintenance engine, which is coded in Standard ML and consists of all the tools and methods; the user interface, which is coded in C++ as a stand-alone application running as a separate process; and the data store, which contains the parsed source code in the form of an abstract syntax tree extended with “containers” and “annotations” [Baum 93].

The Recoginzer is a prototype which finds occurrences of commonly used data structures and algorithms, defined as clichés, and builds a hierarchical description of the program. It was developed at MIT as part of the Programmer’s Apprentice project. The program under evaluation is first translated into a “language-independent graphical representation”, the Plan Calculus. It is then encoded as a flow graph and parsed to produce a design tree. Finally, documentation is generated [Rich 93].

The COBOL/SRE (COBOL System Renovation Environment) project is a software re-engineering environment for COBOL systems. It was developed by Andersen Consulting’s Center for Strategic Technology Research. COBOL/SRE was developed as a set of tools to address the problem of “identifying and extracting components from large legacy COBOL systems” based on the concepts of reusable
component recovery. Reusable component recovery represents one of several approaches in dealing with legacy systems. In reusable component recovery, functional components of the system are “recognized, recovered, adapted, and finally reused in new system development.” This approach requires deep analysis and understanding of the legacy code. To this end, COBOL/SRE includes such components as system level analysis, data model recovery, concept recognition and program level analysis. The system-level analysis includes system inventory, system analysis, and system browsing capabilities. The data model recovery component identifies a virtual data model based on analysis performed on data record mappings, data assignments, and data flows. The concept recognition component uses “plans” to “describe parts and constraints among parts of concepts to be recognized.” Finally, the program-level analysis component assists program analysts in program understanding activities by providing parsing and program text browsing, flow analysis, complexity analysis and anomaly detection, and program segmentation. COBOL/SRE uses such features as condition-based slicing, forward slicing/ripple-effect analysis, segment management and composition operations, and knowledge based concept recognition to facilitate system level analysis and browsing, syntactic analysis, semantic analysis, data model recovery, and distributed execution architecture in reusable software component recovery from legacy COBOL systems [Ning 94].

The DESIRE (DESign Information Recovery Environment) system is a suite of tools that uses informal information (comments, identifier names, design documents)
rather than formal information (syntax trees and program semantics) to aid in program understanding, specifically addressing the concept assignment problem. The concept assignment problem is defined as "the problem of discovering these human-oriented issues and assigning them to their realizations within a specific program or its context." DESIRE is a program-understanding assistant containing facilities to assist the user in addressing the concept assignment problem. These facilities include three scenarios: suggestive data names, patterns of relationships, and intelligent agent. Scenario one, suggestive data names, assigns key concepts to specific program concepts to provide a framework whereby a human reverse engineer may perform further detailed analysis. Scenario two, patterns as relationships, identifies "clusters of related functions and data that form the framework of the program." Scenario three, intelligent agent, allows the user to browse the code looking for "evidence of key concepts based on the user's experience." DESIRE has been used for "exploration for debugging or porting," and "documentation for understanding and reporting" [Bigg 94].

2.3 Structure Identification

Structure identification is the process of determining static properties of a software system. Research in this area includes such projects as RE², data-flow-diagram (DFD) extraction, program graph models, and the FORTRAN Reverse-Engineering package.

Bendusi, et. al. describe the development of a methodology to extract low level design documents from Pascal code using Transformation Analysis. The
methodology produces structure charts and data-flow diagrams using JSP and Warnier-Orr methodologies [Bend92]. The RE\textsuperscript{2} project explores "reverse-engineering and re-engineering techniques to facilitate reuse re-engineering." The project uses functional and data abstraction to extract reusable components from existing systems. Additionally, it seeks to introduce abstract data types into languages that do not make any provisions for the implementation of abstract data types [Canf 93]. Cimitile introduces an algebraic representation of program modules to generate program graph models. Using these program graph models, a flow-graph, a nesting tree of program control structures, and a tree of program paths are produced from software coded in FORTRAN, COBOL or Pascal [Cimi 91]. Finally, the Fortran Reverse Engineering package analyzes FORTRAN code and produces structure charts and module specifications [Gili 90].

Each of these research efforts extracts static components from source code. They do not modify or interpret the extracted data. This extraction process does not provide the deeper comprehension that program understanding offers, but rather serves as a preliminary stage of program understanding. Additionally, program understanding and structure identification serve as preliminary stages to object recovery.

2.4 Design & Specification Recovery

A software design is a description of the software system [Pfle 91]. It is the process of "producing a description of implementation from which source code can be developed [Ruga 90]" A software specification, on the other hand, is a
description of the systems capabilities [Pfle 91]. Both software specification and design are vital components of the forward engineering lifecycle. They are vital documentation that represents the system. However, as previously discussed, because legacy systems have undergone years of extensive maintenance, what was originally accurate specification and design documentation typically is no longer accurate. Therefore, a key objective of reverse engineering is recovery of lost information, specifically, system specification and design [Chik 90]. There have been numerous research efforts in design and specification recovery including such projects as REDO, RECAST, NuMIL and RIGI [Lano 93; Edwa 93; Choi 90; Till 93].

Choi & Sacchi explore the extraction of the functional and dynamic properties of large systems and develop a process to reverse-engineer system level design description. They developed a module interconnection language, NuMIL, which is used to represent the extracted design [Choi 90]. Liu & Wilde propose a methodology to recover object-like features from a non-object oriented system. The methodology uses features such as abstract data types to identify object-like features using persistent data and formal parameters [Liu 90]. Lividas & Roy extend this research by introducing the concept of the receiver of a procedure. Thus, the research is extended to explore the object-like features in receivers [Livi 92].

Sward & Steigerwald have developed a two-phase methodology to reverse-engineer procedural code into natural language. Phase one describes the data
structures in three steps: list the data structures, list where the data structures are
defined, and write a natural language description of the data structures. Phase two
uses a five step procedure to describe the procedures of the system. Phase two
involves the following steps: list all procedures in the system, list the parameters for
each of these procedures, consider each data structure individually, list the parts of
the data structure that each procedure uses and write natural language descriptions
for each procedure. They claim that by extracting a natural language description of
the source code, that the forward-engineering process will allow the system to be
implemented in the object-oriented paradigm [Swar 94].

The RECAST project was carried out at the Centre for Software
Maintenance, University of Durham, as part of the DTI/ED project under the
Information and Engineering Advanced Technology program supported by a SERC
grant. The RECAST (Reverse Engineering into CaSe Technology) methodology
extracts a SSADM (Structured Systems Analysis and Design Method) from
COBOL code. Thus, the project extracts a procedural design from legacy COBOL
code. The RECAST framework has four phases: population of the repository,
preliminary transformations, logical restructuring, and translation into SSADM
notation. Phase one parses the source code and generates PSL statements to
populate the PSL/PSA repository of SSADM. Phase two resolves any naming
difficulties (synonyms and homonyms) and carries out preliminary transformations
on the source system. Phase three is the heart of RECAST. During this phase, a set
of transformations is used to restructure the repository descriptions while

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maintaining system functionality. Finally, phase four translates the meta language description of the system into SSADM. The final output is the set of documents required for SSAMD's Physical Design phase [Edwa 93].

The RIGI project involves such concepts of reverse-engineering as software analysis and program understanding to identify software artifacts and form an abstract representation of the system. RIGI discovers and analyzes the structure of large software systems in two phases. Phase one involves the automatic and language-dependent extraction of software artifacts. This is performed by parsing the source code and storing the artifacts in a repository. Phase two involves semi-automatic and language independent "subsystem composition methods that generate hierarchies of subsystems." That is, using the variables, procedures, modules, and subsystems to construct software components [Till 93; Mull 94].

Subramaniam and Byrne strive to derive an object model from legacy FORTRAN code. Using application domain knowledge and system artifacts including documentation and source code they define a nine-step process involving both top-down and bottom-up approaches. The process includes identifying potential objects and classes, mapping objects to classes, identifying attributes, identifying methods, and determining relationships [Subr 96].

In addition to design recovery, there have been several projects dedicated to the recovery of a system specification. Such projects include REDO, REFORM and a methodology introduced by Gannod & Cheng. The aim of the REFORM (Reverse Engineering using FORmal Methods) project is to develop a formal specification in
Z from legacy IBM Assembler code. This project was conducted at the Centre for Software Maintenance at the University of Durham as part of research funded by IBM(UK), DTI, and SERC. The REFORM system uses a three phase methodology to transform the source code into a specification. Phase one uses a source to wide-spectrum language (WSL) translator to translate the assembler into an intermediate form. It produces code modules and the relations among the modules and stores this information in a database. Phase two involves using the code stored in the database and working interactively with the program transformer to produce a specification. Again, the resulting code is stored in the database. The third and final phase uses a program integrator to assemble the code in a WSL and translate this specification in WSL to a Z specification [Yang 91].

The REDO (Reengineering, Documentation and validation of systems) project was conducted at Oxford University by the Programming Research Group (PRG) as part of funded research known as the ESPRIT project. The goal of the REDO project was to reverse-engineer COBOL to the formal specification language, Z. This was done via an intermediate language, Uniform, and a functional description language. Further research in the project included the development of the object-oriented specification language Z++ and the development of a methodology to extract the object-oriented components of COBOL and represent those components in Z++ [Lano 93].
2.5 System Migration

System migration involves the transformation of a software system from one language to another. Bryne discusses the development of a methodology to develop an Ada implementation from a FORTRAN code and update the documentation. The methodology involves extracting detailed design information from the FORTRAN source code. From the detailed design, a high level design is extracted and represented by data-flow and control-flow diagrams. The following eight-step procedure to extract the design is presented: collect information, examine information, extract the structure, record functionality, record data-flow, record control-flow, review recovered design, and generate documentation. The recovered design is then implemented in Ada and new documentation is produced [Bryn 91].

Ong & Tsai have developed a methodology to translate FORTRAN code to class-based C++ code. They examine aggregated data structures and subprogram parameters to help facilitate the translation. Data flow analysis is used to gather information on program variables. Using this information, subprograms are analyzed for objects in global variables, local variables and formal parameters. Methods are extracted based on a heuristic that determines data usage by defining three categories: use-only, use-and-set, and define-only. Based on the classification of the variables, methods are defined which read the object's state, create the object (constructor), or modify the object's state [Ong 93].
2.6 Relevance to the Dissertation

The research presented in the dissertation serves to extend and enhance the body of research discussed in this chapter. It spans several areas of reverse-engineering including program understanding and structure identification with major emphasis in the area of design and specification recovery. The methodology presented in the dissertation has similar theoretical foundations to the research presented, however there exists some fundamental differences. These similarities and differences are detailed in Figure 2.1. In the related research, only [Liu 90; Liva 92; Lano 93; Ong 93; Subr 96] seek to obtain object-oriented characteristics from non-object-oriented code. [Lano 93] focus strictly on COBOL source code, and therefore, does not deal with many of the issues encountered with FORTRAN. [Liu 90; Liva 92; Ong 93] each seek to extract object characteristics from non-object-oriented code, but use abstract data types as the basis of forming these object groupings. These methodologies fall short for FORTRAN because of its lack of abstract data types and user defined types. Therefore, although other methodologies may also take a data-driven approach to extraction of objects, the data elements that are considered are vastly different. Thus, the methodology presented in the dissertation expands and enhances the current body of research by increasing the domain of applicability of object recovery methodologies. This is exemplified in [Subr 96], which references and is based upon the research contained herein, and specifies C++ as the language of implementation.
<table>
<thead>
<tr>
<th>Methodology</th>
<th>Source Language</th>
<th>Data Structures</th>
<th>Class Extraction</th>
</tr>
</thead>
<tbody>
<tr>
<td>REDO</td>
<td>COBOL</td>
<td>required</td>
<td>yes</td>
</tr>
<tr>
<td>RECAST</td>
<td>COBOL</td>
<td>required</td>
<td>no</td>
</tr>
<tr>
<td>Ong &amp; Tsai</td>
<td>FORTRAN</td>
<td>not required</td>
<td>methods only; class-based C++ methods only</td>
</tr>
<tr>
<td>Liu &amp; Wilde</td>
<td>COBOL</td>
<td>required</td>
<td></td>
</tr>
<tr>
<td>FORM</td>
<td>imperative</td>
<td>not required</td>
<td>yes</td>
</tr>
</tbody>
</table>

**Figure 2.1**
Comparison of Related Research
Chapter 3

FORM: The FORTRAN Object Recovery Methodology

The methodology detailed in the dissertation is a three phase methodology for extracting an object-oriented design from imperative code, specifically FORTRAN-77. The FORTRAN Object Recovery Methodology (FORM) consists of a pre-processing phase to restructure the source code, resolve the aliases in the global variables and actual parameters, and resolve the COMMON block followed by Object Extraction, Class Abstraction and Formation of the Inheritance Hierarchy. An overview of the methodology is given in Figure 3.1. The result of FORM is an object-oriented design including hierarchy diagrams and interaction diagrams.

3.1 Pre-processing

The pre-processing phase is necessary to “clean up” the source code so that it may be evaluated accurately for object extraction. There are two types of preprocessing that must occur: actual parameters and global variables. The actual parameters must undergo a pre-processing phase to resolve any aliasing that occurs with the formal parameters. The global variables must undergo a pre-processing phase to resolve aliasing and to determine which variables serve only as placeholders. This pre-processing phase results in code that is ready to be analyzed for object extraction.
Figure 3.1
Overview of FORM
**Input:** Call graph of the source code represented as a tree with \( n \) levels

where the formal parameters, and actual parameters for each node

are maintained in two lists: formal and actual.

**Output:** Call graph of the source code with aliasing resolved.

1. Begin at the root node and traverse the tree using a depth first traversal.

2. For each node, maintain the following lists:
   - formal\([i,k]\): the list of formal parameters
   - actual\([i,j]\): the list of actual parameters

where: \( i = 1..n \) is the level in the tree

   \( j \) is the number of actual parameters

   \( k \) is the number of formal parameters

3. for \( i = 1..n \) do
   
   \( j = 1 \)

   while actual\([i,j]\) <> eol do
     
     \( k=0 \)

     while formal\([i,k]\) <> eol do
       
       if actual\([i,j]\) = formal\([i,k]\)
       then actual\([i,j]\) = actual\([i-1,j]\]
       
       od

     od

   od

---

**Figure 3.2**

Algorithm to Resolve Actual Parameter Aliasing
3.1.1 The Aliasing Problem — Actual Parameters

Because the first phase of the extraction process involves the analysis of the actual parameters, it is important that a single name of an actual parameter corresponds to a unique data element. That is, when the subroutine calls are considered independently of the source code and the call graph, no aliasing should occur. This is not the case, however. Because of the scoping rules of FORTRAN, as well as most imperative languages, the data element that is referenced in a subroutine call is based not only on the subroutine issuing the call, but also the order of nesting of the subroutines in the call graph.

There are two instances when the aliasing of parameter names in the subroutines occurs: (1) local variables of the same name in different subroutines are used as actual parameters, and (2) actual parameters and formal parameters have the same names and nested calls occur. Before any type of analysis is performed, the calling sequence must be considered. Thus, the call graph is used to give unique names to variables referencing a single location.

To solve the problem of local variables of the same name in different subroutines used as actual parameters, the name of the subroutine of declaration is attached in a dot notation to the beginning of each local variable. The source code is updated with the new variable names and uniqueness is guaranteed. To solve the problem of aliasing that occurs when actual parameters have the same names as formal parameters, the call graph is necessary. Using the call graph, mappings are determined as follows: when a call is issued by SUB1 to a subroutine SUB2, and
SUB2 issues a call to SUB3 where the name of a formal parameter appears in as an actual parameter, the actual parameter in SUB2 is replaced by the corresponding actual parameter of the calling subroutine, SUB1. Considering the call graph as a tree with the main program as the root, the resolution proceeds in a top-down manner. Beginning at the root node, list the mapping of actual parameters to formal parameters for each call. Traverse the tree in a depth-first manner. Maintain the mapping for all actual parameters to formal parameters. For each node, replace all occurrences of formal parameters in the call statements with the corresponding actual parameters and derive the actual parameter to formal parameter mapping for the next node in the sequence. The algorithm to resolve the actual parameter aliasing is given in Figure 3.2.

Thus, the aliases have been resolved, and attribute extraction can proceed. Using the resolved call statements the actual parameter lists are evaluated and attributes extracted.

3.1.2 Determining Placeholder Variables

To facilitate the identification of objects in the COMMON block, the first step is to determine, for each COMMON statement, which variables are actually used and which variables are serving as placeholders, i.e. variables not referenced or defined in the subroutine. This determination is done by analyzing the program unit over which the COMMON statement is valid (for each COMMON statement) using data reference analysis techniques. The algorithm to detect placeholders is given in Figure 3.3.
Let P be a FORTRAN program and let C be the COMMON area where

\[ C = \text{union of all } C_j, j = 0 \ldots k \text{ where} \]

- \( C_0 \) is unnamed
- \( C_i \) is a uniquely named COMMON, \( i = 1 \ldots k \).

Consider all references to the COMMON areas, and assume that there are \( m \geq 0 \) such references.

Let \( A_n, n = 1..m \), be a reference to the common area, and

Let \( B_n, n = 1..m \), be the program block over which \( A_n \) is valid

Let \( D_n, n = 1..m \), be the set of placeholders of \( A_n \).

Define \( \text{ref}[n] = \) the set of variables of \( A_n \) that are referenced in \( B_n, n = 1..m \).

Define \( \text{def}[n] = \) the set of variables of \( A_n \) that are defined in \( B_n, n = 1..m \).

Then, \( \text{Union}(\text{ref}[n], \text{def}[n]) = \) the set of all variables of \( A_n \) that are referenced directly in \( B_n \), and

\[ D_n = A_n \setminus \text{Union}(\text{ref}[n], \text{def}[n]) = \text{the set of all placeholders of } A_n \].

**Figure 3.3**

*Algorithm to Determine Placeholders*

The placeholders are determined using the use and defines lists. For each reference to a COMMON area, the union of both the use and defines lists is
determined. This represents all COMMON variables that are not placeholders in
the subroutine for that reference. Using set subtraction, the non-placeholder
variables are subtracted from the list of all COMMON variables for the reference
leaving the set of placeholder variables for the reference. Hence, by computing
variable usage for each COMMON statement, and excluding the set of used
variables from the set of all variables, the set of variables acting as placeholders is
determined.

3.1.3 Resolving the Aliases

When a COMMON statement is used there is a risk of aliasing. Variables
specified to be in the COMMON area are available to all program modules in which
the corresponding COMMON statement appears. The problem of aliasing occurs
because the variable names associated with the COMMON area may be different in
the main program and each subroutine. Because the position of a variable in the
COMMON statement determines the memory location to which it maps, and
because unique variable names can be used in each module, it is possible that in each
module, different names are given to a single memory location, i.e. aliasing. To
accurately identify the objects, these aliases must be resolved. Therefore, the second
step is to resolve the aliases to the COMMON block. There are essentially two
approaches that can be taken to perform the resolution: (1) brute force and (2)
computational.
3.1.3.1 The Brute Force Method

One method for resolving the aliases of the COMMON block is simply "brute force." This method enumerates each element of the COMMON statements and proceeds to match variables position by position. This method works, but is tedious, slow and not very elegant. Arrays must be enumerated and matched element by element.

Example:

Given the following primary COMMON statement:

```
COMMON     r1, r2, A[2, 3], r3
```

and the following candidate COMMON statement:

```
COMMON     s1, s2, s3, s4, s5, B[2, 2]
```

enumerate as follows:

```
COMMON     r1, r2, A[1,1], A[2,1], A[1,2], A[2,2], A[1,3], A[2,3], r3
COMMON     s1, s2, s3, s4, s5, B[1,1], B[2,1], B[1,2], B[2,2]
```

and match the variables position by position:

```
(s1, r1), (s2, r2), (s3, A[1,1]), (s4, A[2,1]), (B[1,1], A[1,2]), ... etc.
```

3.1.3.2 The Computational Method

The alternative method provides a more elegant solution. This method begins matching positions and upon reaching an array, computes the offset required for its resolution. This method avoids the enumeration of each array.

Since the resolution is performed on a syntactically correct program, we can assume that there are no type conflicts in the COMMON statements since this...
would result in a syntax error. Let the COMMON statement in the main program
serve as the COMMON statement to which all others will be resolved, and refer to it
as the "primary COMMON statement." As resolution is being performed on a
COMMON statement, it will be referred to as the "candidate COMMON
statement." Once resolution is performed on a COMMON statement it is referred to
as a "resolved COMMON statement."

Let the primary COMMON statement be of the form: COMMON \( v_1, v_2, \ldots, v_p \).

Let the candidate COMMON statement be of the form: COMMON \( w_1, w_2, \ldots, w_c \).

A function, \( f \), that will map a variable from the candidate COMMON
statement to a variable in the primary COMMON statement is defined using
separation of case. There are four cases that must be considered in alias resolution
of the COMMON block:

1. No arrays are present in the primary or candidate COMMON statements.
2. Arrays are present in the primary but not the candidate COMMON
   statement.
3. Arrays are present in the candidate but not the primary COMMON
   statement.
4. Arrays are present in both the primary and candidate COMMON
   statements.
Consider case 1, the case when there are no arrays present in either the primary COMMON statement or the candidate COMMON statement. This is the most trivial case in that each variable listed in the candidate COMMON statement will correspond directly to a variable listed in the primary COMMON statement, and, as discussed before, no type consideration is necessary. For all i, 1..p, \( v_i \) is not an array and for all j, 1..c, \( w_j \) is not an array. Then for \( k = 1..c \), \( f(w_k) = v_k \). Thus, the mapping is direct, i.e. the variables of the candidate COMMON statement are mapped to the variables in the primary COMMON statement that occupy corresponding positions in the statements.

Next, consider cases 2 and 3, when arrays appear in either the primary COMMON statement or the candidate COMMON statement but not both. When an \( nxm \) array is reached in the primary (resp. candidate) COMMON statement, \( mn \) consecutive locations are assigned in column major manner, i.e. (1,1) (2,1), (3,1) ... (1,2), (2, 2) etc. Map the array to \( nm \) locations in the candidate (resp. primary) COMMON statement. That is to say, if the array is in the primary COMMON statement, \( mn \) variables in the candidate COMMON statement will be mapped to the array name. If the array appears in the candidate COMMON statement, then the array will be renamed to the \( nm \) corresponding variables in the primary COMMON statement.

More specifically, consider case 2, when arrays are present in the primary COMMON statement. For some i, 1..p, \( v_i \) is an array, and for all j, 1..c, \( w_j \) is not an array. Then define a function \( g \) such that
\[
g(v_i) = 1 \quad \text{if and only if } v_i \text{ is not an array and}
\]
\[
= mn \quad \text{if and only if } v_i \text{ is an nxm array},
\]

Then \( g(v_i) \) is the number of locations allocated in the primary COMMON statement. If \( v_i \) is an array, further note the elements of \( v_i \) as \( v_i\{\text{row, col} \} \). Now consider \( w_k \), the \( k^{th} \) element in the candidate COMMON statement. Then find a \( z \), \( z > 0 \), such that \( g(v_i) = k \), if such a \( z \) exists. If there exists such a \( z \), then \( f(w_k) = v_z \) if \( v_z \) is not an array, and \( f(w_k) = v_z\{n,m\} \) if \( v_z \) is an array. If no such \( z \) exists, then find \( y \) such that \( g(v_i) = \text{glb}(k) \), where \( \text{glb}(k) \) is the greatest integer less than \( k \). Let \( l = \text{glb}(k) \) and define \( t = k-l \). Since \( v_{y+1} \) is an array, we must define \( f \) such that \( w_k \) is mapped to a particular element of \( v_{y+1} \). Let \( c = \text{TRUNC}((t-1),n) \) and let \( d = \text{MOD}((t-1),n) \). Then \( f(w_k) = v_{y+1}\{d+1, c+1\} \).

Now, consider case 3, where arrays are present in the candidate COMMON statement, but not the primary COMMON statement. Let \( w_k \) be an nxm array and \( v_h \) is not an array. Then we must define \( f \) such that \( w_k \) is mapped to \( v_h, v_{h+1}, ..., v_{j+nm-1} \). Therefore, \( f(w_k\{i,j\}) = v_{(h-1) + (j-1)n + i} \).

Finally, consider case 4, when arrays appear in both the primary and candidate COMMON statements, two subcases are possible: (i) the arrays have equal dimension, (ii) the dimension of the array in the primary COMMON statement is greater than the dimension of the array in the candidate COMMON statement. We consider only the case where the array in the candidate COMMON statement does
not exceed the boundaries of the array in the primary COMMON statement. If the array dimensions are equal, then this reduces to the trivial case. The mapping between the two arrays is direct. If the dimensions of the arrays do not match, specifically, if the dimension of the primary array is greater than the dimension of the candidate array, then the resolution becomes more complex.

Let A be an array in the primary COMMON statement with dimension mn, and let B be an array in the candidate COMMON statement with dimension ij such that mn > ij. In the general case, B is an alias to some ij locations of A, not necessarily beginning at A[1,1] or ending with A[n,m]. Thus, B may reference the ij "middle" locations of A, such that r+ij+s = mn for some 0 < r <= mn, 0 < s <= mn. Pictorially,

```
|------------------- nm -------------------| array A[n,m]
|-----r-----|----- ij -----|----- s -----| array B[i,j] aliases a subset of A.
```

It is necessary to determine exactly which segment of A is aliased by array B because of the possibility of dummy variables representing a portion of A. The algorithm to resolve the COMMON block using the computational method is given in Figure 3.4. It should be noted that the resolution method involves two-dimensional arrays, but is easily adapted to one-dimensional arrays by letting m = 1, i.e. setting the number of columns equal to 1.
1. Determine the size of the array in the primary COMMON statement, i.e. mn, and call this value "size\_primary"

2. Determine the size of the array in the candidate COMMON statement and call this value "size\_candidate"

3. Compute \( x = \text{TRUNC}(r/n), \quad y = \text{MOD}(r/n) \)

4. The variables in the \( r \) locations alias \( A[n,x] A\{1..y, x+1\} \) (note: the notation \( \{ \} \) is used to denote only a single column of an array, while \( [\] \) is standard array notation).

5. Compute \( u = n - y \).

\( (u \) is the number of locations necessary to complete the column started by the \( r \) variables.\)

6. If \( u < ij \) then \( A\{y+1..n, x+1\} \) denotes the remainder of the column.

\( (i.e. y+1...n \) is \( u \) rows of column \( x+1).\)

Compute the following:

\[
c = \text{TRUNC}(ij-u / n), \quad (c = \) the number of complete columns of \( A \) included in \( B)\)
\[
d = \text{MOD}(ij-u / n), \quad (d = \) the remaining number of slots of \( A \) included in \( B)\)
\]

If \( c > 0 \) then the remainder of \( B \) aliases \( A\{n , (x+2) ... (x+2+c-1)\} A\{d, (x+2+c)\}\)

else \( (c = 0) \) \( B \) aliases \( A(d, (x+2) )\)

7. If \( u = ij \) then \( A\{y+1..n, x+1\} \) is the aliased positions of \( A \), i.e. the remainder of the column

8. If \( u > ij \) then \( A\{ (y+1) ... (y+1+ij), (x+1) \} \) denotes the alias of array \( B \).

\( (i.e. a \) portion of the \( x+1 \) column of \( A).\)

9. The next \( s \) variables in the candidate COMMON statement alias the next \( s \) locations of \( A\).

\[
f(w_j) = A\{(y+1)...n, (x+1)\} A\{n, (x+2)...(x+2+c-1)\} A\{d,(x+2+c)\}\]

if and only if \( u < ij \) and \( c > 0 \)

\[
f(w_j) = A\{(y+1)...n, (x+1)\} A\{d, (x+2)\} \) if and only if \( u < ij \) and \( c = 0 \)
\]

\[
f(w_j) = A\{(y+1)...n, (x+1)\} \) if and only if \( u = ij \)
\]

\[
f(w_j) = A\{(y+1)...(y+1+ij), (x+1)\} \) if and only if \( u > ij \)
\]

and \(f(w_{j+1}) = A\{d+1, x+2+c\} \) if and only if \( u < ij \) and \( c > 0 \)

\[
f(w_{j+1}) = A\{d+1, x+2\} \) if and only if \( u < ij \) and \( c = 0 \)
\]

\[
f(w_{j+1}) = A\{1, x+2\} \) if and only if \( u = ij \)
\]

\[
f(w_{j+1}) = A\{(y+1+ij)+1, x+1\} \) if and only if \( u > ij \)
\]

and \(f(w_{j+k}) = A\{((d+k-1) \text{ mod } n)+1, (x+2+c) + ((k-1)\text{TRUNC}(n)+1) \) for \( k = 1...s\)

---

**Figure 3.4**

Algorithm for COMMON Block Resolution
Notation:

$A_{\{1..2, 3\}}$ represents the elements $A[1,3], A[2,3]$

$A_{\{2,3\}}$ represents the single element $A[2,3]$

$A[2,2]$ represents the elements $A[1,1], A[2,1], A[1,2], A[2,2]$

$A_n$ includes all COMMON statements, both named and unnamed. Since alias resolution must be performed on COMMON statements that access the same area, i.e. those with the same name or no name at all, it is necessary to partition $A$ into $k+1$ disjoint sets where each set contains all COMMON statements that access the same area of the COMMON block. Thus, there will be $(k+1)$ primary COMMON statements, one for each of the $(k+1)$ sets. When performing the resolution, it is necessary to use the primary COMMON statement for the set to which the candidate COMMON statement belongs.

At this point, the preprocessing phase is completed. The placeholders have been determined and the aliases have been resolved. The source code is prepared for the object extraction phase.

3.2 Object Extraction

The Object Extraction phase is divided into two stages: Attribute Identification and Method Identification. Attribute Identification uses a data-driven bottom up approach to analyze two aspects of the source code: actual parameters and global variables. Method Identification uses a new variation of traditional program slicing techniques to extract methods based on an object's attributes. The
output of the Object Extraction phase is a set of candidate objects that will serve as input to phase two, Class Abstraction.

An object, O, is identified as a two-tuple, (D,M) where D is the set of data items (or attributes) and M is the set of methods that act on those data items. Two possible approaches to object extraction are top-down or bottom-up. A top-down approach begins with all data elements contained in a single object and proceeds to divide the object into smaller objects. Although this approach has some merit, the margin of error is on the side of objects whose attribute sets are too small, i.e. they do not adequately represent a functionally cohesive unit. The bottom-up approach constructs objects by first determining the cohesive strength between each pair of data items and proceeds to form groupings based on levels of cohesion. Because a bottom-up approach results in objects that are highly cohesive, this is the approach taken by FORM.

The functionality of a program is viewed at three levels. At the top-level, the functionality is that of the entire program. This view is too coarse grained to directly aid in object extraction, however, it may provide some insight into the type of objects that may be formed. The second level concentrates on the functionality of the individual subroutines. The third, and most fine-grained view, considers the functionality of each line of code. The view of the subroutine as the unit of functionality is the approach taken in this work. The consideration of the subroutine as the unit of functionality of the analysis facilitates the evaluation of two aspects of program variables: actual parameters and global variables.
3.2.1 Attribute Extraction — Actual Parameter Analysis

By considering each subroutine as a unit of functionality, the actual parameters are then necessary to perform the function of the given subroutine. Based on these guidelines, FORM seeks to obtain the largest set of parameters representing the strongest cohesive unit. The cohesive strength of a pair of parameters is measured by determining the frequency in which they are both necessary for the execution of a function (where the subroutine is the unit of functionality). Measuring the cohesion of a pair parameters for a given subroutine results in the consideration of three cases:

(i) both parameters are necessary,
(ii) only one parameter of the pair is necessary, and
(iii) neither parameter is necessary.

The cohesion value of a given pair of parameters is affected by each case as follows: case (i) increases the cohesive value, case (ii) decreases the cohesive value, and case (iii) does not affect the cohesive value. A cost function, i.e. a function that maps each pair of parameters to a real number, is defined for a pair of parameters i and j with respect to subroutine f. Using a greedy approach results in a cost function, c, that, for a given pair of parameters, weights the necessity of both parameters of the pair as a stronger condition than the necessity of only one parameter of the pair. Therefore, the cost function is increased by .2 when both parameters are necessary for the execution of f, and only reduced by .1 when only one parameter is necessary for the execution of f. By adjusting the amount c is increased or decreased, the
"greediness" of the approach is determined. Thus, the cost function, c, for a pair of parameters i and j with respect to subroutine f is as follows:

\[
c(i,j) = \begin{cases} 
  c(i,j) & \text{if and only if neither } i \text{ nor } j \text{ is necessary for the execution of } f \\
  c(i,j) + .2 & \text{if and only if both } i \text{ and } j \text{ are necessary for the execution of } f \\
  c(i,j) - .1 & \text{if and only if either } i \text{ or } j \text{ (but not both) is necessary for the execution of } f 
\end{cases}
\]

A bottom-up approach is used to construct a graph that maintains the value of the cost function, c. This graph is represented as a weighted adjacency matrix, M, i.e. an adjacency matrix whose entries are real numbers. M[i,j] is assigned a value based on the result of the cost function, c(i,j). Thus, the value assigned by the cost function c(i,j) is stored in M[i,j] and is proportional to the degree of functionality by which i and j are related. Once the matrix, M, is instantiated, a threshold table is determined. A threshold table consists of two columns: threshold value and data sets. The threshold value is a non-negative real number that is determined from M as follows: for each non-negative real number in M, add a row to the threshold table with that value as the threshold value. For each threshold value, corresponding data sets are computed using the transitive closure algorithm. From this table, a "desirable" threshold level is determined by the human reverse engineer. In selecting a desirable threshold level, the goal is to find the largest data sets with the strongest cohesion, thereby minimizing the number of
singletons. By setting a threshold on the value necessary to be considered relevant, the set of data contained in an object is determined. One benefit of this representation is that it facilitates the consideration of various sets of objects based upon varying the threshold.

<table>
<thead>
<tr>
<th>Step 1.</th>
<th>Resolve aliasing of local variables</th>
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<tr>
<td>Step 2.</td>
<td>Resolve aliasing of actual parameters</td>
</tr>
<tr>
<td>Step 3.</td>
<td>Perform parameter analysis on the call statements generated in Step 2 and generate a weighted adjacency matrix using the cost function, c.</td>
</tr>
<tr>
<td>Step 4.</td>
<td>Generate the threshold table.</td>
</tr>
</tbody>
</table>

**Figure 3.5**

**General Algorithm for Attribute Extraction from Actual Parameters**

The general algorithm for attribute extraction from actual parameters is shown in Figure 3.5. This four-step procedure inputs the raw source code and performs two resolution steps: resolve all local variables, and resolve the actual parameters. Once the raw source code has been resolved, the resolved source code is analyzed and a weighted adjacency matrix, M is generated using the algorithm in Figure 3.6. The threshold table is then generated from M using the transitive closure algorithm. It is at this point that the human reverse engineer determines an appropriate threshold level, thereby determining the data sets for the candidate
Let \( P \) be a structured FORTRAN program
With \( n \) subroutine calls
And \( m \) (distinct) actual parameters

(i) For \( i = 1 \) to \( n \) do
    \( \text{CALL}_i = \text{set of actual parameters of subroutine call } i \)
    If subroutine \( i \) is a function
        Then \( \text{CALL}_i = \text{CALL}_i \) union with the function resultant of subroutine \( i \)
    od

(ii) Let \( G = (V,E) \) be a graph
    \( V = \) the arbitrary ordered set of actual parameters and function resultants.
    and denote the elements of \( V \) as \( v_1, v_2, \ldots, v_m \) /* note \( |V| = m *\)
    \( E = \{\} \)

(iii) \( M[1..m, 1..m] \) ARRAY of REAL /* a weighted adjacency matrix */
     \( AP[1..n, 1..m] \) ARRAY of BOOLEAN /* \( n \) sets of actual parameters */
     /* Construct the graph, represented as a weighted adjacency matrix */
     /* Initially \( G \) consists of only a set of vertices with no edges */
    For \( i = 1 \) to \( m \) do
        For \( j = 1 \) to \( m \) do
            \( M[i,j] = 0 \)
        od
    od
    /* Initialize the sets of actual parameters; \( AP[i,j] = 1 \) if and only if \( v_j \) is an element of \( \text{CALL}_i \)
    For \( i = 1 \) to \( n \) do
        For \( j = 1 \) to \( m \) do
            If \( v_j \) is an element of \( \text{CALL}_i \)
                Then \( AP[i,j] = 1 \)
            Else \( AP[i,j] = 0 \)
        od
    od
    /* Perform the analysis on the sets \( AP \) */
    For \( i = 1 \) to \( n \) do
        For \( j = 1 \) to \( m \) do
            For \( k = j+1 \) to \( m \) do
                If \( AP[i,j] = 1 \) and \( AP[i,k] = 1 \) /* both parameters are necessary*/
                    Then \( M[j,k] = M[j,k] + 0.2 \)
                Else if \( AP[i,j] = 0 \) and \( AP[j,k] = 0 \) /* inconclusive */
                    Then skip
                Else \( M[j,k] = M[j,k] - 0.1 \) /* only one is 0 */
            od
        od
    od

(iii) The output is \( r \leq n \) connected graphs. The vertices of each connected graph represents
the number of attributes for a distinct candidate object.

**Figure 3.6**
Attribute Extraction – Parameter Analysis

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objects. Therefore, the result of the threshold analysis on actual parameters is a
grouping of the actual parameters into data sets which will represent the attribute
sets of candidate objects.

3.2.2 Attribute Extraction -- Global Variable Analysis

The approach to global variable analysis concentrates on the COMMON
block in FORTRAN because special considerations must be made for FORTRAN
that are not necessary in other imperative languages. Specifically, COMMON block
resolution and the determination of placeholders is not necessary in imperative
languages such as C, Pascal and COBOL. The approach described in the
dissertation for attribute extraction based on global variable analysis generalizes to
these languages readily by using scoping rules and location of global variable
declaration. Therefore, the primary focus will be on the COMMON block in
FORTRAN as it is the most involved.

By considering the subroutine as the unit of functionality, the COMMON
variables referenced in the COMMON statement of a subroutine are necessary to
perform the function of the given subroutine. Realizing this, FORM seeks to obtain
the largest set of global variables that represent the strongest cohesive unit. The
cohesive strength of a pair of COMMON variables is measured by determining the
frequency in which they are both necessary for the execution of the subroutine. To
measure the cohesion of a pair of COMMON variables, three cases must be
considered:
(i) both COMMON variables are necessary,

(ii) only one COMMON variable is necessary, and

(iii) neither COMMON variable is necessary.

The value of the cohesive measure of a given pair of COMMON variables is affected by each case as follows: case (i) increases the value, case (ii) decreases the value, and case (iii) does not modify the value. The greedy approach taken by the algorithm results in a cost function that, for a given pair of variables, weights the necessity of both variables of a pair as a stronger condition than the necessity of only one variable of the pair. Therefore, the cost function, $c$, is increased by 0.2 when both parameters are necessary for the execution of the subroutine, and only decreased by 0.1 when only one variable is necessary for the execution of the subroutine. By adjusting the amount that $c$ is increased or decreased, the "greediness" of the approach is determined. The values chosen are 0.1 and 0.2, and define the necessity of both variables to be twice as important as the necessity of only one. Thus, the cost function, $c$, for a pair of variables $i$ and $j$ with respect to COMMON statement $f$ is as follows:

\[
c(i,j) = \begin{cases} 
  c(i,j) & \text{if and only if neither } i \text{ nor } j \text{ is necessary for the} \\
  c(i,j) + .2 & \text{execution of } f \\
  c(i,j) - .1 & \text{if and only if either } i \text{ or } j \text{ (but not both) is necessary for the} \\
  & \text{execution of } f
\end{cases}
\]
The cohesive strength for the pair of variables is stored in a weighted adjacency matrix, $M$, where $M[i,j]$ is assigned a real number value based on the result of the cost function $c(i,j)$. Once the matrix $M$ is instantiated, a threshold table is constructed. The threshold table consists of two columns: threshold value and data sets. The threshold value is a non-negative real number and is determined from $M$ by creating a row in the threshold table for each non-negative value in $M$. Corresponding data sets are computed for each threshold value using the transitive closure algorithm. Based upon this threshold table, the human reverse engineer selects the appropriate threshold level. The corresponding data sets translate to attribute sets of candidate objects.

The general algorithm for attribute extraction based on global variable analysis is given in Figure 3.7. This four-step procedure inputs the raw source code and performs two resolution steps: resolution of placeholders in the COMMON statements and resolution of aliases in the COMMON statements. Once the resolution has been performed, the source code is analyzed and a weighted adjacency matrix, $M$, is generated using the algorithm in Figure 3.8. The threshold table is then generated from $M$ using the transitive closure algorithm. At this point, the human reverse engineer determines an appropriate threshold level, thereby determining the attribute sets for the candidate objects. The result of the threshold analysis on global variables is a grouping of the global variables into data sets which will represent the attribute sets of the candidate objects.
Step 1. Determine placeholders COMMON statements
Step 2. Resolve aliasing of COMMON variables
Step 3. Perform parameter analysis on the COMMON statements generated in Step 2 and generate a weighted adjacency matrix using the cost function, c.
Step 4. Generate the threshold table.

Figure 3.7
General Algorithm for Attribute Extraction from COMMON variables

At this point, the attribute extraction phase is completed. Actual parameters and global variables have been evaluated independently and attribute sets determined. Actual parameter analysis and global variable analysis result in threshold tables that are evaluated by a human reverse engineer to determine attribute sets for candidate objects. Note that the threshold analysis for actual parameters and global variables is performed independently because what may be a desirable threshold value for actual parameters is not necessarily a desirable threshold value for global variables.

The object extraction phase is not yet complete. Recall the definition of an object, O = (D,M). To this point, the data sets, D, of the candidate objects have been defined. Thus, the final step in object extraction is the extraction of the methods, M, that correspond with the data sets, D, thereby producing the candidate objects.
Let \( P \) be a structured FORTRAN program
With \( n \) COMMON statements
And \( m \) distinct variables in the COMMON area
(i) Preprocessing Phase
a. Resolve the aliases of the COMMON block
b. Determine \( R_i \) for each \( B_i \)
(ii) Let \( G = (V, E) \) be a graph
\( V = \) the arbitrary ordered set of all variables in the COMMON area,
and denote the elements of \( V \) as \( v_1, v_2, \ldots, v_m \) /* note \(|V| = m*/
\( E = \{ \} \)
(iii) \( M[1..m, 1..m] \) ARRAY of REAL /* a weighted adjacency matrix */
\( A[1..n, 1..m] \) ARRAY of BOOLEAN /* \( n \) sets of COMMON variables */
/* Construct the graph, represented as a weighted adjacency matrix */
/* Initially \( G \) consists of only a set of vertices with no edges */
For \( i = 1 \) to \( m \) do
  For \( j = 1 \) to \( m \) do
    \( M[i,j] = 0 \)
  od
od /* Initialize the sets of COMMON variables; \( C[i,j] = 1 \) if and only if \( v_j \) is an element of \( R_i \)
For \( i = 1 \) to \( n \) do
  For \( j = 1 \) to \( m \) do
    If \( v_j \) is an element of \( R_i \)
      Then \( C[i,j] = 1 \)
      Else \( C[i,j] = 0 \)
    od
od /* Perform the analysis on the sets \( C \) */
For \( i = 1 \) to \( n \) do
  For \( j = 1 \) to \( m \) do
    For \( k = j+1 \) to \( m \) do
      If \( C[i,j] = 1 \) and \( C[i,k] = 1 \) /* both parameters are necessary*/
        Then \( M[j,k] = M[j,k] + 0.2 \)
      Else if \( C[i,j] = 0 \) and \( C[i,k] = 0 \) /* inconclusive */
        Then skip
      Else \( M[j,k] = M[j,k] - 0.1 \) /* only one is 0 */
    od
  od
od /* The output is \( r < n \) connected graphs. The vertices of each connected graph represents
the number of attributes for a distinct candidate object. */

\textbf{Figure 3.8}
\textbf{Attribute Extraction – COMMON Variable Analysis}
3.2.3 Method Extraction

The procedure for extracting methods from the source code identifies statements that modify at least one of the attributes of the object to which it belongs. One approach is to first look to extract methods with no concern of the grouping of data sets to form object attributes. In this approach, the focus is on obtaining groups of statements that constitute some unit of functionality and the entire object extraction procedure is then driven by the method extraction. While this approach has some merit, to determine reasonable functionality would require extensive domain knowledge. Thus, the degree of generality for such an approach is very low in that the methodology itself would require major adaptations to adequately extract objects from various application domains. FORM takes the alternative approach.

The approach to method extraction is a data-driven approach and has a much higher degree of generality. Analysis is performed on the source code and results in data groupings that correspond to attributes of candidate objects. The nature of the analysis is such that it is domain independent but language dependent, however, in most cases this language dependence generalizes further to paradigm dependence. That is, the analysis is performed on a given language (e.g. FORTRAN, COBOL, C, Pascal, etc.) or a class of languages (i.e. imperative) without prior knowledge of the application domain. Thus, methods are extracted following the extraction of data sets. Moreover, the data sets drive the method extraction algorithm. By performing the object extraction in this manner, a large
part of the extraction can be automated and the knowledge of a domain expert utilized for refinement.

The theoretical foundation of the method extraction procedure is program slicing [Weis 84]. Program slicing is defined as a "decomposition based on data flow and control analysis [Weis 84]." A slicing criterion is defined as the tuple \( C = \langle i, V \rangle \) where "\( i \)" is a statement number and \( V \) is a set of variables. \( R(0,C,n) \) is defined as the set of relevant variables at statement "\( n \)" and is defined as all variables "\( v \)" such that:

1. \( n = i \) and \( v \) is in \( V \), or
2. \( n \) is an immediate predecessor of a node \( m \) such that either
   a. \( v \) is in \( \text{REF}(n) \) and there is a \( w \) in both \( \text{DEF}(n) \) and \( R(0,C,m) \), i.e. \( w \) is relevant at statement \( m \) and \( v \) is used to define \( w \) at the previous statement. Thus, if \( w \) is a relevant variable at the node following \( n \), and \( w \) is given a new value at \( n \), then \( w \) is no longer relevant and all the variables used to define \( w \)'s value are relevant, or
   b. \( v \) is not in \( \text{DEF}(n) \) and \( v \) is in \( R(0,C,m) \), i.e. \( v \) is relevant at statement \( m \) and is not defined in the previous statement. Thus, if a relevant variable at the next node is not given a value at node \( n \), then it is still relevant at node \( n \).

Then \( S(0,C) \) is a set of statements, i.e. the slice where \( S(0,C) \) is all nodes \( n \) such that \( R(0, C, n+1) \) intersect \( \text{DEF}(n) \) is not empty. Thus, if a relevant variable is defined in
a previous statement, than that statement is included in the slice. Additionally, any branch statement which can choose to execute or not execute some statement in S(0,C) should also be included in the slice [Weis 84].

To use program slicing for method extraction, we defined extensions to the program slicing in [Weis 84]. First, the slicing criterion, C, is defined as C = <M,V> where M is a module, or block of statements, i.e. a subroutine or the main program, and V is the set of attributes of a given object. Recall that once the appropriate threshold value is chosen, the corresponding data sets represent attributes of candidate objects. These data sets are then used to drive the method extraction. For each data set, program slicing is performed on a subset of the modules and each resultant slice becomes a method in the corresponding object. Because the data sets are derived from actual parameters or global variables, the method extraction process must be performed with variation in each case. Specifically, when slicing for methods corresponding to actual parameters, consideration must be given to the formal parameter mapping based upon the CALL statements in which the actual parameters appear. Such consideration is not necessary when slicing for methods corresponding to global variables.

Method extraction for data sets comprised of actual parameters is driven by the system’s CALL statements. Let K be the set of all CALL statements of the system. Then for a given data set, D, form the set P, such that P contains all CALL statements that contain one or more elements of D as an actual parameter. For each element of P, define the slicing criterion C = <M,V> such that M is the called
subroutine and $V$ is the set of formal parameters that correspond to the elements of $D$ appearing in the CALL statement as actual parameters. Note that because $P$ is a set and not a bag, redundancy is eliminated. Thus, each data set $D$ has at most $|P|$ methods, i.e. one method for each element of $P$.

Let $n$ = the number of data sets comprised of COMMON variables, and  
$m$ = the number of subroutines in the system.

Then,  
For $i = 1$ to $n$ do  
For $j = 1$ to $m$ do  
Compute the slice on $<M_j, D_i>$ and let  
Method $j$ of object $i$ equal this slice.  
od  
od

**Figure 3.9**
Method Extraction Algorithm for Data Sets Comprised of COMMON Variables

Method extraction for data sets comprised of global variables is more straightforward than for actual parameters. Each subroutine in the system is sliced on the criterion $C = <M, V>$ where $M$ is the module and $V$ is the set of COMMON variables in the data set. Thus for data sets comprised of COMMON variables, the extraction algorithm is given in Figure 3.9. For each object there are at most $m$ methods which are defined by using program slicing on each subroutine. Using each data set that is comprised of COMMON variables as a variable set for a slicing
criterion and each subroutine as the statement set for a slicing criterion, the methods are extracted.

It is important to realize that the method extraction procedure in both the actual parameters and COMMON variables does not attempt to assign semantic names to the methods. Although this may appear a shortcoming at first, a deeper investigation into the area reveals that by not attempting to semantically qualify the methods, the scope of the methodology is much broader. That is, an objective of the methodology is generality across many application domains. The assignment of semantic naming would require a great amount of domain specific knowledge and, therefore, restrict the generality of the methodology as a whole.

At this point, the first phase, Object Extraction, of the methodology is completed. The result of this phase is a set of candidate objects. These candidate objects serve as input to the second phase, Class Abstraction.

3.3 Class Abstraction

In phase one, Object Extraction, candidate objects were extracted from the source code. Phase two, Class Abstraction evaluates the candidate objects extracted in phase one, and clusters the candidate objects to form classes. To facilitate the clustering process, the candidate objects are analyzed to obtain the following information: number of attributes, number of methods, type signature of the attributes, and use and defines lists of each method. Clusters are formed from the set of candidate objects based on an identity measure. The classes are determined by mapping each object cluster to a unique class.
Definition 3.1: Identical Objects

Two objects $O_1$ and $O_2$ are defined to be identical objects when the following criteria is satisfied:

1. The number of attributes of $O_1$ equals the number of attributes of $O_2$.
2. The number of methods of $O_1$ equals the number of methods of $O_2$.
3. The attribute type signature of $O_1$ is identical to the attribute type signature of $O_2$.
4. The subroutines of derivation of $O_1$ are identical to the subroutines of derivation of $O_2$.
5. Corresponding methods of $O_1$ and $O_2$ differ only where attribute names are concerned.

If all five criteria are met, the two objects are said to be identical and are clustered together. This determination is made for each pair of objects. Thus, for $n$ objects, at most $C(n,2)$ tests must be performed because the definition of identical objects is transitive and partitions the set of objects into equivalence classes. Additionally, at least $(n-1)$ tests must be performed. The upperbound $C(n,2)$ occurs when at most two objects are grouped together and those two are the last two tested. The lowerbound of $(n-1)$ occurs when a single equivalence class is formed that contains all objects, i.e., all objects are identical and a single cluster is formed.
Once the set of objects has been partitioned into equivalence classes, the mapping to classes is straightforward. Each equivalence class maps to a unique class in the object model. Thus, the mapping between object equivalence classes and classes in the object model is one-to-one and onto, i.e. isomorphic.

**Lemma 3.1** Let $C$ be the set of classes in the object model, $E$ be the set of object equivalence classes, and $O$ be the set of objects. Then $|C| = |E| \leq |O|$.

**Proof:**

By definition, each element of $E$ (an object equivalence class) maps to one and only one element of $C$ (a class in the object model). Assume $|C| < |E|$. Then either some element of $E$ maps to more than one element of $C$ ($|C| > |E|$) or some element of $E$ maps to no element of $C$ ($|C| < |E|$). But this contradicts the definition, therefore, $|C| = |E|$.

By definition, each element of $O$ maps to one and only one element of $E$. Assume $|E| > |O|$. Then some element of $O$ maps to more than one element of $E$. but this contradicts the definition, therefore $|E| \leq |O|$.

Therefore, $|C| < |E| \leq |O|$. (QED)

### 3.3.1 Attribute Definition

Once the equivalence classes have been defined and mapped to classes in the object model, it is necessary to determine the set of attributes for each class. Each object in the equivalence class has a unique set of attributes. Because the objects of an equivalence class are identical, the attributes of the objects in that class are
identical by Definition 3.1. Using this definition, it is possible to abstract attributes for the class.

Consider some object equivalence class, \( E \), and the corresponding class in the object model, \( C \). Let \( O \) be some object in \( E \) and represent the number of attributes of \( O \) as \( n_a(O) \). By Definition 3.1, every object in \( E \) has an equal number of attributes, so denote the number of attributes of any object in \( E \) as \( n_a(E) \). Then, the corresponding class, \( C \), will have \( n_a(E) \) attributes. Because no consideration is given to the semantic nature of these attributes, they are to be designated as \( att_1, att_2, att_3, \ldots, att_{n_a(E)} \).

Once the attributes are determined, it is necessary to determine the type of each attribute. Let \( O \) be some object in \( E \), and denote the type signature of the attributes of \( O \) as \( ts(O) \). Since every object in \( E \) has an identical attribute signature by Definition 3.1, denote the attribute type signature of any object in \( E \) as \( ts(E) \). Thus, the corresponding class, \( C \), will have type signature \( ts(E) \). Thus, careful definition of identical objects and properly clustering the objects in such a way that the clusters represent equivalence classes, the procedure to define attributes of the classes is quite elegant.

3.3.2 Method Definition

The final step in the class abstraction phase is to abstract a set of class methods from the cluster of objects that corresponds to the class. The definition of methods of a class requires the consideration of two factors: number of methods and method content. That is, for each class the first step in the method definition
procedure is to determine the number of methods the class will contain and the second procedure is to instantiate the methods. Again, careful definition of identical objects and properly forming the object clusters has served to reduce the effort required to define the methods of a class.

**Lemma 3.2** Let E be some object equivalence class, C be the class in the object model that corresponds to E and O be some object in E. Denote the number of methods of O as \( nm(O) \). Further, denote the number of methods of E as \( nm(E) \) and the number of methods of C as \( nm(C) \). Then \( nm(O) = nm(E) = nm(C) \).

**Proof:**

1. \( nm(O) = nm(E) \): By Definition 3.1, identical objects have an equivalent number of methods. Consider some object equivalence class, E. Then, E is formed through a mapping of clusters of identical objects. Moreover, the mapping of object clusters to object equivalence classes has been shown to be isomorphic. Therefore, E maps to a single object cluster containing objects which all have an equivalent number of methods. Therefore, \( nm(O) = nm(E) \).

2. \( nm(E) = nm(C) \): Each object equivalence class, E, maps directly to one and only one object class C. Specifically, each method in E maps to a method of C. Therefore, \( nm(E) = nm(C) \).

Therefore, \( nm(O) = nm(E) = nm(C) \). (Q.E.D.)

By Lemma 3.2, each class, C, contains exactly the number of methods of its corresponding object equivalence class. Each method is then denoted as Method1, Method2, ..., Method\( nm(C) \). Hence, the first step in method definition, determination
of the number of methods of an object class, is straightforward. The next step in the method definition procedure is to instantiate the methods.

Consider an object equivalence class, E. Then, the objects contained in the cluster of objects, O, that maps to E are identical and by Definition 3.1, their methods differ only where attribute names are concerned. So, consider some object \( o \) in O. Then, each method of \( o \) maps to a method in C such that the attribute variable names in the methods of \( o \) are replaced with the corresponding attribute variable names of C.

Upon completion of the method definition procedure, the Class Abstraction phase of FORM is completed. At this point, objects have been identified and classes in the object model have been abstracted. At this point we have an object oriented design that consists of a single-level hierarchy. That is, no parent classes are defined for the class structure. Therefore, the next phase of the methodology is to define parent classes by Abstraction of the Inheritance Hierarchy.

3.4 Abstraction of the Inheritance Hierarchy

Abstraction of the Inheritance Hierarchy involves clustering the classes of the object model based on similarity measures. Because the classes have two components (attributes and methods) two similarity measures are discussed: attribute-based similarity and method-based similarity. The flexibility and generality of the method then allows the human reverse engineer to determine how these similarity measures may be used to best serve the needs of the project. Thus, the human reverse engineer may choose to utilize the information generated by only one
similarity measure, or perform the procedure to synthesize the information of both measures. Again, in an effort to preserve the generality of the methodology, the decision of how best to utilize the information generated is left to the human reverse engineer.

The similarity analysis is performed using the five criteria considered for class formation: number of attributes, number of methods, type signature of attributes, and subroutine of derivation of the methods. Consider a class, $C$, with $na(C)$ attributes and $nm(C)$ methods. Then the type signature of the attributes of $C$ is represented as a bag, $B_1$, whose elements are the types of the attributes of $C$. Moreover, $|B_1| = na(C)$. Further, the subroutines of derivation of the methods of $C$ are represented as a bag, $B_2$, whose elements are the names of the subroutines that were sliced to generate the methods of the class. Additionally, $|B_2| = nm(C)$. This criteria is used to perform the two types of analysis on the classes: attribute-based similarity and method-based similarity. The result of this analysis is a weighted adjacency matrix that is further analyzed to produce a threshold table. Based upon this threshold table, the set of classes is partitioned into disjoint sets of clusters which map to the parent classes of the inheritance hierarchy.

### 3.4.1 Attribute-Based Similarity

The attribute-based similarity measure determines the similarity of a pair of classes based on the similarity of their attributes. For a pair of classes, a similarity measure is assigned based on two characteristics of the classes' attributes: number and type signature. This value is stored in a weighted adjacency matrix from which
a threshold table is constructed using the transitive closure algorithm. The algorithm for computing the attribute-based similarity measure for each pair of classes in the object model is given in Figure 3.10.

Let $n$ be the number of classes in the object model.

Let $M$ be an $n \times n$ weighted adjacency matrix whose rows and columns represent the classes of the object model.

Define $R$ to be the row vector such that $R_i$ is the $i$th class of the object model.

Define $L$ to be the column vector such that $L_j$ is the $j$th class of the object model.

Let $na(C)$ represent the number of attributes of a class $C$.
Let $as(C)$ represent the attribute type signature of a class $C$.

1. Initialize $M$ to the zero matrix.
2. For $i = n$ do
3. For $j = i+1$ to $n$ do
4. If $na(R_i) = na(L_j)$ then $M[i,j] = M[i,j] + 0.2$
5. else $M[i,j] = M[i,j] - 0.1$. 
6. fi
7. $id = |as(R_i) \text{ intersect } as(L_j)|$
8. $sim = id / \max(na(R_i), na(L_j))$
10. od
11. od

**Figure 3.10**

*Algorithm to Compute Attribute-Based Similarity*

The algorithm for computing the attribute-based similarity evaluates pairs of classes for similarity in number of attributes by determining if the classes have the same number of attributes, or they do not, no consideration is given to the difference in the number of attributes. This approach is taken because counting the number of attributes does not give information as to how they are used. However, because

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objects can not be considered identical without having the same number of attributes, it is a necessary consideration. Evaluation of the attribute type is used to provide information on how the attributes may be used. By considering the type signature of the attributes of a class, it is possible to ascertain a similarity relationship between classes. Additionally, it is important to realize that the similarity measure is not binary, but serves to provide a measurement of the degree of similarity. Through the use of the thresholding concept, the human reverse engineer may determine a desirable degree of similarity.

3.4.2 Method-Based Similarity

The method-based similarity measure determines the similarity of a pair of classes based on the similarity of their methods. For a pair of classes, a similarity measure is assigned based on two characteristics of the classes' methods: number and subroutine of derivation. This value is stored in a weighted adjacency matrix from which a threshold table is constructed using the transitive closure algorithm. The algorithm for computing the method-based similarity measure for each pair of classes in the object model is given in Figure 3.11.

The algorithm for computing the method-based similarity evaluates pairs of classes for similarity in number of methods by determining if the classes have the same number of methods. This is a binary consideration, that is either the classes have the same number of methods, or they do not, no consideration is given to the difference in the number of methods. This approach is taken because counting the
Let \( n \) be the number of classes in the object model.

Let \( M \) be a \( n \times n \) weighted adjacency matrix whose rows and columns represent the classes of the object model.

Define \( R \) to be the row vector such that \( R_i \) is the \( i^{th} \) class of the object model.

Define \( L \) to be the column vector such that \( L_j \) is the \( j^{th} \) class of the object model.

Let \( nn(C) \) represent the number of methods of a class \( C \).

Let \( sd(C) \) represent the subroutine of derivation of the methods of a class \( C \).

1. Initialize \( M \) to the zero matrix.
2. For \( i = n \) do
3. For \( j = i+1 \) to \( n \) do
4. If \( nm(R_i) = nm(L_j) \)
5. then \( M[i,j] = M[i,j] + 0.2 \)
6. else \( M[i,j] = M[i,j] - 0.1 \).
7. fi
8. \( id = |sd(R_i \ intersect \ sd(L_j)| \)
9. \( sim = id / \ max(sd(R_i), sd(L_j)) \)
10. \( M[i,j] = M[i,j] + sim \)
11. od
12. od

**Figure 3.11**

Algorithm to Compute Method-Based Similarity

number of methods does not give information as to their functionality. However, because objects cannot be considered identical without having the same number of methods, it is a necessary consideration. Evaluation of the subroutine of derivation is used to provide information the functionality of the methods. By considering the subroutine of derivation of the methods of a class, it is possible to ascertain a similarity relationship between classes. As with attribute-based similarity, the method-based similarity measure is not binary, but serves to provide a measurement...
of the degree of similarity. Additionally, the thresholding concept allows the human reverse engineer to determine a desirable degree of similarity

3.4.3 Combining Threshold Tables

Upon completion of the attribute and method based similarity measures, the human reverse engineer then determines the most appropriate use of these methods for their particular case. The methodology affords them several options: emphasize the attribute-based similarity measure, or emphasize the method-based similarity measure. This results in the necessity to synthesize the information contained in the separate threshold tables.

To combine the information of both threshold tables, each table is first considered independently and a threshold value is chosen for each table. The result is two sets of class clusters, one for attribute-based similarity, AC, and a second for method-based similarity, MC. These two clusters are combined to form a single cluster, CC. The clustering algorithm is given in Figure 3.12.

This analysis results in the set CC of parent classes. The inheritance hierarchy is formed by creating a parent class as follows: for every powerset PS in CC, create a parent class whose child classes are the elements of the powerset. The abstraction of the inheritance hierarchy is the last step in the methodology to extract the object model. The final phase of the process involves the representation of the object model.
1. Let $U$ be the universe of all classes in the object model.
2. Let $\text{FINISHED}$ be a set that is initially empty.
3. For each element $e$ in $U$
4. if $e$ is a singleton in $\text{AC}$, and $e$ is a singleton in $\text{MC}$ then
5. $e$ is a singleton in $\text{CC}$
6. add $e$ to $\text{FINISHED}$
7. else
8. for each element $f$ that is clustered with $e$ in both $\text{AC}$ and $\text{MC}$ do
9. cluster $e$ and $f$ in $\text{OC}$
10. add $e$ and $f$ to the set $\text{FINISHED}$
11. od
12. endif
13. for each element $e$ in $U/\text{FINISHED}$ do
14. if $e$ is a clustered with $f$ in ($\text{AC}$ or $\text{MC}$)
15. // the reverse engineer choose $\text{AC}$ or $\text{MC}$
16. then cluster $e$ and $f$ in $\text{OC}$
17. else cluster $e$ as a singleton in $\text{OC}$
18. endif
19. od
20. od

Figure 3.12
Clustering Algorithm

3.5 Representation of the Object Model

The representation of the object model marks the final phase in the methodology. The extracted object-oriented design is represented in two types of diagrams and several supporting documents. The two categories of diagrams are the hierarchy diagrams and the interaction diagrams. The hierarchy diagrams represent the static elements of the design and include such documents as the object
templates, class templates, and the object/class mapping diagram. The interaction diagrams describe the dynamic elements of the design and include such documents as the method invocation diagram and the state interrogation diagram.

3.5.1 The Hierarchy Diagrams

The first type of diagrams is the hierarchy diagrams. The hierarchy diagrams represent the inheritance hierarchy. These diagrams depict a data view of the system. The hierarchy diagrams consist of a set of object templates, class templates and an object/class mapping diagram.

The object template contains all pertinent information about each object in the system. For each object extracted from the system, there is a corresponding object template. The object template contains the object name, attribute names and types, method interface and subroutines of derivation of the methods. The object template is given in Figure 3.13.

```
ObjectName is

Attributes attribute1:type1, ... attributeN:typeN

Methods method1, method2, ..., methodJ

SubDerivation subroutine1, subroutine2, ..., subroutineK

Figure 3.13
Object Template
```

The class templates are similar to the object templates, but represent the result of the abstraction of objects into classes. The class template contains the class
name, parent class(es), attribute names and types, and method interface. The object/class mapping diagram is incorporated into the class template and describes which objects are clustered to form classes. The class template is given in Figure 3.14.

ClassName is \{object_name1, object_name2, etc.\}

ParentClass is \{ParentClass\}

Attributes attribute1: type1, ..., attributei: typei

Methods method1, method2, ..., methodj

Figure 3.14
Class Template

3.5.2 The Interaction Diagrams

The interaction diagrams describe class interactions and introduce the element of control flow into the object model. There are two considerations in forming the interaction diagrams: (a) Call statements in subroutines possibly perform a computation and pass information back to the calling subroutine. This information is possibly used elsewhere in the calling subroutine. This is preserved in the object model as a message passed to an object with the corresponding method. (b) Messages may need to be passed to an object to interrogate state information. These two considerations define under what circumstances messages are passed between objects, specifically, method invocation and state interrogation.

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The method invocation diagram is related to subroutine invocation in FORTRAN. In FORTRAN, a call statement invokes a subroutine, while, in the object model, methodA passes a method to methodB. MethodA will be determined by which subroutine the call statement appears. This is done by the following procedure: (1) determine the subroutine of invocation of the call statement, (2) determine which objects have a method that was derived from the given subroutine, (3) determine the information returned by the call statement, (4) determine which of the objects in #2 use the information returned by the call statement. Each of these objects is an object that initiates the message, i.e. methodA. MethodB is determined as follows: (1) determine which subroutine is invoked by the call statement, (2) determine which methods of each object have that subroutine as the subroutine of derivation, and (3) each of the corresponding objects will be the object to which the message is passed. The method invocation template is given in Figure 3.15.

```
ClassName
MethodName invokes ClassName.methodname1

MethodName invokes ClassName.methodnamej

Figure 3.15
Method Invocation Template
```

The state interrogation diagram represents which messages are passed among the objects to interrogate state information. If objectA references a variable which is not an attribute or local variable of objectA, then it is referencing an
attribute of another object. Therefore, a message must be sent to the object containing the variable as an attribute. Each method of every object must be evaluated. Because there are no global variables in the object model as were in FORTRAN, each reference to a COMMON variable will translate to a state interrogation method. The state interrogation template is given in Figure 3.16.

```
ClassName

MethodNamen  interrogates  ClassNamei.attributej

MethodNamem  interrogates  ClassNamek.attributez
```

Figure 3.16
State Interrogation Template

This collection of diagrams comprises the representation of the object model as extracted from the source code. These diagrams represent both static and dynamic properties of the system. The diagrams are object-oriented and represent the system at a higher level of abstraction than the original source code. This representation facilitates the modification of the system’s properties at a higher level of abstraction in an effort to reduce future maintenance costs. Moreover, because this is a system design, there are no restrictions placed on the choice of an implementation language.

3.6 Validation and Evaluation of FORM

Software quality is a multifaceted concept that can be described from different perspectives. Five perspectives, as in [Kitc 96] are the transcendental view, user view, manufacturing view, product view, and value-based view. The
definition of software quality is based upon the perspective taken. However, these views do not address the design phase of the software lifecycle. Moreover, the issues pertinent to forward engineering do not necessarily parallel those pertinent to reverse engineering. In the forward engineering process, a design is developed based upon a requirements specification which details user expectations and needs. Thus, we expect and require that the design meets the requirements specification, thereby meeting user needs. The quality of a forward engineered design can be discussed in several contexts, such as how well the design represents the requirements specification, or how the design evaluates using a given set of metrics, as in [Li 95]. In reverse engineering, however, this is not the case.

The reverse engineering process begins with source code that has undergone extensive maintenance and no longer satisfies the user needs. Rather than continue to nurse an antiquated system, the decision is made to extract the functionality of the system and utilize new technologies while making the required changes at a higher level of abstraction, thereby improving overall system quality, decreasing future maintenance costs, and satisfying current user needs. Hence, to measure the quality of a reverse engineered design in terms of current user needs is not reasonable. The reverse engineered design necessarily does not satisfy user needs. That was the primary motivation for reverse engineering the system. Therefore, when evaluating the quality of a reverse engineered design, one cannot simply rely on traditional methods.
There are numerous research efforts which present methodologies to extract an object-oriented design from imperative code [Liu 90; Liva 92; Lano 93; Ong 93; Subr 96]. Little discussion, however, is given to the issues involved in evaluating the quality of an object-oriented design extracted from an imperative language because the issues surrounding reverse-engineered designs differ from those involved in evaluating a forward-engineered design.

3.6.1 Traditional View of Software Quality

To discuss the quality of a software design, whether forward or reverse engineered, the concept of software quality must be defined. As stated in [Kitc 96], the definition of software quality is based on the perspective taken — transcendental, user, manufacturing, product, and value-based. The transcendental view sees quality as an unattainable goal because it can be recognized, but never completely defined. The user view is a very personal and concrete view of how the product meets the user’s needs. The manufacturing view focuses on whether or not the right product was produced, i.e. it is based on “document what you do and do what you say.” The product view considers the inherent characteristics of the product. The value-based view measures quality by what the user is willing to pay for. Based on the perspective taken, a single product’s quality measure may evaluate very differently. This is the underlying issue of the anomalous results caused by using forward engineering metrics to measure quality in a reverse engineered design.
The traditional discussion of a "good" design takes the product view. A "good" design is classified as having the following characteristics: modifiability, modularity, levels of abstraction, loose coupling, high cohesion. Moreover, a good design should support understanding and automation. [Pfle 91, Jone 90] Because, "there is no definitive way of establishing what is meant by a "good" design," (e.g., allowing efficient code to be produced, a minimal design whose implementation is maximally compact, or a design that has maximal maintainability) no single metric will suffice, hence, a suite of metrics for measuring the quality of object-oriented designs must be considered. [Somm 89, Chid 94]

The following metrics, discussed fully in [Li 95] and [Chid 94], were developed to measure the quality of object-oriented designs because metrics related to procedural systems are unable to characterize the concepts of inheritance, classes and message passing (the core concepts of the object-oriented paradigm): depth of the inheritance tree, number of children, response for a class, and lack of cohesion in methods [Li 95, Chid 94]. Each of these metrics is discussed individually, explaining any anomalous values that result in the context of reverse engineering.

Two metrics are related to the inheritance hierarchy, and, therefore, the scope of properties: depth of inheritance and number of children. The depth of the inheritance tree (DIT) for a class is the length of the maximum path from the root node to the class node. It defines the depth of the class in the inheritance tree. Therefore, a derived (sub)class has a DIT value equal to the DIT of its parent class + 1. The DIT represents the tradeoff between reusability through inheritance and
simplicity of system understanding. The number of children (NOC) of a class is the number of immediate descendants of a class. These metrics are collected from a reverse-engineered object-oriented design in the same manner as they are collected from a forward-engineered design. During the reverse engineering process, the criteria used for the formation of the inheritance hierarchy may predetermine the depth of the inheritance tree. Unless some threshold value is determined such that the abstraction of the inheritance hierarchy continues until the threshold is reached, the maximum DIT will be determined before the process ever begins. Therefore, the maximum scope of properties of a class is dependent on the methodology. [Li 95, Chid 94]

The response for a class (RFC) is defined as the number of methods that can be invoked in response to a message that is sent to an object of the class. This includes not only methods within the class, but also external methods. Because objects communicate using message passing, the RFC uses the methods as a measure of communication and, therefore, an indication of the effort required to test and debug an object. In the context of reverse engineering, one factor that will greatly inflate the value of RFC is the use of global variables. Excessive use of global variables will result in increased message passing and method invocation, thereby inflating the RFC. [Li 95, Chid 94]

The lack of cohesion in methods (LCOM) is the number of disjoint sets of local methods. The local methods are grouped into sets such that in each set, methods in the set share an instance variable with at least one other member of the
set. Hence, a highly cohesive class will have many methods that share instance variables and therefore, a low LCOM value. This promotes encapsulation, and reduces complexity. [Li 95, Chid 94] In the context of reverse engineering, the classes will necessarily have a high degree of cohesion based on the methodology used for object extraction. The methodology defined in [Ache 94] and [Ache 95] results in classes that are highly cohesive by extracting the objects based on the cohesive strength of the parameters.

The four metrics described above were designed to evaluate a forward-engineered object-oriented design. They quantitatively measure the quality of the design based on coupling (DIT, NOC), cohesion (LCOM), abstraction (DIT, NOC), modifiability (RFC, LCOM), and modularity (DIT, NOC). Each of these metrics measures the quality of the design based on the product view. Because the design is forward engineered, these criteria can be used to drive the development and, therefore provide a reasonable yardstick to measure the resulting design. In the context of reverse engineering, however, the constraints set forth by the source code may make it unreasonable to expect to achieve the same design quality when measured by these forward-engineering metrics. For this particular reason, an alternative view is recommended for the evaluation of the quality of reverse engineered designs.

3.6.2 Software Quality – Reverse Engineering Perspective

Because reverse engineering does not involve making modifications to the extracted design, the designs that are reverse engineered from legacy systems will
necessarily evaluate less than optimally using current metrics. However, when reengineering activities begin, (i.e., the reverse-engineered design is forward engineered to meet the new system requirements), the extracted design will be modified to improve the overall quality as per the product view. Thus, evaluating the reverse-engineered design requires that a different perspective be adopted.

Based on the definition of reverse engineering, the goal of the reverse engineering process is to extract the design of the system under evaluation. This means that the view most appropriate to evaluating the quality of the extracted design is the manufacturing view. Therefore, the extracted design is to be evaluated using the manufacturing view and the reengineered design is to be evaluated using the product view. By evaluating the extracted design using the manufacturing view, the reverse-engineer can be certain that qualities such as functional equivalence are maintained while giving less attention to such qualities as cohesion and coupling. Likewise, once the reverse-engineered design is reengineered to meet the new requirements of the system, the design is then evaluated using the product view, thereby focusing attention on measuring such qualities as coupling and cohesion which become vital considerations.

To evaluate the system under the manufacturing view, two criteria are presented: statement coverage and functional equivalence. Although neither of these are new metrics, the consideration in the context of reverse engineering is novel.
Let SI be the source code of the legacy system to be reverse-engineered, and let D1 be the reverse-engineered design. Then, the statement coverage of the D1 is equal to the number of statements of SI mapped into methods of D1, divided by the total number of statements of S1.

The statement coverage value is a direct computation. It provides insight into functional equivalence and may also aid in the detection of dead code. If the statement coverage is not 100%, it implies one of two cases: (i) some of the system's functionality may not be preserved or (ii) the statements not extracted represent dead code. In either case, it provides the reverse engineer with valuable information that will assist the reengineering process. Case (i) implies that the reverse engineering process itself must be reconsidered whereas case (ii) represents the detection of dead code. It is not the case, however, that 100% statement coverage implies functional equivalence, and vice versa. Therefore, both measurements are necessary.

Consider two software systems S1 and S2, where S1 is the legacy system to be reengineered and S2 is the implementation of the reverse-engineered design of S1. The design of S2 is said to be functionally equivalent to S1 if and only if when S1 and S2 are run on the same input, the resultant outputs are identical. This concept of functional equivalence is most important. It answers the question “did we extract the right design.” There is a disadvantage, however, associated with the determination of functional equivalence. To make the determination of functional equivalence requires that the reverse engineered design be implemented, thereby
providing the opportunity for errors in the translation from design to code. Hence, a functionally equivalent design that is incorrectly translated may appear functionally unequivalent, and vice versa. Until developments are made towards guaranteeing 100% correctness in design implementation, this measurement will be dependent on the skill of the programmer that implements the design.

Two case studies were performed on FORTRAN systems. System A evaluated to 100% statement coverage with functional equivalence. System B evaluated to 94% statement coverage, as a result of dead code, with functional equivalence.

3.7 Summary and Concluding Remarks

The FORTRAN Object Recovery Methodology (FORM) is a three phase methodology that extracts an object-oriented design from imperative code. Because FORTRAN is chosen as the source language, special considerations were required, thereby resulting in the development of an extensive pre-processing phase. The pre-processing phase includes alias resolution and determining placeholder values resulting from the use of the COMMON block.

The phases of the methodology include object extraction, class abstraction and abstraction of the inheritance hierarchy (Figure 3.4). Algorithms are given for each phase. The representation of the resulting object-oriented design required the development of a series of diagrams to adequately express the features unique to reverse-engineered designs.
The evaluation of reverse-engineered designs require considerations unique from those of forward-engineered designs. Because the original system was reverse-engineered for a variety of reasons, including no longer satisfying user needs it is not reasonable to measure the quality of such designs using metrics formulated for forward-engineered designs which, necessarily, satisfy user needs. Therefore, the evaluation and validation of FORM required the development of a new set of metrics. The metrics used to evaluate the resulting design include statement coverage and functional equivalence. These metrics evaluate the system under the manufacturing view. They are not new metrics, however, their use in this context is novel. The evaluation resulting from the use of these metrics ensure the validity of the extracted design.
Chapter 4

Case Studies

The research detailed in the dissertation develops a methodology that utilizes the concepts of reverse engineering to extract an object-oriented design from imperative code. This chapter will offer a step-by-step demonstration of the methodology by performing two case studies. The case studies were chosen for several reasons. Firstly, because the majority of scientific and engineering software systems currently in use are coded in imperative languages, specifically, FORTRAN-77, this language was chosen for the source code. Secondly, because the COMMON block in FORTRAN requires such great attention, examples were chosen to demonstrate both the complexity involved by extensive use of the COMMON block as well as the methodology’s performance.

The first case study is a statistics program to compute the standard deviation of two sets of numbers. The second is a program based on graph theory. Both are written in FORTRAN.

4.1 Statistics Case Study

The program used in this case study is a statistics program written in FORTRAN. It is small in size (less than 500 lines of code), and reads two data sets of integers from a file, stores them in arrays and computes the standard deviation of each data set. The program makes extensive use of subprogramming but does not include any COMMON variables.

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Using the algorithm for parameter analysis in Figure 3.6, we have:

\[ P = \text{STATISTICS} \quad / \ast \text{the source program} \ast / \]

\[ n = 5 \quad / \ast \text{the number of subroutine calls} \ast / \]

\[ m = 6 \quad / \ast \text{the number of distinct actual parameters} \ast / \]

The next step is to form the sets CALL1 - CALL5 and the sets V and E. CALL1 - CALL5 correspond to the sets of actual parameters of each subroutine call. The sets V and E represent the distinct actual parameters and function resultants. The corresponding sets are as follows:

- CALL1 = \{m, expa, n, expb,\}
- CALL2 = \{expa, m, stda\}
- CALL3 = \{expa, m, stda, expb, n, stdb\}
- CALL4 = \{\}
- \( \text{V} = \{m, \text{expa, n, expb, stda, stdb}\} \)
- \( \text{E} = \{\}\)\2

Continuing with the algorithm, construct the weighted adjacency matrix, M.

The resulting matrix is shown in Figure 4.1.

<table>
<thead>
<tr>
<th></th>
<th>k</th>
<th>l</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>j</td>
<td>m</td>
<td>expa</td>
<td>n</td>
<td>expb</td>
<td>stda</td>
<td>stdb</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>m</td>
<td>0</td>
<td>0.6</td>
<td>0.2</td>
<td>0.2</td>
<td>0.3</td>
<td>-0.1</td>
</tr>
<tr>
<td>2</td>
<td>expa</td>
<td>0</td>
<td>0</td>
<td>0.2</td>
<td>0.2</td>
<td>0.3</td>
<td>-0.1</td>
</tr>
<tr>
<td>3</td>
<td>n</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0.6</td>
<td>-0.1</td>
<td>0.3</td>
</tr>
<tr>
<td>4</td>
<td>expb</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>-0.1</td>
<td>0.3</td>
</tr>
<tr>
<td>5</td>
<td>stda</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>6</td>
<td>stdb</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

Figure 4.1
Weighted Adjacency Matrix, M
Once the weighted adjacency matrix $M$ has been formed, the next step in attribute extraction is the generation of the threshold table. A threshold table is generated for $M$ using the transitive closure algorithm on each non-negative value of $M$. The resulting threshold table is shown in Figure 4.2.

<table>
<thead>
<tr>
<th>Threshold Values</th>
<th>Data Sets</th>
</tr>
</thead>
<tbody>
<tr>
<td>$&gt;0$</td>
<td>${m, n, \text{expa}, \text{expb}, \text{stda}, \text{stdb}}$</td>
</tr>
<tr>
<td>$&gt;0.2$</td>
<td>${m, \text{expa}, \text{stda}} {n, \text{expb}, \text{stdb}}$</td>
</tr>
<tr>
<td>$&gt;0.3$</td>
<td>${m, \text{expa}} {n, \text{expb}} {\text{stda}} {\text{stdb}}$</td>
</tr>
<tr>
<td>$&gt;0.6$</td>
<td>${m} {n} {\text{stda}} {\text{stdb}} {\text{expa}} {\text{expb}}$</td>
</tr>
</tbody>
</table>

Figure 4.2
Threshold Table for Matrix $M$

Given the threshold table for program $P$, we must select a desirable threshold to complete the attribute analysis. This is done by the human reverse engineer. In selecting a threshold level, the goal is to find the largest data sets with the strongest cohesion, thereby minimizing the number of singleton data sets. Using this heuristic, a threshold value of 0.2 is selected from the threshold table. Selecting a threshold of 0.2 results in two objects. Object 1 has the attribute set $\{m, \text{expa}, \text{stda}\}$. Object 2 has the attribute set $\{n, \text{expb}, \text{stdb}\}$. Using the method extraction algorithms, object 1 has 3 methods and object 2 has 3 methods. The resulting objects templates are given in Figure 4.2 and Figure 4.3.

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Object 1 is

Attributes

- expa: array[14] of integer
- m : integer
- stda : real

Methods

Method 1

begin
    Read (5, 10, end = 15) m, (expa(i), i=1..14)
end

Method 2

begin
    tot = 0.0
    sum = 0.0
    DO 60 i = 1, m
        tot = tot + expa(i)
    60 continue
    mean = tot / m
    DO 70 j = 1, m
        ind(j) = mean - expa(j)
        sum = sum + ind(j)**2
    70 continue
    stda = sqrt(sum/(m-1))
end

Method 3

begin
    write(6, 80) 'Experiment A', ' Measurements', ((expa(i), i=1..m)
    80 format '/* excluded */'
    write (3, 90) 'Standard Deviation', stda
    90 format '/* excluded */'
    return
end

SubDerivation Input, Std, Print

Figure 4.3

Extracted Object Templates: Object 1
Object2 is

Attributes

\begin{itemize}
\item \texttt{expb} : array[14] of integer
\item \texttt{n} : integer
\item \texttt{stdb} : real
\end{itemize}

Methods

Method1
\begin{verbatim}
begin
   Read (5,10, end = 15) n, \texttt{(expb}(i),i=1..14)
end
\end{verbatim}

Method2
\begin{verbatim}
begin
   tot = 0.0
   sum = 0.0
   DO 60 i = 1, n
      tot = tot + expb(i)
   60 continue
   mean = tot / n
   DO 70 j = 1, n
      ind(j) = mean - exp(j)
      sum = sum + ind(j)**2
   70 continue
   stdb = sqrt(sum/(m-1))
end
\end{verbatim}

Method3
\begin{verbatim}
begin
   write(6, 80) 'Experiment A', 'Measurements', ((expb(i),i=1..n)
80 format /* excluded */
   write (3,90) 'Standard Deviation', stdb
90 format /* excluded */
   return
end
\end{verbatim}

Figure 4.4

Extracted Object Templates: Object 2

Hence, two objects were extracted, each with three attributes and three methods. Next, we abstract the inheritance hierarchy using the two techniques of attribute-based similarity and method-based similarity. Using attribute-based
similarity, the following statistics are generated: maximum number of attributes is 3, number of identical types is 3, and percentage of similarity of attributes is 100%. Using method-based similarity, the following statistics are generated: maximum number of methods is 3, number of identical subroutines of derivation is 3, and percentage similarity of methods is 100%. Based on the similarity measures, we can see that object 1 and object 2 are identical objects and are, therefore, combined to form a class. The resulting class template follows in Figure 4.5.

A deeper analysis of the result reveals a statement coverage of 100% and functional equivalence. That is to say, all of the statements of the source code were extracted into the object model. Moreover, functional equivalence was determined by implementing the extracted design in C++ and comparing the outputs. Because the outputs were identical, functional equivalence was established. No method invocation templates or state interrogation templates were necessary as the example doesn't make use of the COMMON block.

Thus, the case study demonstrates the methodology's capability to extract an object-oriented design that maintains the functionality of the source code. The simplicity of the extracted design reflects that of the source code. The two extracted objects were identified as identical and mapped into a single class. This case study was well defined and well documented. Therefore, the resulting design was easily evaluated for functional equivalence and statement coverage. The next case study involves a much more complex system with poor documentation.
Class 1 is \{object 1, object 2\}

ParentClass is \{\}

Attributes

\texttt{a1: array[14] of integer}

\texttt{a2: integer}

\texttt{a3: real}

Methods

Method 1
begin
read \(a2\)
end

Method 2:
begin
\texttt{tot = 0.0}
\texttt{sum = 0.0}
\texttt{DO 60 i = 1, a2}
\texttt{\hspace{1em} tot = tot + \texttt{a1(i)}}
\texttt{60 continue}
\texttt{mean = tot / a2}
\texttt{DO 70 j = 1, a2}
\texttt{\hspace{1em} ind(j) = mean - \texttt{exp(j)}}
\texttt{\hspace{1em} sum = sum + ind(j) ** 2}
\texttt{70 continue}
\texttt{\hspace{1em} a3 = \texttt{sqrt(sum / (a2 - 1)}}
end

Method 3
begin
\texttt{write 'Experiment ', 'Measurements ', (a1(j), j=1,a2)}
\texttt{write ' Standard Deviation ', a3}
end

\textbf{Figure 4.5}
\textit{Extracted Class Templates}
4.2 Graph Case Study

The program used in this case study is a medium-sized (500 - 3000 lines of code) FORTRAN program. It is a graph reduction program that makes extensive use of subprograms and the COMMON block. Extensive use of subprogramming required the need for resolving aliases using local variable resolution. Local variable resolution using the algorithm given in Figure 3.2 resulted in the 31 distinct actual parameters given in Figure 4.6.

<table>
<thead>
<tr>
<th>main.pnum</th>
<th>initial.num</th>
<th>initial.i</th>
<th>reduce.face</th>
</tr>
</thead>
<tbody>
<tr>
<td>reduce.arc</td>
<td>reduce.node</td>
<td>loopfacet</td>
<td>loop.num</td>
</tr>
<tr>
<td>vertex.node</td>
<td>vertex.num</td>
<td>series.num</td>
<td>parallel.num</td>
</tr>
<tr>
<td>wye.num</td>
<td>wye.arc(i)</td>
<td>wye.k</td>
<td>wye.da</td>
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<td>wye.db</td>
<td>wye.dc</td>
<td>wye.wa</td>
<td>wye.wb</td>
</tr>
<tr>
<td>wye.wc</td>
<td>delta.num</td>
<td>delta.arc(i)</td>
<td>delta.k</td>
</tr>
<tr>
<td>delta.da</td>
<td>delta.db</td>
<td>delta.dc</td>
<td>delta.wa</td>
</tr>
<tr>
<td>delta.wb</td>
<td>delta.wc</td>
<td>loop.num1</td>
<td></td>
</tr>
</tbody>
</table>

Figure 4.6
Distinct Actual Parameters

Using the algorithm in Figure 3.6, a weighted adjacency matrix was formed and the threshold table in Figure 4.7 was formed.
Threshold Value | Data Sets
--- | ---
$\geq 0$ | \{main.pnum, initial.num, initial.i, reduce.face, reduce.arc, reduce.node, loop.face1, loop.num, loop.num1, vertex.node1, vertex.num, series.num, parallel.num, wye.num, wye.arc(i), wye.k, wye.da, wye.db, wye.dc, wye.wa, wye.wb, wye.wc, delta.num, delta.arc(i), delta.k, delta.da, delta.db, delta.dc, delta.wa, delta.wb, delta.wc\}

$\geq 0.1$ | \{main.pnum\} \{vertex.node1, vertex.num\} \{loop.face1, loop.num1, loop.num\} \{reduce.arc, reduce.node, reduce.face, series.num, parallel.num\} \{wye.k, wye.da, wye.db, wye.dc, wye.wa, wye.wb, wye.wc\} \{delta.k, delta.da, delta.db, delta.dc, delta.wa, delta.wb, delta.wc\} \{initial.i, initial.num\} \{wye.num\} \{delta.num\} \{wye.arc(i)\} \{delta.arc(i)\}

$\geq 0.3$ | \{main.pnum\} \{vertex.node1, vertex.num\} \{loop.face1\} \{loop.num1\} \{loop.num\} \{reduce.arc, reduce.node\} \{reduce.face\} \{series.num\} \{parallel.num\} \{wye.k, wye.da, wye.db, wye.dc, wye.wa, wye.wb, wye.wc\} \{delta.k, delta.da, delta.db, delta.dc, delta.wa, delta.wb, delta.wc\} \{initial.i, initial.num\} \{wye.num\} \{delta.num\} \{wye.arc(i)\} \{delta.arc(i)\}

$\geq 0.6$ | \{main.pnum\} \{vertex.node1\} \{vertex.num\} \{loop.face1\} \{loop.num1\} \{loop.num\} \{reduce.arc\} \{reduce.node\} \{reduce.face\} \{series.num\} \{parallel.num\} \{wye.k, wye.da, wye.db, wye.dc, wye.wa, wye.wb, wye.wc\} \{delta.k, delta.da, delta.db, delta.dc, delta.wa, delta.wb, delta.wc\} \{initial.i\} \{initial.num\} \{wye.num\} \{delta.num\} \{wye.arc(i)\} \{delta.arc(i)\}

$\geq 1.2$ | \{main.pnum\} \{vertex.node1\} \{vertex.num\} \{loop.face1\} \{loop.num1\} \{loop.num\} \{reduce.arc\} \{reduce.node\} \{reduce.face\} \{series.num\} \{parallel.num\} \{wye.k, wye.da, wye.db, wye.dc\} \{wye.wa\} \{wye.wb\} \{wye.wc\} \{delta.k, delta.da, delta.db, delta.dc, delta.wa, delta.wb, delta.wc\} \{initial.i\} \{initial.num\} \{wye.num\} \{delta.num\} \{wye.arc(i)\} \{delta.arc(i)\}

$\geq 2.4$ | \{main.pnum\} \{vertex.node1\} \{vertex.num\} \{loop.face1\} \{loop.num1\} \{loop.num\} \{reduce.arc\} \{reduce.node\} \{reduce.face\} \{series.num\} \{parallel.num\} \{wye.k, wye.da, wye.db, wye.dc\} \{wye.wa\} \{wye.wb\} \{wye.wc\} \{delta.k, delta.da, delta.db, delta.dc\} \{delta.wa\} \{delta wb\} \{delta.wc\} \{initial.i\} \{initial.num\} \{wye.num\} \{delta.num\} \{wye.arc(i)\} \{delta.arc(i)\}

Figure 4.7
Threshold Table For Actual Parameters

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Using the heuristics described for selecting a desirable threshold level, a threshold value of 0.3 is selected. Selecting a threshold of 0.3 we get 16 data sets, corresponding to 16 objects. Several of the corresponding object templates are given in the following Figure 4.8 with the complete set given in Appendix A1. The objects shown in Figure 4.8 represent varying complexity: from Object 1, with one simple method to Object 10 with multiple, more complicated methods.

Object 1 is
Attributes
main.pnum : real

Methods

Method 1
begin
    READ(*,*) PNUM
end

SubDerivation {Main}

Object 8 is
Attributes
series.num : integer

Methods

Method 1
begin
    IF (FNODE(EDGE1) EQ. NODE) THEN
        EDGE2 = FLEDGE(EDGE1)
    IF (FNODE(EDGE2) EQ. NODE) THEN
        FLEDGE(EDGE1) = BREDGE(EDGE2)
    ELSE

Figure 4.8
Extracted Object Templates
FLEDGE(EDGE1) = FLEDGE(EDGE2) 
ENDIF 
NUM = FLEDGE(EDGE1) 
IF (FREDGE(NUM) .EQ. EDGE2) THEN 
FREDGE(NUM) = EDGE1 
ENDIF 
NUM = FREDGE(EDGE1) 
ELSE 
EDGE2 = BLEDGE(EDGE1) 
IF (FNODE(EDGE2) .EQ. NODE) THEN 
BREDGE(EDGE1) = BREDGE(EDGE2) 
BLEDGE(EDGE1) = BLEDGE(EDGE2) 
ENDIF 
NUM = BREDGE(EDGE1) 
IF (BLEDGE(NUM) .EQ. EDGE2) THEN 
BLEDGE(NUM) = EDGE1 
ENDIF 
NUM = BLEDGE(EDGE1) 
NUM = RFACE(EDGE1) 
IF (NUM .EQ. LFACE(EDGE1)) THEN 
ELSE 
NUM = LFACE(EDGE1) 
ENDIF 

SubDerivation {Series} 

Object 10 is 
Attributes
wye.k, wye.da, wye.db, wye.dc, wye.wa, wye.wb, wye.wc : real 

Methods 

Method 1 
begin 
ARC(1) = EDGE 
IF (BNODE(EDGE) .EQ. NODE) THEN 
ARC(2) = BREDGE(EDGE) 
ARC(3) = BLEDGE(EDGE) 
(figure continued)
ELSE
    ARC(2) = FLEDGE(EDGE)
    ARC(3) = FREDGE(EDGE)
ENDIF
DO 110 J = 1,10
    DA = 1 - POS(ARC(1),J)
    DB = 1 - POS(ARC(2),J)
    DC = 1 - POS(ARC(3),J)
    RHO = DA*DB*DC - (DA+DB+DC) + 1
    IF (RHO .GT. 0 ) THEN
        K = 1.0
    ELSE
        K= 0.0
    ENDIF
    POS(ARC(1),J) = 1-WC
    POS(ARC(2),J) = l-WA
    POS(ARC(3),J) = 1-WB
    DA = 1 - NEG(ARC(1),J)
    DB = 1 - NEG(ARC(2),J)
    DC = 1 - NEG(ARC(3),J)
    RHO = DA*DB*DC - (DA+DB+DC) + 1
    IF (RHO .GT. 0 ) THEN
        K = 0.0
    ELSE
        K= 1.0
    ENDIF
    DA = 1 - POINT(ARC(1),J)
    DB = 1 - POINT(ARC(2),J)
    DC = 1 - POINT(ARC(3),J)
    K = 0.5
    POINT(ARC(1),J) = 1-WC
    POINT(ARC(2),J) = 1-WA
    POINT(ARC(3),J) = 1-WB
110 CONTINUE
end

Method2
begin
    IF ( K .EQ. 0 ) THEN
        A1 = DA + DB*DC - DA*DB*DC

    (figure continued)
\[
B_1 = DB + DA*DC - DA*DB*DC
\]
\[
C_1 = DC + DB*DA - DA*DB*DC
\]
\[
WA = \text{DSQRT}(B_1*C_1/A_1)
\]
\[
WB = \text{DSQRT}(A_1*C_1/B_1)
\]
\[
WC = \text{DSQRT}(B_1*A_1/C_1)
\]

ENDIF

IF (DABS(WA-WB) .LE. 0.00001) THEN
ELSE

WC = (1-DC)*(DB-DA)/(WA-WB)

ENDIF

SubDerivation \{Wye, Transform\}

Object 16 is

Attributes
\[
\text{delta.arc(i)} : \text{integer}
\]

Methods
Method 1
begin
\[
ARC(1) = \text{EDGE}
\]
IF (RFACE(EDGE) .EQ. FACE) THEN
ARC(2) = FREDGE(EDGE)
ARC(3) = BREDGE(EDGE)
ELSE
ARC(2) = BLEDGE(EDGE)
ARC(3) = FLEDGE(EDGE)
ENDIF

end

SubDerivation \{Delta\}

The next step involves performing analysis on the COMMON variables. Using the algorithm given in Figure 3.8, a weighted adjacency matrix is generated, and a threshold table is formed. The partial threshold table is shown in Figure 4.9. Upon observation of the table, it becomes apparent that as the threshold value...
<table>
<thead>
<tr>
<th>Threshold</th>
<th>Data Sets</th>
</tr>
</thead>
<tbody>
<tr>
<td>&gt; 0</td>
<td>{fnode, bnode, lface, rface, dnode, dface, label, fledge, bledge, bledge, nn, na, nf, sore, sink1, flag, facnum, nodnum, arcnum, pos, neg, point, stprob, upprob, loprob, ernpos, ermeg, nterm, term1, term2, term3, term4, above, below, incdnt, toplevel, toptop, topser, topper, topvert, toploop} {sink2} {oface}</td>
</tr>
<tr>
<td>&gt; 0.1</td>
<td>{fnode, bnode, lface, rface, dnode, dface, label, fledge, bledge, bledge, nn, na, nf, sore, sink1, flag, facnum, nodnum, arcnum, pos, neg, point, stprob, upprob, loprob, ernpos, ermeg, nterm, term1, term2, term3, term4, above, below, incdnt, toplevel, toptop, topser, topper, topvert, toploop} {sink2} {oface} {facnum} {nodnum} {nterm}</td>
</tr>
<tr>
<td>&gt; 0.2</td>
<td>{fnode, bnode, lface, rface, dnode, dface, label, fledge, bledge, bledge, nn, na, nf, sore, sink1, flag, arcnum, pos, neg, point, ernpos, ermeg, nterm1, term1, term2, term3, term4, above, below, incdnt, toplevel, toptop, topser, topper, topvert, toploop} {stprob, upprob, loprob} {sink2} {oface} {facnum} {nodnum} {nterm} {sore} {sink1}</td>
</tr>
<tr>
<td>&gt; 0.3</td>
<td>{fnode, bnode, lface, rface, dnode, dface, label, fledge, bledge, bledge, nn, na, nf, flag, arcnum, pos, neg, point, ernpos, ermeg, incdnt} {topdel, toptop, topser, topper, topvert, toploop} {stprob, upprob, loprob} {term1, term2, term3, term4} {above, below} {sink2} {oface} {facnum} {nodnum} {nterm} {sore} {sink1} {arcnum}</td>
</tr>
<tr>
<td>&gt; 0.4</td>
<td>{fnode, bnode, lface, rface, dnode, dface, label, fledge, bledge, bledge, nn, na, nf, flag, pos, neg, point, incdnt} {erpios, errneg} {stprob, upprob, topper, topvert, toploop} {stprob, upprob, loprob} {term1, term2, term3, term4} {above} {below} {sink2} {oface} {facnum} {nodnum} {nterm} {sore} {sink1} {arcnum}</td>
</tr>
<tr>
<td>&gt; 0.5</td>
<td>{fnode, bnode, lface, rface, dnode, dface, label, fledge, bledge, bledge, nn, na, nf, flag, pos, neg, point, incdnt} {erpios, errneg} {stprob, upprob, topper, topvert, toploop} {stprob, upprob, loprob} {term1, term2, term3, term4} {above} {below} {sink2} {oface} {facnum} {nodnum} {nterm} {sore} {sink1} {arcnum} {topwye}</td>
</tr>
<tr>
<td>&gt; 0.7</td>
<td>{bnode} {rface} {dnode} {dface} {incdnt} {label} {fledge} {fledge} {bledge} {bledge} {pos} {neg} {point} {erpios} {errneg} {stprob} {topper} {topvert} {toploop} {stprob} {upprob} {lopob} {term1} {term2} {term3} {term4} {above} {below} {sink2} {oface} {facnum} {nodnum} {nterm} {sore} {sink1} {arcnum} {topwye} {nf} {nn} {na} {rface} {fnode} {flag}</td>
</tr>
<tr>
<td>&gt; 0.8</td>
<td>{bnode} {rface} {dnode} {dface} {incdnt} {label} {fledge} {fledge} {bledge} {bledge} {pos} {neg} {point} {erpios} {errneg} {stprob} {topper} {topvert} {toploop} {stprob} {upprob} {lopob} {term1} {term2} {term3} {term4} {above} {below} {sink2} {oface} {facnum} {nodnum} {nterm} {sore} {sink1} {arcnum} {topwye} {nf} {nn} {na} {rface} {fnode} {flag}</td>
</tr>
</tbody>
</table>

Figure 4.9
Threshold Table For COMMON Variables
increases, so does the number of singleton sets. Thus, after the 0.5 threshold level, the number of singleton sets becomes undesirable, and only continues to increase. Therefore, using the heuristics outlined for selecting a threshold value, 0.3 is selected. Thus, global variable analysis results in the extraction of 12 objects at the 0.3 threshold level. The complete set of corresponding object templates are given in Appendix A2, with a representative subset following in Figure 4.10. The objects in Figure 4.10 were chosen to represent varying degrees of complexity. Object 17, the more complex object, has nine methods while Object 21 has a single method and Object 23 has no methods, and serves to detect dead code.

Object 17 is

Attributes
fnode, bnode, lface, rface, dnode, dface, label : integer
fledge, fredge, bledge, bledge, nn, na, nf, flag, incdnt: integer
pos, neg, point, errpos, errneg : real

Methods

Method 1
begin
IF (BNODE(EDGE) .EQ. NODE) THEN
NODE1 = FNODE(EDGE)
NUM = FLEDGE(EDGE)
ELSE
BLEDGE(NUM) = FREDGE(EDGE)
ENDIF
NUM = FREDGE(EDGE)
IF(FLEDGE(NUM).EQ. EDGE) THEN
FLEDGE(NUM) = FREDGE(EDGE)
ELSE
FREDGE(NUM) = FREDGE(EDGE)
ENDIF

Figure 4.10
Extracted Object Templates

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ELSE
    BREDGE(NUM) = FLEDGE(EDGE)
ENDIF
ELSE
    NODE1 = BNODE(EDGE)
    NUM = BLEDGE(EDGE)
    IF(BREDGE(NUM).EQ. EDGE) THEN
        BREDGE(NUM) = BREDGE(EDGE)
    ELSE
        FLEDGE(NUM) = BREDGE(EDGE)
    END IF
ENDIF
    NUM = BREDGE(EDGE)
ENDIF
    IF(BLEDGE(NUM).EQ. EDGE) THEN
        BLEDGE(NUM) = BLEDGE(EDGE)
    ELSE
        FREDGE(NUM) = BLEDGE(EDGE)
    END IF
ENDIF
DNODE(NODE1) = DNODE(NODE1)-1
DFACE(NUM1) = DFACE(NUM1)-2
DNODE(NODE) = 0
LABEL(EDGE) = 0
NN=NN-1
NA=NA-1
end

Method2
begin
    IF (RFACE(EDGE) .EQ. FACE) THEN
        IF(BLEDGE(NUM).EQ. EDGE) THEN
            BLEDGE(NUM) = BLEDGE(EDGE)
        ELSE
            FREDGE(NUM) = BLEDGE(EDGE)
        END IF
        NUM = BLEDGE(EDGE)
        IF(FLEDGE(NUM).EQ. EDGE) THEN
            FLEDGE(NUM) = FLEDGE(EDGE)
        ELSE
            BREDGE(NUM) = FLEDGE(EDGE)
        END IF
    ENDIF
    NUM = BREDGE(EDGE)
    IF(FLEDGE(NUM).EQ. EDGE) THEN
        FLEDGE(NUM) = FLEDGE(EDGE)
    ELSE
        BREDGE(NUM) = FLEDGE(EDGE)
    END IF
    (figure continued)
ELSE
  NUM = BREDGE(EDGE)
  IF(FREDGE(NUM).EQ. EDGE) THEN
    FREDGE(NUM) = FREDGE(EDGE)
  ELSE
    BLEDGE(NUM) = FREDGE(EDGE)
  ENDIF
  NUM = FREDGE(EDGE)
  IF(BREDGE(NUM).EQ. EDGE) THEN
    BREDGE(NUM) = BREDGE(EDGE)
  ELSE
    FLEDGE(NUM) = BREDGE(EDGE)
  ENDIF
ENDIF
DFACE(FACE1) = DFACE(FACE1)-1
DNODE(NUM1) = DNODE(NUM1)-2
DFACE(FACE) = 0
LABEL(EDGE) = 0
NF=NF-1
NA=NA-1

end

Method3
begin
  ARC(1) = EDGE
  IF (BNODE(EDGE) .EQ. NODE) THEN
    ARC(2) = BREDGE(EDGE)
    ARC(3) = BLEDGE(EDGE)
  ELSE
    ARC(2) = FLEDGE(EDGE)
    ARC(3) = FREDGE(EDGE)
  ENDIF
  DO 10 I = 1,3
    ROT(I) = MOD(I,3) + 1
    IF (BNODE(ARC(I)) .EQ. NODE) THEN
      TEMP(1,I) = FNODE(ARC(I))
      TEMP(2,I) = RFACE(ARC(I))
      TEMP(3,I) = FREDGE(ARC(I))
      TEMP(4,I) = FLEDGE(ARC(I))
    ELSE
      (figure continued)
\[
\begin{align*}
\text{TEMP}(1,I) &= \text{BNODE}(\text{ARC}(I)) \\
\text{TEMP}(2,I) &= \text{LFACE}(\text{ARC}(I)) \\
\text{TEMP}(3,I) &= \text{BLEDGE}(\text{ARC}(I)) \\
\text{TEMP}(4,I) &= \text{BREDGE}(\text{ARC}(I)) \\
\text{END IF} \\
\text{TEMP}(5,I) &= \text{LABEL}(\text{ARC}(I))
\end{align*}
\]

10 CONTINUE

DO 20 I = 1,3
RFACE(ARC(I)) = NEWFAC
BNODE(ARC(I)) = TEMP(1,I)
LFACE(ARC(I)) = TEMP(2,I)
FNODE(ARC(I)) = TEMP(3,ROT(I))
BLEDGE(ARC(I)) = TEMP(4,1)
FREDGE(ARC(I)) = ARC(ROT(I))
BREDGE(ARC(I)) = ARC(ROT(ROT(I)))
LABEL(ARC(I)) = Min(TEMP(5,I),TEMP(5,ROT(I)))
20 CONTINUE

DFACE(NEWFAC) = 3
DO 25 I = 1,3
NUM = FREDGE(ARC(I))
IF(LFACE(NUM) .EQ. TEMP(2,I)) THEN
BLEDGE(NUM) = ARC(I)
ELSE
FREDGE(NUM) = ARC(I)
END IF
25 CONTINUE

DO 30 I = 1,3
NUM = LFACE(ARC(I))
DFACE(NUM) = DFACE(NUM) - 1
30 CONTINUE

DO 40 I = 1,3
NUM = FNODE(ARC(I))
DNODE(NUM) = DNODE(NUM) + 1
40 CONTINUE

DO 110 J = 1,10
DA = 1 - POS(ARC(1),J)
DB = 1 - POS(ARC(2),J)
DC = 1 - POS(ARC(3),J)
POS(ARC(1),J) = 1 - WC
POS(ARC(2),J) = 1 - WA

(figure continued)
\[ \text{POS(ARC(3),J)} = 1 - \text{WB} \]
\[ \text{ERRPOS(J)} = \text{ERRPOS(J)} + \left| \text{WA} \times \text{WB} \times \text{WC} - \text{DA} \times \text{DB} - \text{DA} \times \text{DC} - \text{DB} \times \text{DC} + 2 \times \text{DA} \times \text{DB} \times \text{DC} \right| \]
\[ \text{DA} = 1 - \text{NEG(ARC(1),J)} \]
\[ \text{DB} = 1 - \text{NEG(ARC(2),J)} \]
\[ \text{DC} = 1 - \text{NEG(ARC(3),J)} \]
\[ \text{NEG(ARC(1),J)} = 1 - \text{WC} \]
\[ \text{NEG(ARC(2),J)} = 1 - \text{WA} \]
\[ \text{NEG(ARC(3),J)} = 1 - \text{WB} \]
\[ \text{ERRNEG(J)} = \text{ERRNEG(J)} + \left| \text{WA} \times \text{WB} \times \text{WC} - \text{DA} \times \text{DB} - \text{DA} \times \text{DC} - \text{DB} \times \text{DC} + 2 \times \text{DA} \times \text{DB} \times \text{DC} \right| \]
\[ \text{DA} = 1 - \text{POINT(ARC(1),J)} \]
\[ \text{DB} = 1 - \text{POINT(ARC(2),J)} \]
\[ \text{DC} = 1 - \text{POINT(ARC(3),J)} \]
\[ \text{POINT(ARC(1),J)} = 1 - \text{WC} \]
\[ \text{POINT(ARC(2),J)} = 1 - \text{WA} \]
\[ \text{POINT(ARC(3),J)} = 1 - \text{WB} \]

110 \text{ CONTINUE}
\[ \text{DNODE(NODE)} = 0 \]
\[ \text{NN} = \text{NN} - 1 \]
\[ \text{NF} = \text{NF} + 1 \]

\text{end}

\text{Method4}
\text{begin}
\text{ARC(1)} = \text{EDGE}
\text{IF} (\text{RFACE(EDGE)} .EQ. \text{FACE}) \text{ THEN} \]
\[ \text{ARC(2)} = \text{FREDGE(EDGE)} \]
\[ \text{ARC(3)} = \text{BREDGE(EDGE)} \]
\text{ELSE}
\[ \text{ARC(2)} = \text{BLEDGE(EDGE)} \]
\[ \text{ARC(3)} = \text{FLEDGE(EDGE)} \]
\text{ENDIF}
\text{DO } 10 \text{ I} = 1,3
\[ \text{ROT(I)} = \text{MOD(I,3)} + 1 \]
\text{IF} (\text{RFACE(ARC(I)) .EQ. FACE}) \text{ THEN}
\[ \text{TEMP(1,I)} = \text{FNODE(ARC(I))} \]
\[ \text{TEMP(2,I)} = \text{LFACE(ARC(I))} \]
\[ \text{TEMP(3,I)} = \text{FLEDGE(ARC(I))} \]
\[ \text{TEMP(4,I)} = \text{BLEDGE(ARC(I))} \]
\text{(figure continued)
ELSE
    TEMP(1,I) = BNODE(ARC(I))
    TEMP(2,I) = RFACE(ARC(I))
    TEMP(3,I) = BREDGE(ARC(I))
    TEMP(4,I) = FREDGE(ARC(I))
ENDIF
    TEMP(5,I) = LABEL(ARC(I))
DO 20 I = 1,3
    BNODE(ARC(I)) = NEWNOD
    FNODE(ARC(I)) = TEMP(1,I)
    LFACE(ARC(I)) = TEMP(2,I)
    RFACE(ARC(I)) = TEMP(2,ROT(I))
    FLEDGE(ARC(I)) = TEMP(3,I)
    FREDGE(ARC(I)) = TEMP(4,ROT(I))
    BREDGE(ARC(I)) = ARC(ROT(I))
    BLEDGE(ARC(I)) = ARC(ROT(ROT(I)))
LABEL(ARC(I)) = MIN(TEMP(5,I), TEMP(5,ROT(I)))
20 CONTINUE
    DNODE(NEWNOD) = 3
DO 25 I = 1,3
    NUM = FREDGE(ARC(I))
    IF(FNODE(NUM) .EQ. TEMP(1,I)) THEN
        FLEDGE(NUM) = ARC(I)
    ELSE
        BREDGE(NUM) = ARC(I)
    ENDIF
25 CONTINUE
DO 30 I = 1,3
    NUM = RFACE(ARC(I))
    DFACE(NUM) = DFACE(NUM) + 1
30 CONTINUE
DO 40 I = 1,3
    NUM = FNODE(ARC(I))
    DNODE(NUM) = DNODE(NUM) - 1
40 CONTINUE
DO 110 J = 1,10
    DA = POS(ARC(1),J)
    DB = POS(ARC(2),J)
    DC = POS(ARC(3),J)
    POS(ARC(1),J) = WC
    POS(ARC(2),J) = WA

(figure continued)
\[ \text{POS}(\text{ARC}(3), J) = WB \]

\[ \text{ERRPOS}(J) = \text{ERRPOS}(J) + \text{DABS}(WA*WB*WC-DA*DB-DA*DC-DB*DC+2*DA*DB*DC) \]

\[ DA = \text{NEG}(\text{ARC}(1), J) \]
\[ DB = \text{NEG}(\text{ARC}(2), J) \]
\[ DC = \text{NEG}(\text{ARC}(3), J) \]
\[ \text{NEG}(\text{ARC}(1), J) = WC \]
\[ \text{NEG}(\text{ARC}(2), J) = WA \]
\[ \text{NEG}(\text{ARC}(3), J) = WB \]

\[ \text{ERRNEG}(J) = \text{ERRNEG}(J) + \text{DABS}(WA*WB*WC-DA*DB-DA*DC-DB*DC+2*DA*DB*DC) \]

\[ DA = \text{POINT}(\text{ARC}(1), J) \]
\[ DB = \text{POINT}(\text{ARC}(2), J) \]
\[ DC = \text{POINT}(\text{ARC}(3), J) \]
\[ \text{POINT}(\text{ARC}(1), J) = WC \]
\[ \text{POINT}(\text{ARC}(2), J) = WA \]
\[ \text{POINT}(\text{ARC}(3), J) = WB \]

\[ \text{DFACE}(\text{FACE}) = 0 \]
\[ NF = NF - 1 \]
\[ NN = NN + 1 \]

\text{end}

\text{Method5}
\text{begin}
\text{IF (RFACE(EDGE1).EQ. FACE) THEN}
\text{EDGE2 = FREDGE(EDGE1)}
\text{IF (RFACE(EDGE2).EQ. FACE) THEN}
\text{FREDGE(EDGE1) = BLEDGE(EDGE2)}
\text{BREDGE(EDGE1) = FLEDGE(EDGE2)}
\text{RFACE(EDGE1) = LFACE(EDGE2)}
\text{ELSE}
\text{FREDGE(EDGE1) = FREDGE(EDGE2)}
\text{BREDGE(EDGE1) = BREDGE(EDGE2)}
\text{RFACE(EDGE1) = RFACE(EDGE2)}
\text{ENDIF}
\text{NUM = FREDGE(EDGE1)}
\text{IF(BREDGE(NUM).EQ. EDGE2) THEN}
\text{BREDGE(NUM) = EDGE1}

\text{(figure continued)}
ELSE
    FLEDGE(NUM) = EDGE1
ENDIF
NUM = BREDGE(EDGE1)
IF (FREDGE(NUM) .EQ. EDGE2) THEN
    FREDGE(NUM) = EDGE1
ELSE
    BLEDGE(NUM) = EDGE1
ENDIF
ELSE
    EDGE2 = FLEDGE(EDGE1)
    IF (RFACE(EDGE2) .EQ. FACE) THEN
        FLEDGE(EDGE1) = FLEDGE(EDGE2)
        BLEDGE(EDGE1) = BLEDGE(EDGE2)
        LFACE(EDGE1) = LFACE(EDGE2)
    ELSE
        FLEDGE(EDGE1) = BREDGE(EDGE2)
        BLEDGE(EDGE1) = FREDGE(EDGE2)
        LFACE(EDGE1) = RFACE(EDGE2)
    ENDIF
    NUM = FLEDGE(EDGE1)
    IF (BLEDGE(NUM) .EQ. EDGE2) THEN
        BLEDGE(NUM) = EDGE1
    ELSE
        FREDGE(NUM) = EDGE1
    ENDIF
ELSE
    NUM = BREDGE(EDGE1)
    IF (FLEDGE(NUM) .EQ. EDGE2) THEN
        FLEDGE(NUM) = EDGE1
    ELSE
        BREDGE(NUM) = EDGE1
    ENDIF
ENDIF
LABEL(EDGE1) = MIN(LABEL(EDGE1), LABEL(EDGE2))
LABEL(EDGE2) = 0
NUM = FNODE(EDGE1)
DNODE(NUM) = DNODE(NUM)-1
1000 IF (RFACE(EDGE2) .EQ. FACE) THEN
    IF (INCDNT(LFACE(EDGE2)) .GT. 0)
        INCNT(LFACE(EDGE2)) = EDGE1
    ELSE
        INCNT(LFACE(EDGE2)) = EDGE1
    ENDIF
IF(INCDNT(RFACE(EDGE2)) .GT. 0)
    INCDNT(RFACE(EDGE2)) = EDGE1
ENDIF
DFACE(FACE)=0
DO 110 J = 1,10
    POS(EDGE1,J)=
        POS(EDGE1,J)+POS(EDGE2,J)-POS(EDGE1,J)*POS(EDGE2,J)
    POINT(EDGE1,J)=
        POINT(EDGE1,J)+POINT(EDGE2,J)-
        POINT(EDGE1,J)*POINT(EDGE2,J)
    NEG(EDGE1,J)=
        NEG(EDGE1,J)+NEG(EDGE2,J)-NEG(EDGE1,J)*NEG(EDGE2,J)
110    CONTINUE
    NF=NF-1
    NA=NA-1
end

Method6 begin
    IF (FNODE(EDGE1) .EQ. NODE) THEN
        EDGE2 = FLEDGE(EDGE1)
    IF (FNODE(EDGE2) .EQ. NODE) THEN
        FLEDGE(EDGE1) = BREDGE(EDGE2)
        FREDGE(EDGE1) = BLEDGE(EDGE2)
        FNODE(EDGE1) = BNODE(EDGE2)
    ELSE
        FLEDGE(EDGE1) = FLEDGE(EDGE2)
        FREDGE(EDGE1) = FREDGE(EDGE2)
        FNODE(EDGE1) = FNODE(EDGE2)
    ENDIF
    NUM = FLEDGE(EDGE1)
    IF (FREDGE(NUM) .EQ. EDGE2) THEN
        FREDGE(NUM) = EDGE1
    ELSE
        BLEDGE(NUM) = EDGE1
    ENDIF
    NUM = FREDGE(EDGE1)
    IF (FLEDGE(NUM) .EQ. EDGE2) THEN
        FLEDGE(NUM) = EDGE1
    ELSE
        BREDGE(NUM) = EDGE1
    ENDIF
(figure continued)
ELSE
  EDGE2 = BLEDGE(EDGE1)
  IF (FNODE(EDGE2) .EQ. NODE) THEN
    BREDGE(EDGE1) = BREDGE(EDGE2)
    BLEDGE(EDGE1) = BLEDGE(EDGE2)
    BNODE(EDGE1) = BNODE(EDGE2)
  ELSE
    BREDGE(EDGE1) = FREDGE(EDGE2)
    BLEDGE(EDGE1) = FREDGE(EDGE2)
    BNODE(EDGE1) = FNODE(EDGE2)
  ENDIF
  NUM = BREDGE(EDGE1)
  IF (BLEDGE(NUM) .EQ. EDGE2) THEN
    BLEDGE(NUM) = EDGE1
  ELSE
    FREDGE(NUM) = EDGE1
  ENDIF
  NUM = BLEDGE(EDGE1)
  IF (BREDGE(NUM) .EQ. EDGE2) THEN
    BREDGE(NUM) = EDGE1
  ELSE
    FLEDGE(NUM) = EDGE1
  ENDIF
ENDIF

LABEL(EDGE1) = MIN(LABEL(EDGE1), LABEL(EDGE2))
LABEL(EDGE2) = 0
NUM = RFACE(EDGE1)
DFACE(NUM) = DFACE(NUM)-1
1000 IF (BNODE(EDGE2) .EQ. NODE) THEN
  IF (INCDNT(FNODE(EDGE2)) .GT. 0)
    INCDNT(FNODE(EDGE2)) = EDGE1
  ELSE
    IF (INCDNT(BNODE(EDGE2)) .GT. 0)
      INCDNT(BNODE(EDGE2)) = EDGE1
  ENDIF
  DNODE(NODE) = 0
  DO 110 J = 1, 10
    POS(EDGE1, J) = POS(EDGE1, J)*POS(EDGE2, J)
    NEG(EDGE1, J) = NEG(EDGE1, J)*NEG(EDGE2, J)
    POINT(EDGE1, J) = POINT(EDGE1, J)*POINT(EDGE2, J)
 110 CONTINUE

(figure continued)
\texttt{NN=NN-1}  \\
\texttt{NA=NA-1}  \\
\texttt{end}  \\

\texttt{Method7}  \\
\texttt{begin}  \\
\texttt{READ(4,*) NN, NA, NF}  \\
\texttt{DO 15 J=1, NA}  \\
\texttt{READ(4,*) I, BNODE(I), FNODE(I), LFACE(I), RFACE(I)}  \\
\texttt{READ(4,*) BREDGE(I), BLEDGE(I), FREDGE(I), FREDGE(I)}  \\
\texttt{ARCNUM(J) = I}  \\
\texttt{15 CONTINUE}  \\
\texttt{DO 16 J=1, NN}  \\
\texttt{READ(4,*) I, DNODE(I)}  \\
\texttt{NODNUM(J) = I}  \\
\texttt{16 CONTINUE}  \\
\texttt{DO 17 K=1, NF}  \\
\texttt{READ(4,*) I, DFACE(I)}  \\
\texttt{FACNUM(K) = I}  \\
\texttt{17 CONTINUE}  \\
\texttt{READ(*,*) PNUM}  \\
\texttt{DO 110 J = 1, 10}  \\
\texttt{DO 47 I = 1, NA}  \\
\texttt{POS(I,J) = PNUM + J*0.02}  \\
\texttt{NEG(I,J) = PNUM + J*0.02}  \\
\texttt{POINT(I,J) = PNUM + J*0.02}  \\
\texttt{47 CONTINUE}  \\
\texttt{110 CONTINUE}  \\
\texttt{LABEL(START) = 1}  \\
\texttt{EBOT = START}  \\
\texttt{OCURR=START}  \\
\texttt{111 IF (BNODE(OCURR) .EQ. SORE) THEN}  \\
\texttt{SFACE(OCURR) = RFACE(OCURR)}  \\
\texttt{OCURR = BREDGE(OCURR)}  \\
\texttt{ELSE}  \\
\texttt{SFACE(OCURR) = LFACE(OCURR)}  \\
\texttt{OCURR = FREDGE(OCURR)}  \\
\texttt{ENDIF}  \\
\texttt{IF (OCURR .NE. START) THEN}  \\
\texttt{LABEL(OCURR) = 1}  \\
\texttt{NCOUNT = NCOUNT + 1}  \\

(figure continued)
NEXT(EBOT) = OCURR
EBOT = OCURR
NEXT(EBOT) = 0
GOTO 1111
ENDIF
137 ESCAN = ETOP
CFACE = SFACE(ESCAN)
WRITE(*,*) 'SCANNING EDGE #', ESCAN
ECURR = ESCAN
122 IF (CFACE .EQ. RFACE(ECURR)) THEN
    NUM = FNODE(ECURR)
    ECURR = FREDGE(ECURR)
ELSE
    NUM = BNODE(ECURR)
    ECURR = BLEDGE(ECURR)
ENDIF
. IF (LABEL(ECURR) .EQ. 0) THEN
    LABEL(ECURR) = LABEL(ESCAN) + 1
    NCOUNT = NCOUNT + 1
    WRITE(*,*) 'labelling edge #', ECURR, 'by label', LABEL(ECURR)
    IF (NCOUNT .EQ. NA) GOTO 1333
    SNODE(ECURR) = NUM
    IF (ETOP .EQ. 0 ) THEN
        OTOP = ECURR
    ELSE
        NEXT(OBOT) = ECURR
    ENDIF
    OBOT = ECURR
    NEXT( OBOT) = 0
ENDIF
IF (LABEL(ECURR) .EQ. LABEL(ESCAN)) THEN
    ETOP = NEXT(ETOP)
    IF (ETOP .EQ. 0 ) THEN
        IF(OTOP .EQ. 0 ) THEN
            GOTO 1333
        ELSE
            GOTO 237
        ENDIF
    ELSE
        GOTO 237
    ENDIF
ENDIF
GOTO 137
ENDIF

(figure continued)
GOTO 122
237 OSCAN = OTOP
    CNODE = SNODE(OSCAN)
    OCURR = OSCAN
222 IF (CNODE .EQ. BNODE(OCURR)) THEN
    NUM = LFACE(OCURR)
    OCURR = BLEDGE(OCURR)
ELSE
    NUM = RFACE(OCURR)
    OCURR = FREDGE(OCURR)
ENDIF
IF (LABEL(OCURR) .EQ. 0) THEN
    NCOUNT = NCOUNT + 1
    LABEL(OCURR) = LABEL(OSCAN) + 1
WRITE(*,*) 'labelling edge #', OCURR, 'by label', LABEL(OCURR)
    IF (NCOUNT .EQ. NA) GOTO 1333
    SFACE(OCURR) = NUM
    IF (ETOP .EQ. 0 ) THEN
        ETOP = OCURR
    ELSE
        NEXT(EBOT) = OCURR
    ENDIF
    EBOT = OCURR
    NEXT(EBOT) = 0
ENDIF
IF (LABEL(OCURR) .EQ. LABEL(OSCAN)) THEN
    OTOP = NEXT(OTOP)
    NEXT(OSCAN) = 0
    IF (OTOP .EQ. 0) THEN
        IF(ETOP .EQ. 0) THEN
            GOTO 1333
        ELSE
            GOTO 137
        ENDIF
    ENDIF
ENDIF
GOTO 237
ENDIF
GOTO 222
end

(figure continued)
Method 8
begin
INCDNT(NUM) = 0
ABOVE(BELOW(NUM)) = ABOVE(NUM)
BELOW(ABOVE(NUM)) = BELOW(NUM)
ABOVE(NUM) = 0
BELOW(NUM) = 0
end

Method 9
begin
IF (FLAG .EQ. 1) THEN
FACE = NUM
IF (DFACE(FACE) .EQ. 1) THEN
IF (TOPLOOP .GT. 0) THEN
ABOVE(TOPLOOP) = FACE
BELOW(FACE) = TOPLOOP
ENDIF
TOPLOOP = FACE
INCDNT(FACE) = ARC
GOTO 1000
ENDIF
ENDIF
IF (DFACE(FACE) .EQ. 2) THEN
IF (TOPPAR .GT. 0) THEN
ABOVE(TOPPAR) = FACE
BELOW(FACE) = TOPPAR
ENDIF
TOPPAR = FACE
INCDNT(FACE) = ARC
GOTO 1000
ENDIF
EDGE1 = ARC
IF (RFACE(EDGE1) .EQ. FACE) THEN
EDGE2 = FREDGE(EDGE1)
EDGE3 = BREDGE(EDGE1)
ELSE
EDGE2 = BLEDGE(EDGE1)
EDGE3 = FLEDGE(EDGE1)
ENDIF
NCHECK = MIN(LABEL(EDGE1), LABEL(EDGE2), LABEL(EDGE3))

(figure continued)
NSUM = LABEL(EDGE1) + LABEL(EDGE2) + LABEL(EDGE3)

IF (NSUM .EQ. (3 * NCHECK + 2)) THEN
  INCNDNT(FACE) = EDGE1
  IF (TOPDEL .GT. 0) THEN
    ABOVE(TOPDEL) = FACE
    BELOW(FACE) = TOPDEL
  ENDIF
  TOPDEL = FACE
ENDIF
GOTO 1000
ENDIF

NODE = NUM
IF (NODE .EQ. SORE) GOTO 1000
IF (NODE .EQ. TERM1) GOTO 1000
IF (NODE .EQ. TERM2) GOTO 1000
IF (NODE .EQ. TERM3) GOTO 1000
IF (NODE .EQ. TERM4) GOTO 1000
IF (DNODE(NODE) .EQ. 0) GOTO 1000
IF (DNODE(NODE) .EQ. 1) THEN
  IF (TOPVERT .GT. 0) THEN
    ABOVE(TOPVERT) = NODE
    BELOW(NODE) = TOPVERT
  ENDIF
  TOPVERT = NODE
  INCNDNT(NODE) = ARC
  GOTO 1000
ENDIF

IF (DNODE(NODE) .EQ. 2) THEN
  IF (TOPSER .GT. 0) THEN
    ABOVE(TOPSER) = NODE
    BELOW(NODE) = TOPSER
  ENDIF
  TOPSER = NODE
  INCNDNT(NODE) = ARC
  GOTO 1000
ENDIF

EDGE1 = ARC
IF (BNODE(EDGE1) .EQ. NODE) THEN
  EDGE2 = BREDGE(EDGE1)
  EDGE3 = BLEDGE(EDGE1)
ELSE
  (figure continued)
EDGE2 = FLEDGE(EDGE1)
EDGE3 = FREDGE(EDGE1)
ENDIF
NCHECK = MIN(LABEL(EDGE1), LABEL(EDGE2), LABEL(EDGE3))
NSUM = LABEL(EDGE1) + LABEL(EDGE2) + LABEL(EDGE3)
IF (NSUM .EQ. (3 * NCHECK + 2)) THEN
  INCNDT(NODE) = EDGE1
  IF (TOPWYE .GT. 0) THEN
    ABOVE(TOPWYE) = NODE
    BELOW(NODE) = TOPWYE
  ENDIF
  TOPWYE = NODE
ENDIF
end

SubDerivation {vertex, loop, wye, delta, parallel, series, remove, positive, main}

Object21 is
Attributes
above, below : integer

Methods

Method1
begin
  IF (DFACE(FACE) .EQ. 1) THEN
    IF (TOPLOOP .GT. 0) THEN
      ABOVE(TOPLOOP) = FACE
      BELOW(FACE) = TOPLOOP
    ENDIF
  ENDIF
  IF (DFACE(FACE) .EQ. 2) THEN
    IF (TOPPAR .GT. 0) THEN
      ABOVE(TOPPAR) = FACE
      BELOW(FACE) = TOPPAR
    ENDIF
  ENDIF
  IF (NSUM .EQ. (3 * NCHECK + 2)) THEN
    IF (TOPDEL .GT. 0) THEN
      ABOVE(TOPDEL) = FACE
      BELOW(FACE) = TOPDEL
    ENDIF
  ENDIF
end

(figure continued)
ENDIF
ENDIF
NODE = NUM
IF(DNODE(NODE) .EQ. 1) THEN
  IF(TOPVERT .GT. 0) THEN
    ABOVE(TOPVERT) = NODE
    BELOW(NODE) = TOPVERT
  ENDIF
ENDIF
IF(DNODE(NODE) .EQ. 2) THEN
  IF(TOPSER .GT. 0) THEN
    ABOVE(TOPSER) = NODE
    BELOW(NODE) = TOPSER
  ENDIF
ENDIF
IF (NSUM .EQ. (3*NCHECK+2)) THEN
  IF (TOPWYE .GT. 0) THEN
    ABOVE(TOPWYE) = NODE
    BELOW(NODE) = TOPWYE
  ENDIF
ENDIF
end

SubDerivation {positive}

Object23 is
Attributes
  oface : integer
Methods
  SubDerivation {}

Because object 22 and object 23 have no methods, a more in depth analysis is performed. These objects were determined to contain attributes that correspond to variables in the source code which are never used. That is, the attributes of object 22 and object 23 are never defined or referenced in the source code. Thus, the
declaration of these variables in the source code is unnecessary. It is in this manner that "dead code" can be detected during object extraction.

At this point, the object extraction process is completed. A total of 28 objects were extracted from the source code. Upon reviewing the extracted objects, two cases of dead code were detected. These two objects are then dropped from further consideration. Thus, class abstraction and instantiation of the inheritance hierarchy are performed on the remaining 26 objects. At this point, we begin class abstraction and inheritance hierarchy instantiation using the similarity technique. Similarity is measured in two distinct areas: attributes and methods. Then, the results are compiled and a class hierarchy is reported.

Attribute-based similarity is computed for the actual parameters using the algorithm given in Figure 3.10. The results are given in Figure 4.11.

<table>
<thead>
<tr>
<th>Threshold Value</th>
<th>Clusters</th>
</tr>
</thead>
<tbody>
<tr>
<td>&gt;= 0.0</td>
<td>(1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16)</td>
</tr>
<tr>
<td>&gt;= 0.2</td>
<td>(1, 10, 11) (2, 3, 4, 5, 6, 7, 8, 9, 12, 13, 14, 15, 16)</td>
</tr>
<tr>
<td>&gt;= 0.4</td>
<td>(1, 10, 11) (2, 3, 4, 5, 6, 7, 8, 9, 12, 13, 14, 15, 16)</td>
</tr>
<tr>
<td>&gt;= 0.6</td>
<td>(1) (10, 11) (2, 3, 4, 5, 6, 7, 8, 9, 12, 13, 14, 15, 16)</td>
</tr>
<tr>
<td>&gt;= 0.7</td>
<td>(1) (10, 11) (2, 3, 4, 5, 6, 7, 8, 9, 12, 13, 14, 15, 16)</td>
</tr>
<tr>
<td>** &gt;= 0.9</td>
<td>(1) (2, 6, 12) (10, 11) (3, 4, 5, 7, 8, 9, 13, 14, 15, 16)</td>
</tr>
</tbody>
</table>

Figure 4.11
Attribute-Based Similarity of Actual Parameters

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Next, method based similarity is computed using the algorithm in Figure 3.11. The results are shown in Figure 4.12.

<table>
<thead>
<tr>
<th>Threshold value</th>
<th>Clusters</th>
</tr>
</thead>
<tbody>
<tr>
<td>&gt;= 0.0</td>
<td>(1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16)</td>
</tr>
<tr>
<td>&gt;= 0.2</td>
<td>(1) (2) (3, 4, 5) (6, 7) (8) (9) (12) (10, 11, 13, 14, 15, 16)</td>
</tr>
<tr>
<td>** &gt;= 0.4</td>
<td>(1) (2) (3, 4, 5) (6, 7) (8) (9) (10, 11) (12) (13, 15) (14, 16)</td>
</tr>
<tr>
<td>&gt;= 0.7</td>
<td>(1) (2) (3, 4, 5) (6, 7) (8) (9) (10) (11) (12) (13, 15) (14, 16)</td>
</tr>
</tbody>
</table>

**Figure 4.12**
Method-Based Similarity of Actual Parameters

The results of the attribute-based similarity analysis and the method-based similarity analysis are used in the algorithm given in Figure 3.12 to generate clusters. Using either attribute clustering or method clustering techniques, two distinct sets of clusters are obtained from which the human reverse engineer selects to give the inheritance model. The clusters formed using attribute clustering are \{(1) (2, 6, 12) (3, 4, 5) (7, 8, 9) (10, 11) (13, 15) (14, 16)\}. The clusters formed using method clustering are \{(1) (2) (3, 4, 5) (6, 7) (8) (9) (10, 11) (12) (13, 15) (14, 16)\}. Next, attribute based similarity analysis is performed for the COMMON variables. The results are given in Figure 4.13.
Next, method-based similarity is computed. The results are given in Figure 4.14.

Using the attribute clustering techniques the following clusters are formed:

techniques, the following clusters are formed: (17) (18) (21) (19, 28) (24, 25) (20, 26, 27).

Because there are no identical objects, each of the objects extracted is abstracted as a class. The clusters obtained from combining threshold tables represent the clustering of the classes into the inheritance hierarchy. Either attribute-based clustering or method-based clustering is chosen and the corresponding clusters are used in the formation of the inheritance hierarchy. So, based on the clusters formed using method-based clustering, a parent class, say P1, is formed from classes 19 and 28. Likewise, P2 is formed from classes 24 and 25, and P3 is formed from classes 20, 26 and 27. Similarly for the clusters formed using attribute-based clustering.

After class abstraction is performed, the human reverse-engineer is given the option of attribute-based clustering or method-based clustering for the instantiation of the inheritance hierarchy. Choosing the attribute-based clustering for both parameter and global variable analysis results in the following inheritance hierarchy: (I) (2,6,12) (3,4,5) (7,8,9) (10,11) (13,15) (14,16) (17) (19) (21) (18, 20) (24, 25) (26, 27, 28). This means that classes (1) (17) (19) have no parent class. However, a parent class is abstracted for classes (2) (6) (12), namely, (2, 6, 12). Likewise, seven other parent classes are abstracted: (7, 8, 9) (10, 11) (13, 15) (14, 16) (18, 20) (24, 25) (26, 27, 28). A representative selection of the corresponding class templates follow in Figure 4.15. Classes were chosen to represent those that are formed of single objects (Class1 and Class2), as well as multiple objects.
(Class2-6-12). Similarly, classes were chosen that have no parent class (Class1, Class17, and Class2-6-12) as well as that have a parent class (Class2). Additionally, the classes were chosen which represent varying numbers of attributes and methods.

Class1 is {object1}

ParentClass  {}

Attributes
  main.pnum : real

Methods
  Method 1
  begin
    READ(*,*) PNUM
  end

Class2 is {object2}

ParentClass is {Class2-6-12}

Attributes
  vertex.node1, vertex.num : integer

Methods
  Method 1
  begin
    IF (BNODE(EDGE) .EQ. NODE) THEN
      NODE1 = FNODE(EDGE)
      NUM = FLEDGE(EDGE)
    IF (FREDGE(NUM).EQ. EDGE) THEN
      FREDGE(NUM) = FREDGE(EDGE)
    ENDIF
    NUM = FREDGE(EDGE)
    IF (FLEDGE(NUM).EQ. EDGE) THEN
      FLEDGE(NUM) = FLEDGE(EDGE)
   ENDIF
  end

Figure 4.15
Class Templates
ENDIF
ELSE
    NODE1 = BNODE(EDGE)
    NUM = BLEDGE(EDGE)
    IF(BREDGE(NUM).EQ. EDGE) THEN
        BREDGE(NUM) = BREDGE(EDGE)
    ENDIF
    NUM = BREDGE(EDGE)
ENDIF
end

Class2-6-12 is {object2, object6, object12}
  ParentClass is {}

Attributes
    vertex.node1, vertex.num : integer
    reduce.arc, reduce.node : integer
    initial.i, initial.num : integer

Methods

*** see object templates for object2, object6 and object 12 ***

Class17 is {object17}
  ParentClass {} 

Attributes
    fnode, bnode, fface, rface, dnode, dface, label : integer
    fledge, fredge, bledge, bledge, nn, na, nf, flag, incdnt: integer
    pos, neg, point, errpos, errneg : real

Methods

*** see object17 object template ***
The state interrogation templates represent which messages are passed among objects to interrogate state information. If a class references an attribute which is not an attribute or local variable of the class, then it is interrogating another class. Each method of every class is evaluated. The state interrogation templates are given in Figure 4.16.

A deeper analysis of the design indicates a statement coverage of 97% and displays the methodology's ability to detect dead code. Hence, the extraction process is complete and the object-oriented design and related design documents have been extracted from the FORTRAN source code.

Thus, the methodology is demonstrated successful for a system of moderate complexity. As expected, the objects and classes in this case study were more complex than those of the statistics case study. This is due to the increased

Class 17
Method 9 interrogates Class 18.toppar
Method 9 interrogates Class 18.topser
Method 9 interrogates Class 18.topvert
Method 9 interrogates Class 18.toploop

Class 18
Method 1 interrogates Class 21.below
Method 2 interrogates Class 17.dface
Method 2 interrogates Class 17.dnode

Class 19
Method 1 interrogates Class 17.pos
Method 1 interrogates Class 17.neg
Method 1 interrogates Class 17.point
Method 3 interrogates Class 17.pos

Figure 4.16
State Interrogation Templates

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Method3 interrogates Class17.neg
Method3 interrogates Class17.point

Class20
Method2 interrogates Class27.sore

Class21
Method1 interrogates Class17.dface
Method1 interrogates Class17.dnode
Method1 interrogates Class18.topdel
Method1 interrogates Class18.toppar
Method1 interrogates Class18.topser
Method1 interrogates Class18.topwyne
Method1 interrogates Class18.toploop

Class24
Method1 interrogates Class17.nf

Class25
Method1 interrogates Class17.nn

Class28
Method1 interrogates Class17.bnode
Method1 interrogates Class17.fnode

complexity in the original system itself, which the diagrams resulting from the methodology mirror accurately. One major factor in this complexity is the extensive use of COMMON variables. Their influence can be clearly seen in the state interrogation templates which tell when a class must interrogate the state of another class. This type of message passing is greatly increased by the use of COMMON variables in the original system. Additionally, the methodology was able to detect dead code in the system. Due to the magnitude of the original system, and the lack of documentation, there is a high probability that the dead code would have continued to go undetected under routine maintenance. Finally, the class hierarchy
is also demonstrative of the complexity of the system. In a system of little or no complexity, there would have been fewer classes with a small or no hierarchy.

4.3 Summary

The two case studies in this chapter demonstrate varying degrees of difficulty. The statistics case study demonstrates the accuracy of the methodology for small systems. In addition to the validation of the extracted design using the metrics of statement coverage and functional equivalence, evaluation of the extracted design indicates that it exhibits the qualities expected. The graph case study demonstrates the scalability of the methodology. This system is more complex because of increased lines of code and extensive use of global variables in the form of the COMMON block. Again, the results of the methodology are as expected. The extracted design includes a more sophisticated inheritance hierarchy. The extensive use of COMMON variables results in the necessity for numerous state interrogations, which is portrayed in the state interrogation diagrams. Thus, through the case studies, we have demonstrated that the methodology successfully extracts an object-oriented design from systems of varying complexity.
Chapter 5

Conclusions and Future Research

The goal of this research was to study the issues related to migrating legacy systems coded in imperative languages to the object-oriented paradigm and to develop reverse-engineering techniques to facilitate the migration. Section 5.1 summarizes the contributions resulting from this work. Section 5.2 describes future work.

5.1 Contributions

FORM facilitates the extraction of an object-oriented design from imperative FORTRAN code using graph theory combined with a data-driven approach. The contributions of the work include:

- The simultaneous paradigm shift and design extraction facilitates the migration of legacy systems to updated technologies, specifically the object-oriented paradigm.
- The extraction of a design from legacy code allows necessary maintenance to be performed at a higher level of abstraction, specifically the design level, thereby reducing current and future maintenance costs.
- System functionalities which are otherwise lost due to incomplete or inaccurate documentation are recovered.
• Issues related to the necessity of the development of software metrics specifically for reverse engineering are identified.

Thus, the research results in a comprehensive methodology, the development of which identified several open problems in the area of reverse engineering. Throughout the development of FORM are various contributions to the area of reverse engineering including the following:

• The construction of new algorithms, including algorithms to resolve actual parameter aliasing, determine placeholders in the COMMON block of FORTRAN, resolve the COMMON block of FORTRAN, extract attributes from formal parameters and global variables, extract methods for candidate objects, and form class clusters to abstract an inheritance hierarchy.

• The formulation and proof of lemmas which determine the class cardinality in the object model and the method cardinality for each class.

These contributions will now be related to the various phases of the methodology. The preprocessing phase, which prepares the code for extraction, required the development of algorithms to resolve the aliases in the actual parameters and the COMMON block.

The first phase of the methodology, Object Extraction, uses a data-driven approach to define candidate objects in the imperative code. This required the development and definition of such concepts as weighted adjacency matrix and
thresholding. Additionally, modifications to the traditional program slicing were required to facilitate the definition of methods of the candidate objects.

Phase two, Class Abstraction, uses the concept of identical objects to facilitate the forming of classes from the candidate objects. The classes are partitioned into equivalence classes which are mapped into unique classes in the object model. This results in Lemma 3.1 which describes the relationship among the cardinality of the set of classes in the object model, the set of object equivalence classes, and the set of objects. To complete phase two, the methods are extracted. This is done by first determining the number of methods contained in a class and then instantiating the methods. This results in the development of Lemma 3.2 which describes the relationship between the number of methods of a class in the object model and a class in the object equivalence class. The corresponding lemmas are stated and proved.

Phase three, Abstraction of the Inheritance Hierarchy, defines the concept of similarity analysis of object classes and uses this analysis to develop a class clustering technique. The definition of these techniques involved the development of algorithms to calculate both attribute-based similarity and method-based similarity.

Thus, the research has resulted in the development of a methodology to extract object-oriented designs from imperative legacy systems, with specific attention given to FORTRAN. The benefits of using the methodology include: the ability to capture system functionality which may not be apparent due to poor
system structure, and the reduction of future maintenance costs of the system as a
direct effect of accurate system documentation and updated programming

techniques.

5.2 Future Research

The research described in this dissertation has numerous potential future
directions. At this point several research opportunities exist:

- The next phase in the reverse-engineering process involves the abstraction of the
  object-oriented design into a formal specification. This phase requires the
  investigation of the current formal specification languages for the object-
  oriented paradigm and possible extension of such languages.

- The development of techniques to translate the design into an object-oriented
  implementation would be a valuable extension.

- The research could be further extended by formulating an adaptation of the
  methodology to other imperative languages (such as COBOL) or to other
  paradigms.

- The development of metrics to measure features specifically related to reverse-
  engineered systems is a possible area of research.

- Related to the research of reverse-engineered system metrics is that of
  refinement. With a suite of metrics defined for a reverse-engineered design, the
  area of refinement of a design with respect to the metrics is envisioned as future
  research.
References


[Bigg90] Biggerstaff, T.J. "Human-Oriented Conceptual Abstractions in the Reengineering of Software" In IEEE Conference on Software Engineering, 1990, pp 120.


Appendix A1
Object Templates for Actual Parameters

Object1 is
Attributes
    main.pnum : real

Methods

Method 1
begin
    READ(*,*) PNUM
end

SubDerivation {Main}

Object2 is
Attributes
    vertex.node1, vertex.num : integer

Methods

Method 1
begin
    IF (BNODE(EDGE) .EQ. NODE) THEN
        NODE1 = FNODE(EDGE)
        NUM  = FLEDGE(EDGE)
        IF (FREDGE(NUM).EQ. EDGE) THEN
            FREDGE(NUM) = FREDGE(EDGE)
        ENDIF
    NUM  = FREDGE(EDGE)
    IF (FLEDGE(NUM).EQ. EDGE) THEN
        FLEDGE(NUM) = FLEDGE(EDGE)
    ENDIF
ELSE
    NODE1 = BNODE(EDGE)
    NUM  = BLEDGE(EDGE)
    IF (BREDGE(NUM).EQ. EDGE) THEN
        BREDGE(NUM) = BREDGE(EDGE)
    ENDIF
ENDIF
NUM = BREDGE(EDGE)
ENDIF

SubDerivation {Vertex}

Object3 is
Attributes
loop.face1 : integer

Methods
Method1
begin
IF (RFACE(EDGE) .EQ. FACE) THEN
FACE1 = LFACE(EDGE)
ELSE
FACE1 = RFACE(EDGE)
ENDIF
end

SubDerivation {Loop}

Object4 is
Attributes
loop.num1 : integer

Methods
Method1
begin
NUM1 = BNODE(EDGE)
end

SubDerivation {Loop}

Object5 is
Attributes
loop.num : integer

Methods
Method 1
begin
    IF (RFACE(EDGE) .EQ. FACE) THEN
        NUM = FLEDGE(EDGE)
        IF (BLEDGE(NUM).EQ. EDGE) THEN
            BLEDGE(NUM) = BLEDGE(EDGE)
        ENDIF
        NUM = BLEDGE(EDGE)
    ELSE
        NUM = BREDGE(EDGE)
        IF (FREDGE(NUM).EQ. EDGE) THEN
            FREDGE(NUM) = FREDGE(EDGE)
        ENDIF
        NUM = FREDGE(EDGE)
    ENDIF
end

SubDerivation {Loop}

Object6 is
Attributes
    reduce.arc, reduce.node : integer

Methods

Method1
begin
    10   IF (TOPLOOP .GT. 0) THEN
        ARC = INCDNT(TOPLOOP)
        GOTO 10
    ENDIF
    IF (TOPVERT .GT. 0) THEN
        NODE = TOPVERT
        ARC = INCDNT(TOPVERT)
        GOTO 10
    ENDIF
    IF (TOPSER .GT. 0) THEN
        NODE = TOPSER
        ARC = INCDNT(TOPSER)
        GOTO 10
    ENDIF
    20   IF (TOPPAR .GT. 0) THEN

ARC = INCDNT(TOPPAR)
GOTO 10
ENDIF
30 IF (TOPWYE .GT. 0) THEN
   NODE = TOPWYE
   ARC = INCDNT(TOPWYE)
   GOTO 10
ENDIF
40 IF (TOPDEL .GT. 0) THEN
   ARC = INCDNT(TOPDEL)
   GOTO 10
ENDIF
end

SubDerivation {Reduce}

Object7 is
Attributes
   reduce.face : integer

Methods

Method1
begin
10 IF (TOPLOOP .GT. 0) THEN
   FACE = TOPLOOP
   GOTO 10
ENDIF
20 IF (TOPPAR .GT. 0) THEN
   FACE = TOPPAR
   GOTO 10
ENDIF
40 IF (TOPDEL .GT. 0) THEN
   FACE = TOPDEL
   GOTO 10
ENDIF
end

SubDerivation {Reduce}

Object8 is
Attributes

    series.num : integer

Methods

Method1
    begin
        IF (FNODE(EDGE1) .EQ. NODE) THEN
            EDGE2 = FLEDGE(EDGE1)
            IF (FNODE(EDGE2) .EQ. NODE) THEN
                FLEDGE(EDGE1) = BREDGE(EDGE2)
            ELSE
                FLEDGE(EDGE1) = FLEDGE(EDGE2)
            ENDIF
            NUM = FLEDGE(EDGE1)
            IF (FREDGE(NUM) .EQ. EDGE2) THEN
                FREDGE(NUM) = EDGE1
            ENDIF
            NUM = FREDGE(EDGE1)
        ELSE
            EDGE2 = BLEDGE(EDGE1)
            IF (FNODE(EDGE2) .EQ. NODE) THEN
                BREDGE(EDGE1) = BREDGE(EDGE2)
                BLEDGE(EDGE1) = BLEDGE(EDGE2)
            ELSE
                BREDGE(EDGE1) = FLEDGE(EDGE2)
                BLEDGE(EDGE1) = FREDGE(EDGE2)
            ENDIF
            NUM = BREDGE(EDGE1)
            IF (BLEDGE(NUM) .EQ. EDGE2) THEN
                BLEDGE(NUM) = EDGE1
            ENDIF
            NUM = BLEDGE(EDGE1)
        ENDIF
        NUM = RFACE(EDGE1)
        IF (NUM .EQ. LFACE(EDGE1)) THEN
            ELSE
                NUM = LFACE(EDGE1)
        ENDIF

SubDerivation {Series}

Object9 is
Attributes
  parallel.num : integer

Methods

Method 1
begin
  IF (RFACE(EDGE1) .EQ. FACE) THEN
    EDGE2 = FREDGE(EDGE1)
    IF (RFACE(EDGE2) .EQ. FACE) THEN
      FREDGE(EDGE1) = BLEDGE(EDGE2)
      BREDGE(EDGE1) = FLEDGE(EDGE2)
    ELSE
      FREDGE(EDGE1) = FREDGE(EDGE2)
      BREDGE(EDGE1) = BREDGE(EDGE2)
    ENDIF
    NUM = FREDGE(EDGE1)
    IF (BREDGE(NUM).EQ. EDGE2) THEN
      BREDGE(NUM) = EDGE1
    ENDIF
    NUM = BREDGE(EDGE1)
  ELSE
    EDGE2 = FLEDGE(EDGE1)
    IF (RFACE(EDGE2) .EQ. FACE) THEN
      FLEDGE(EDGE1) = FLEDGE(EDGE2)
      BLEDGE(EDGE1) = BLEDGE(EDGE2)
    ELSE
      FLEDGE(EDGE1) = BREDGE(EDGE2)
      BLEDGE(EDGE1) = FREDGE(EDGE2)
    ENDIF
    NUM = FLEDGE(EDGE1)
    IF (BLEDGE(NUM).EQ. EDGE2) THEN
      BLEDGE(NUM) = EDGE1
    ENDIF
    NUM = BLEDGE(EDGE1)
  ENDIF
  NUM = FNODE(EDGE1)
  IF (NUM .EQ. BNODE(EDGE1)) THEN
  ELSE
    NUM = BNODE(EDGE1)
  ENDIF
end
SubDerivation \{Parallell\}

Object 10 is
Attributes
\texttt{wye.k, wye.da, wye.db, wye.dc, wye.wa, wye.wb, wye.wc : real}

Methods

Method 1
\begin{verbatim}
begin
ARC(1) = EDGE
IF (BNODE(EDGE) .EQ. NODE) THEN
   ARC(2) = BREDGE(EDGE)
   ARC(3) = BLEDGE(EDGE)
ELSE
   ARC(2) = FLEDGE(EDGE)
   ARC(3) = FREDGE(EDGE)
ENDIF
DO 110 J = 1,10
   DA = 1- POS(ARC(1),J)
   DB = 1- POS(ARC(2),J)
   DC = 1- POS(ARC(3),J)
   RHO = DA*DB*DC - (DA+DB+DC) + 1
   IF (RHO .GT. 0 ) THEN
      K = 1.0
   ELSE
      K = 0.0
   ENDIF
   POS(ARC(1),J) = 1-WC
   POS(ARC(2),J) = 1-WA
   POS(ARC(3),J) = 1-WB
   DA = 1- NEG(ARC(1),J)
   DB = 1- NEG(ARC(2),J)
   DC = 1- NEG(ARC(3),J)
   RHO = DA*DB*DC - (DA+DB+DC) + 1
   IF (RHO .GT. 0 ) THEN
      K = 0.0
   ELSE
      K = 1.0
   ENDIF
   DA = 1- POINT(ARC(1),J)
   DB = 1- POINT(ARC(2),J)
\end{verbatim}
\end{verbatim}
DC = 1- POINT(ARC(3),J)
K = 0.5
POINT(ARC(1),J) = 1-WC
POINT(ARC(2),J) = 1-WA
POINT(ARC(3),J) = 1-WB
110 CONTINUE
end

Method2
begin
IF ( K .EQ. 0 ) THEN
A1 = DA + DB*DC - DA*DB*DC
B1 = DB + DA*DC - DA*DB*DC
C1 = DC + DB*DA - DA*DB*DC
WA = DSQRT(B1*C1/A1)
WB = DSQRT(A1*C1/B1)
WC = DSQRT(B1*A1/C1)
ENDIF
IF (DABS(WA-WB) .LE. 0.00001) THEN
ELSE
WC = (1-DC)*(DB-DA)/(WA-WB)
ENDIF
end

SubDerivation {Wye, Transform}

Object 11 is
Attributes
delta.k, delta.da, delta.db, delta.dc, delta.wa, delta.wb, delta.wc: real

Methods

Method1
begin
IF ( K .EQ. 0 ) THEN
A1 = DA + DB*DC - DA*DB*DC
B1 = DB + DA*DC - DA*DB*DC
C1 = DC + DB*DA - DA*DB*DC
WA = DSQRT(B1*C1/A1)

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WB = DSQRT(A1*C1/B1)
WC = DSQRT(B1*A1/C1)
ENDIF
IF (DABS(WA-WB) .LE. 0.00001) THEN
ELSE
   WC = (1-DC)*(DB-DA)/(WA-WB)
ENDIF
end

Method2
begin
ARC(1) = EDGE
IF (RFACE(EDGE) .EQ. FACE) THEN
   ARC(2) = FREDGE(EDGE)
   ARC(3) = BREDGE(EDGE)
ELSE
   ARC(2) = BLEDGE(EDGE)
   ARC(3) = FLEDGE(EDGE)
ENDIF
DO 110 J =1,10
   DA = POS(ARC(1),J)
   DB = POS(ARC(2),J)
   DC = POS(ARC(3),J)
   RHO = DA*DB*DC - (DA+DB+DC) + 1
   IF (RHO .GT. 0 ) THEN
      K = 0.0
   ELSE
      K = 1.0
   ENDIF
   POS(ARC(1),J) = WC
   POS(ARC(2),J) = WA
   POS(ARC(3),J) = WB
   DA = NEG(ARC(1),J)
   DB = NEG(ARC(2),J)
   DC = NEG(ARC(3),J)
   RHO = DA*DB*DC - (DA+DB+DC) + 1
   IF (RHO .GT. 0 ) THEN
      K = 1.0
   ELSE
      K = 0.0
   ENDIF
   NEG(ARC(1),J) = WC
   NEG(ARC(2),J) = WA
NEG(ARC(3),J) = WB
DA = POINT(ARC(1),J)
DB = POINT(ARC(2),J)
DC = POINT(ARC(3),J)
K = 0.5
POINT(ARC(1),J) = WC
POINT(ARC(2),J) = WA
POINT(ARC(3),J) = WB
110 CONTINUE
end

SubDerivation {Transform, Delta}

Object12 is
Attributes
    initial.i, initial.num : integer

Methods

Method1
begin
    DO 10 J = 1, NA
        I = ARCNUM(J)
        NUM = BNODE(I)
        IF (INCDNT(NUM) .NE. 0) GOTO 20
20        NUM = FNODE(I)
        IF (INCDNT(NUM) .NE. 0) GOTO 30
30        NUM = LFACE(I)
        IF (INCDNT(NUM) .NE. 0) GOTO 40
40        NUM = RFACED
10 CONTINUE
end

SubDerivation {Initial}

Object13 is
Attributes
    wye.num : integer

Methods

Method1
begin
    ARC(1) = EDGE
    IF (BNODE(EDGE) .EQ. NODE) THEN
        ARC(2) = BREDGE(EDGE)
        ARC(3) = BLEdge(EDGE)
    ELSE
        ARC(2) = FLEDGE(EDGE)
        ARC(3) = FREDGE(EDGE)
    ENDIF
    DO 10 I = 1,3
        ROT(I) = MOD(I,3) + 1
        IF (BNODE(ARC(I)) .EQ. NODE) THEN
            TEMP(1,I) = FNODE(ARC(I))
            TEMP(2,I) = RFACE(ARC(I))
            TEMP(3,I) = FREDGE(ARC(I))
            TEMP(4,I) = FREDGE(ARC(I))
        ELSE
            TEMP(1,I) = BNODE(ARC(I))
            TEMP(2,I) = LFACE(ARC(I))
            TEMP(3,I) = BLEdge(ARC(I))
            TEMP(4,I) = BLEdge(ARC(I))
        ENDIF
        TEMP(5,I) = LABEL(ARC(I))
    10 CONTINUE
    DO 20 I = 1,3
        LFACE(ARC(I)) = TEMP(2,I)
        FNODE(ARC(I)) = TEMP(1,ROT(I))
        FREDGE(ARC(I)) = TEMP(4,ROT(I))
    20 CONTINUE
    DO 30 I = 1,3
        NUM = LFACE(ARC(I))
    30 CONTINUE
    DO 40 I = 1,3
        NUM = FNODE(ARC(I))
    40 CONTINUE
end

SubDerivation {Wye}

Object 14
Attributes
delta, num : integer

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Methods

Method 1
begin
    ARC(1) = EDGE
    IF (RFACE(EDGE) .EQ. FACE) THEN
        ARC(2) = FREDGE(EDGE)
        ARC(3) = BREDGE(EDGE)
    ELSE
        ARC(2) = BLEDGE(EDGE)
        ARC(3) = FLEDGE(EDGE)
    ENDIF
    DO 10 I = 1,3
        IF (RFACE(ARC(I)) .EQ. FACE) THEN
            TEMP(1,I) = FNODE(ARC(I))
            TEMP(2,I) = LFACE(ARC(I))
            TEMP(3,I) = FLEDGE(ARC(I))
            TEMP(4,I) = BLEDGE(ARC(I))
        ELSE
            TEMP(1,I) = BNODE(ARC(I))
            TEMP(2,I) = RFACE(ARC(I))
            TEMP(3,I) = BREDGE(ARC(I))
            TEMP(4,I) = FREDGE(ARC(I))
        ENDIF
        TEMP(5,I) = LABEL(ARC(I))
    10 CONTINUE
    DO 20 I = 1,3
        FNODE(ARC(I)) = TEMP(1,I)
        RFACE(ARC(I)) = TEMP(2,ROT(I))
        FREDGE(ARC(I)) = TEMP(4,ROT(I))
    20 CONTINUE
    DO 25 I = 1,3
        NUM = RFACE(ARC(I))
    25 CONTINUE
    DO 30 I = 1,3
        NUM = RFACE(ARC(I))
    30 CONTINUE
    DO 40 I = 1,3
        NUM = FNODE(ARC(I))
    40 CONTINUE
end
SubDerivation \{\text{Delta}\}

Object 15 is
Attributes
\text{wye}.\text{arc}(i) : \text{integer}

Methods
Method 1
begin
\text{ARC}(1) = \text{EDGE}
\text{IF} (\text{BNODE}(\text{EDGE}) \text{ EQ. NODE}) \text{THEN}
\text{ARC}(2) = \text{BREDGE}(\text{EDGE})
\text{ARC}(3) = \text{BLEDGE}(\text{EDGE})
\text{ELSE}
\text{ARC}(2) = \text{FLEDGE}(\text{EDGE})
\text{ARC}(3) = \text{FREDGE}(\text{EDGE})
\text{ENDIF}
end

SubDerivation \{\text{Wye}\}

Object 16 is
Attributes
\text{delta}.\text{arc}(i) : \text{integer}

Methods
Method 1
begin
\text{ARC}(1) = \text{EDGE}
\text{IF} (\text{RFACE}(\text{EDGE}) \text{ EQ. FACE}) \text{THEN}
\text{ARC}(2) = \text{FREDGE}(\text{EDGE})
\text{ARC}(3) = \text{BREDGE}(\text{EDGE})
\text{ELSE}
\text{ARC}(2) = \text{BLEDGE}(\text{EDGE})
\text{ARC}(3) = \text{FREDGE}(\text{EDGE})
\text{ENDIF}
end

SubDerivation \{\text{Delta}\}
Appendix A2
Object Templates for COMMON Variables

Object 17 is

Attributes  
fnode, bnode, iface, rface, dnode, dface, label : integer  
fledge, fredge, bredge, bledge, nn, na, nf, flag, incdnt: integer  
pos, neg, point, errpos, errneg : real

Methods

Method 1
begin
  IF (BNODE(EDGE) .EQ. NODE) THEN
    NODE1 = FNODE(EDGE)
    NUM = FLEDGE(EDGE)
    IF(FREDGE(NUM).EQ. EDGE) THEN
      FREDGE(NUM) = FREDGE(EDGE)
    ELSE
      BREDGE(NUM) = FREDGE(EDGE)
    ENDIF
    NUM = FREDGE(EDGE)
    IF(FLEDGE(NUM).EQ. EDGE) THEN
      FLEDGE(NUM) = FLEDGE(EDGE)
    ELSE
      BREDGE(NUM) = FREDGE(EDGE)
    ENDIF
  ELSE
    NODE1 = BNODE(EDGE)
    NUM = BLEDGE(EDGE)
    IF(BREDGE(NUM).EQ. EDGE) THEN
      BREDGE(NUM) = BREDGE(EDGE)
    ELSE
      FLEDGE(NUM) = BREDGE(EDGE)
    ENDIF
    NUM = BREDGE(EDGE)
    IF(BLEDGE(NUM).EQ. EDGE) THEN
      BLEDGE(NUM) = BLEDGE(EDGE)
    ELSE
      FREDGE(NUM) = BLEDGE(EDGE)
    ENDIF
  ENDIF
ENDIF
DNODE(NODE1) = DNODE(NODE1) - 1
DFACE(NUM1) = DFACE(NUM1) - 2
DNODE(NODE) = 0
LABEL(EDGE) = 0
NN = NN - 1
NA = NA - 1
end

Method2
begin
IF (RFACE(EDGE) .EQ. FACE) THEN
IF (BLEDGE(NUM).EQ. EDGE) THEN
BLEDGE(NUM) = BLEDGE(EDGE)
ELSE
FREDGE(NUM) = BLEDGE(EDGE)
ENDIF
NUM = BLEDGE(EDGE)
IF (FLEDGE(NUM).EQ. EDGE) THEN
FLEDGE(NUM) = FLEDGE(EDGE)
ELSE
BREDGE(NUM) = FLEDGE(EDGE)
ENDIF
ELSE
NUM = BREDGE(EDGE)
IF (FREDGE(NUM).EQ. EDGE) THEN
FREDGE(NUM) = FREDGE(EDGE)
ELSE
BLEDGE(NUM) = FREDGE(EDGE)
ENDIF
NUM = FREDGE(EDGE)
IF (BREDGE(NUM).EQ. EDGE) THEN
BREDGE(NUM) = BREDGE(EDGE)
ELSE
FLEDGE(NUM) = BREDGE(EDGE)
ENDIF
ENDIF
DFACE(FACE1) = DFACE(FACE1) - 1
DNODE(NUM1) = DNODE(NUM1) - 2
DFACE(FACE) = 0
LABEL(EDGE) = 0
NF = NF - 1
NA = NA - 1

end

Method 3
begin
ARC(1) = EDGE
IF (BNODE(EDGE) .EQ. NODE) THEN
ARC(2) = BREDGE(EDGE)
ARC(3) = BLEDGE(EDGE)
ELSE
ARC(2) = FLEDGE(EDGE)
ARC(3) = FREDGE(EDGE)
ENDIF
DO 10 I = 1,3
ROT(I) = MOD(I,3) + 1
IF (BNODE(ARC(I)) .EQ. NODE) THEN
TEMP(1,I) = FNODE(ARC(I))
TEMP(2,I) = RFACE(ARC(I))
TEMP(3,I) = BLEDGE(ARC(I))
TEMP(4,I) = FREDGE(ARC(I))
ELSE
TEMP(1,I) = BNODE(ARC(I))
TEMP(2,I) = LFACE(ARC(I))
TEMP(3,I) = BLEDGE(ARC(I))
TEMP(4,I) = BREDGE(ARC(I))
ENDIF
TEMP(5,I) = LABEL(ARC(I))
10 CONTINUE
DO 20 I = 1,3
RFACE(ARC(I)) = NEWFAC
BNODE(ARC(I)) = TEMP(1,I)
LFACE(ARC(I)) = TEMP(2,I)
FNODE(ARC(I)) = TEMP(1,ROT(I))
BLEDGE(ARC(I)) = TEMP(3,I)
FLEDGE(ARC(I)) = TEMP(4,ROT(I))
FREDGE(ARC(I)) = ARC(ROT(I))
BREDGE(ARC(I)) = ARC(ROT(ROT(I)))
LABEL(ARC(I)) = MIN(TEMP(5,I),TEMP(5,ROT(I)))
20 CONTINUE
DFACE(NEWFAC) = 3
DO 25 I = 1,3
NUM = FLEDGE(ARC(I))
IF(LFACE(NUM) .EQ. TEMP(2,I)) THEN
    BEDGE(NUM) = ARC(I)
ELSE
    FREDGE(NUM) = ARC(I)
ENDIF

25 CONTINUE
DO 30 I = 1,3
    NUM = LFACE(ARC(I))
    DFACE(NUM) = DFACE(NUM) - 1
30 CONTINUE

DO 40 I = 1,3
    NUM = FNODE(ARC(I))
    DNODE(NUM) = DNODE(NUM) + 1
40 CONTINUE

DO 110 J = 1,10
    DA = 1 - POS(ARC(1),J)
    DB = 1 - POS(ARC(2),J)
    DC = 1 - POS(ARC(3),J)
    POS(ARC(1),J) = 1 - WC
    POS(ARC(2),J) = 1 - WA
    POS(ARC(3),J) = 1 - WB
    ERRPOS(J) = ERRPOS(J) + DABS(WA*WB*WC - DA*DB*DC - 2*DA*DB*DC)
    DA = 1 - NEG(ARC(1),J)
    DB = 1 - NEG(ARC(2),J)
    DC = 1 - NEG(ARC(3),J)
    NEG(ARC(1),J) = 1 - WC
    NEG(ARC(2),J) = 1 - WA
    NEG(ARC(3),J) = 1 - WB
    ERRNEG(J) = ERRNEG(J) + DABS(WA*WB*WC - DA*DB*DC - 2*DA*DB*DC)
    DA = 1 - POINT(ARC(1),J)
    DB = 1 - POINT(ARC(2),J)
    DC = 1 - POINT(ARC(3),J)
    POINT(ARC(1),J) = 1 - WC
    POINT(ARC(2),J) = 1 - WA
    POINT(ARC(3),J) = 1 - WB
110 CONTINUE

DNODE(NODE) = 0
NN = NN - 1
NF = NF + 1

end
Method 4
begin

ARC(1) = EDGE
IF (RFACE(EDGE) .EQ. FACE) THEN
ARC(2) = FREDGE(EDGE)
ARC(3) = BREDGE(EDGE)
ELSE
ARC(2) = BLEDGE(EDGE)
ARC(3) = FLEDGE(EDGE)
ENDIF
DO 10 I = 1,3
ROT(I) = MOD(I,3) + 1
IF (RFACE(ARC(I)) .EQ. FACE) THEN
TEMP(1,I) = FNODE(ARC(I))
TEMP(2,I) = LFACE(ARC(I))
TEMP(3,I) = FLEDGE(ARC(I))
TEMP(4,I) = BLEDGE(ARC(I))
ELSE
TEMP(1,I) = BNODE(ARC(I))
TEMP(2,I) = RFACE(ARC(I))
TEMP(3,I) = BREDGE(ARC(I))
TEMP(4,I) = FREDGE(ARC(I))
ENDIF
TEMP(5,I) = LABEL(ARC(I))
DO 20 I = 1,3
BNODE(ARC(I)) = NEWNOD
FNODE(ARC(I)) = TEMP(1,I)
LFACE(ARC(I)) = TEMP(2,I)
RFACE(ARC(I)) = TEMP(2,ROT(I))
FLEDGE(ARC(I)) = TEMP(3,I)
FREDGE(ARC(I)) = TEMP(4,ROT(I))
BREDGE(ARC(I)) = ARC(ROT(I))
BLEDGE(ARC(I)) = ARC(ROT(ROT(I)))
LABEL(ARC(I)) = MIN(TEMP(5,I),TEMP(5,ROT(I)))
20 CONTINUE
DNODE(NEWNOD) = 3
DO 25 I = 1,3
NUM = FREDGE(ARC(I))
IF(FNODE(NUM) .EQ. TEMP(1,I)) THEN
FLEDGE(NUM) = ARC(I)
ELSE
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BREDGE(NUM) = ARC(I)
ENDIF
25 CONTINUE
DO 30 I = 1,3
  NUM = RFACE(ARC(I))
  DFACE(NUM) = DFACE(NUM) + 1
30 CONTINUE
DO 40 I = 1,3
  NUM = FNODE(ARC(I))
  DNODE(NUM) = DNODE(NUM) - 1
40 CONTINUE
DO 110 J = 1,10
  DA = POS(ARC(1),J)
  DB = POS(ARC(2),J)
  DC = POS(ARC(3),J)
  POS(ARC(1),J) = WC
  POS(ARC(2),J) = WA
  POS(ARC(3),J) = WB
  ERRPOS(J) = ERRPOS(J) + DABS(WA*WB*WC-DA*DB-DA*DC-DB*DC+2*DA*DB*DC)
  DA = NEG(ARC(1),J)
  DB = NEG(ARC(2),J)
  DC = NEG(ARC(3),J)
  NEG(ARC(1),J) = WC
  NEG(ARC(2),J) = WA
  NEG(ARC(3),J) = WB
  ERRNEG(J) = ERRNEG(J) + DABS(WA*WB*WC-DA*DB-DA*DC-DB*DC+2*DA*DB*DC)
  DA = POINT(ARC(1),J)
  DB = POINT(ARC(2),J)
  DC = POINT(ARC(3),J)
  POINT(ARC(1),J) = WC
  POINT(ARC(2),J) = WA
  POINT(ARC(3),J) = WB
110 CONTINUE
DFACE(FACE) = 0
NF = NF - 1
NN = NN + 1
end
Method 5

begin

IF (RFACE(EDGE1) .EQ. FACE) THEN
  EDGE2 = FREDGE(EDGE1)
  IF (RFACE(EDGE2) .EQ. FACE) THEN
    FREDGE(EDGE1) = BLEDGE(EDGE2)
    BREDGE(EDGE1) = FLEDGE(EDGE2)
    RFACE(EDGE1) = LFACE(EDGE2)
  ELSE
    FREDGE(EDGE1) = FREDGE(EDGE2)
    BREDGE(EDGE1) = BREDGE(EDGE2)
    RFACE(EDGE1) = RFACE(EDGE2)
  ENDIF
  NUM = FREDGE(EDGE1)
  IF(BREDGE(NUM).EQ. EDGE2) THEN
    BREDGE(NUM) = EDGE1
  ELSE
    FLEDGE(NUM) = EDGE1
  ENDIF
  NUM = BREDGE(EDGE1)
  IF(FLEDGE(NUM).EQ. EDGE2) THEN
    FREDGE(NUM) = EDGE1
  ELSE
    BLEDGE(NUM) = EDGE1
  ENDIF
ELSE
  EDGE2 = FLEDGE(EDGE1)
  IF (RFACE(EDGE2) .EQ. FACE) THEN
    FLEDGE(EDGE1) = FLEDGE(EDGE2)
    BLEDGE(EDGE1) = BLEDGE(EDGE2)
    LFACE(EDGE1) = LFACE(EDGE2)
  ELSE
    FLEDGE(EDGE1) = BREDGE(EDGE2)
    BLEDGE(EDGE1) = FREDGE(EDGE2)
    LFACE(EDGE1) = RFACE(EDGE2)
  ENDIF
  NUM = FLEDGE(EDGE1)
  IF(BLEDGE(NUM).EQ. EDGE2) THEN
    BLEDGE(NUM) = EDGE1
  ELSE
    FREDGE(NUM) = EDGE1
  ENDIF
NUM = BLEDGE(EDGE1)
IF (FLEDGE(NUM) .EQ. EDGE2) THEN
    FLEDGE(NUM) = EDGE1
ELSE
    BREDGE(NUM) = EDGE1
ENDIF
ENDIF
LABEL(EDGE1) = MIN(LABEL(EDGE1), LABEL(EDGE2))
LABEL(EDGE2) = 0
NUM = FNODE(EDGE1)
DNODE(NUM) = DNODE(NUM)-1
1000 IF (RFACE(EDGE2) .EQ. FACE) THEN
    IF (INCDNT(LFACE(EDGE2)) .GT. 0)
        INCDNT(LFACE(EDGE2)) = EDGE1
    ELSE
        IF (INCDNT(RFACE(EDGE2)) .GT. 0)
            INCDNT(RFACE(EDGE2)) = EDGE1
    ENDIF
ENDIF
DFACE(FACE) = 0
DO 110 J = 1, 10
    POS(EDGE1, J) =
        POS(EDGE1, J) + POS(EDGE2, J) - POS(EDGE1, J) * POS(EDGE2, J)
    POINT(EDGE1, J) = POINT(EDGE1, J) + POINT(EDGE2, J) -
        POINT(EDGE1, J) * POINT(EDGE2, J)
    NEG(EDGE1, J) =
        NEG(EDGE1, J) + NEG(EDGE2, J) - NEG(EDGE1, J) * NEG(EDGE2, J)
110 CONTINUE
NF = NF-1
NA = NA-1
end

Method6
begin
    IF (FNODE(EDGE1) .EQ. NODE) THEN
        EDGE2 = FLEDGE(EDGE1)
    IF (FNODE(EDGE2) .EQ. NODE) THEN
        FLEDGE(EDGE1) = BREDGE(EDGE2)
        FREDGE(EDGE1) = BLEEDGE(EDGE2)
        FNODE(EDGE1) = BNODE(EDGE2)
    ELSE
        FLEDGE(EDGE1) = FLEDGE(EDGE2)
        FREDGE(EDGE1) = FREDGE(EDGE2)
    ENDIF
FNODE(EDGE1) = FNODE(EDGE2)
ENDIF
NUM = FLEDGE(EDGE1)
IF (FREDGE(NUM) .EQ. EDGE2) THEN
  FREDGE(NUM) = EDGE1
ELSE
  BLEDGE(NUM) = EDGE1
ENDIF
NUM = FREDGE(EDGE1)
IF (FLEDGE(NUM) .EQ. EDGE2) THEN
  FLEDGE(NUM) = EDGE1
ELSE
  BREDGE(NUM) = EDGE1
ENDIF
ELSE
  EDGE2 = BLEDGE(EDGE1)
  IF (FNODE(EDGE2) .EQ. NODE) THEN
    BREDGE(EDGE1) = BREDGE(EDGE2)
    BLEDGE(EDGE1) = BLEDGE(EDGE2)
    BNODE(EDGE1) = BNODE(EDGE2)
  ELSE
    BREDGE(EDGE1) = FLEDGE(EDGE2)
    BLEDGE(EDGE1) = FREDGE(EDGE2)
    BNODE(EDGE1) = FNODE(EDGE2)
  ENDIF
  NUM = BREDGE(EDGE1)
  IF (BLEDGE(NUM) .EQ. EDGE2) THEN
    BLEDGE(NUM) = EDGE1
  ELSE
    FREDGE(NUM) = EDGE1
  ENDIF
  NUM = BLEDGE(EDGE1)
  IF (BREDGE(NUM) .EQ. EDGE2) THEN
    BREDGE(NUM) = EDGE1
  ELSE
    FLEDGE(NUM) = EDGE1
  ENDIF
ENDIF
LABEL(EDGE1) = MIN(LABEL(EDGE1), LABEL(EDGE2))
LABEL(EDGE2) = 0
NUM = RFACE(EDGE1)
DFACE(NUM) = DFACE(NUM)-1
1000 IF (BNODE(EDGE2) .EQ. NODE) THEN
IF(INCDNT(FNODE(EDGE2)) .GT. 0)
INCDNT(FNODE(EDGE2)) = EDGE1
ELSE
IF(INCDNT(BNODE(EDGE2)) .GT. 0)
INCDNT(BNODE(EDGE2)) = EDGE1
ENDIF
ENDIF
DNODE(NODE) = 0
DO 110 J = 1,10
   POS(EDGE1,J) = POS(EDGE1,J)*POS(EDGE2,J)
   NEG(EDGE1,J) = NEG(EDGE1,J)*NEG(EDGE2,J)
   POINT(EDGE1,J) = POINT(EDGE1,J)*POINT(EDGE2,J)
110 CONTINUE
NN=NN-1
NA=NA-1
end

Method7
begin
  READ(4,*)  NN, NA, NF
  DO 15 J = 1, NA
     READ(4,*)  I,BNODE(I),FNODE(I),LFACE(I),RFACE(I)
     READ(4,*)  BREDGE(I),BLEDGE(I),FLEDGE(I),FREDGE(I)
     ARCNUM(J) =  I
  15 CONTINUE
  DO 16 J = 1,NN
     READ(4,*)  I, DNODE(I)
     NODNUM(J) =  I
  16 CONTINUE
  DO 17 K = 1,NF
     READ(4,*)  I, DFACE(I)
     FACNUM(K) =  I
  17 CONTINUE
  READ(*,*)  PNUM
  DO 110 J = 1,10
     DO 47 I = 1,NA
        POS(I,J) = PNUM + J*0.02
        NEG(I,J) = PNUM + J*0.02
        POINT(I,J) = PNUM + J*0.02
     47 CONTINUE
  110 CONTINUE
  LABEL(START) = 1
EBOT = START
OCURR = START
1111 IF (BNODE(OCURR) .EQ. SORE) THEN
    SFACE(OCURR) = RFACE(OCURR)
    OCURR = BREDGE(OCURR)
ELSE
    SFACE(OCURR) = LFACE(OCURR)
    OCURR = FLEDGE(OCURR)
ENDIF
IF (OCURR .NE. START) THEN
    LABEL(OCURR) = 1
    NCOUNT = NCOUNT + 1
    NEXT(EBOT) = OCURR
    EBOT = OCURR
    NEXT(EBOT) = 0
    GOTO 1111
ENDIF
137 ESCAN = ETOP
    CFACE = SFACE(ESCAN)
    WRITE(*,*) 'SCANNING EDGE #', ESCAN
    ECURR = ESCAN
122 IF (CFACE .EQ. RFACE(ECURR)) THEN
    NUM = FNODE(ECURR)
    ECURR = FREDGE(ECURR)
ELSE
    NUM = BNODE(ECURR)
    ECURR = BLEDGE(ECURR)
ENDIF
IF (LABEL(ECURR) .EQ. 0) THEN
    LABEL(ECURR) = LABEL(ESCAN) + 1
    NCOUNT = NCOUNT + 1
    WRITE(*,*) 'labelling edge #', ECURR, 'by label', LABEL(ECURR)
    IF (NCOUNT .EQ. NA) GOTO 1333
    SNODE(ECURR) = NUM
    IF (OTOP .EQ. 0 ) THEN
        OTOP = ECURR
    ELSE
        NEXT(OBOT) = ECURR
    ENDIF
    OBOT = ECURR
    NEXT(OBOT) = 0
ENDIF
IF (LABEL(ECURR) .EQ. LABEL(ESCAN)) THEN
ETOP = NEXT(ETOP)
IF (ETOP .EQ. 0) THEN
  IF(OTOP .EQ. 0) THEN
    GOTO 1333
  ELSE
    GOTO 237
  ENDIF
ENDIF
GOTO 137
ENDIF
GOTO 122
237  OSCAN = OTOP
     CNODE = SNODE(OSCAN)
     OCURR = OSCAN
222  IF (CNODE .EQ. BNODE(OCURR)) THEN
     NUM = LFACE(OCURR)
     OCURR = BLEDGE(OCURR)
   ELSE
     NUM = RFACE(OCURR)
     OCURR = FREDGE(OCURR)
   ENDIF
IF (LABEL(OCURR) .EQ. 0) THEN
  NCOUNT = NCOUNT + 1
  LABEL(OCURR) = LABEL(OSCAN) + 1
  WRITE(*,*) 'labelling edge #', OCURR, 'by label', LABEL(OCURR)
  IF (NCOUNT .EQ. NA) GOTO 1333
  SFACE(OCURR) = NUM
  IF (ETOP .EQ. 0 ) THEN
    ETOP = OCURR
  ELSE
    NEXT(EBOT) = OCURR
  ENDIF
ENDIF
EBOT = OCURR
NEXT(EBOT) = 0
ENDIF
IF (LABEL(OCURR) .EQ. LABEL(OSCAN)) THEN
  OTOP = NEXT(OTOP)
  NEXT(OSCAN) = 0
  IF (OTOP .EQ. 0) THEN
    IF(ETOP .EQ. 0) THEN
      GOTO 1333
    ELSE
      GOTO 137
    ENDIF
  ENDIF
ENDIF
ENDIF
GOTO 237
ENDIF
GOTO 222

Method8
begin

INCDNT(NUM) = 0
ABOVE(BELOW(NUM)) = ABOVE(NUM)
BELOW(ABOVE(NUM)) = BELOW(NUM)
ABOVE(NUM) = 0
BELOW(NUM) = 0

end

Method9
begin

IF (FLAG .EQ. 1) THEN
FACE = NUM
IF(DFACE(FACE) .EQ. 1) THEN
IF(TOPLOOP .GT. 0) THEN
   ABOVE(TOPLOOP)=FACE
   BELOW(FACE) =TOPLOOP
ENDIF
TOPLOOP = FACE
INCDNT(FACE) = ARC
GOTO 1000
ENDIF
IF(DFACE(FACE) .EQ. 2) THEN
IF(TOPPAR .GT. 0) THEN
   ABOVE(TOPPAR)=FACE
   BELOW(FACE) =TOPPAR
ENDIF
TOPPAR = FACE
INCDNT(FACE) = ARC
GOTO 1000
ENDIF
EDGE1= ARC
IF (RFACE(EDGE1) .EQ. FACE) THEN
EDGE2 = FREDGE(EDGE1)
EDGE3 = BREDGE(EDGE1)
ELSE
EDGE2 = BLEDGE(EDGE1)
EDGE3 = FLEDGE(EDGE1)
ENDIF

NCHECK = MIN(LABEL(EDGE1), LABEL(EDGE2), LABEL(EDGE3))
NSUM = LABEL(EDGE1) + LABEL(EDGE2) + LABEL(EDGE3)
IF (NSUM .EQ. (3*NCHECK+2)) THEN
  INCDNT(FACE) = EDGE1
  IF (TOPDEL .GT. 0) THEN
    ABOVE(TOPDEL) = FACE
    BELOW(FACE) = TOPDEL
  ENDIF
  TOPDEL = FACE
ENDIF
GOTO 1000
ENDIF

NODE = NUM
IF (NODE .EQ. SORE) GOTO 1000
IF (NODE .EQ. TERM1) GOTO 1000
IF (NODE .EQ. TERM2) GOTO 1000
IF (NODE .EQ. TERM3) GOTO 1000
IF (NODE .EQ. TERM4) GOTO 1000
IF (DNODE(NODE) .EQ. 0) GOTO 1000
IF (DNODE(NODE) .EQ. 1) THEN
  IF (TOPVERT .GT. 0) THEN
    ABOVE(TOPVERT) = NODE
    BELOW(NODE) = TOPVERT
  ENDIF
  TOPVERT = NODE
  INCDNT(NODE) = ARC
  GOTO 1000
ENDIF

IF (DNODE(NODE) .EQ. 2) THEN
  IF (TOPSER .GT. 0) THEN
    ABOVE(TOPSER) = NODE
    BELOW(NODE) = TOPSER
  ENDIF
  TOPSER = NODE
  INCDNT(NODE) = ARC
  GOTO 1000
ENDIF

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EDGE1 = ARC
IF (BNODE(EDGE1) .EQ. NODE) THEN
  EDGE2 = BREDGE(EDGE1)
  EDGE3 = BLEEDGE(EDGE1)
ELSE
  EDGE2 = FLEDGE(EDGE1)
  EDGE3 = FREDGE(EDGE1)
ENDIF
NCHECK = MIN(LABEL(EDGE1), LABEL(EDGE2), LABEL(EDGE3))
NSUM = LABEL(EDGE1) + LABEL(EDGE2) + LABEL(EDGE3)
IF (NSUM .EQ. (3*NCHECK+2)) THEN
  INCDNT(NODE) = EDGE1
  IF (TOPWYE .GT. 0) THEN
    ABOVE(TOPWYE) = NODE
    BELOW(NODE) = TOPWYE
  ENDIF
  TOPWYE = NODE
ENDIF
end

SubDerivation {vertex, loop, wye, delta, parallel, series, remove, positive, main}

Object18 is
Attributes
topdel, topser, toppar, topvert, toploop : integer
Methods
Method1
begin
  IF (TOPPAR .EQ. NUM) TOPPAR = BELOW(NUM)
  IF (TOPDEL .EQ. NUM) TOPDEL = BELOW(NUM)
  IF (TOPLOOP .EQ. NUM) TOPLOOP = BELOW(NUM)
  IF (TOPSER .EQ. NUM) TOPSER = BELOW(NUM)
  IF (TOPWYE .EQ. NUM) TOPWYE = BELOW(NUM)
  IF (TOPVERT .EQ. NUM) TOPVERT = BELOW(NUM)
end

Method2
begin
IF (FLAG .EQ. 1) THEN
FACE = NUM
IF (DFACE(FACE) .EQ. 1) THEN
TOPLOOP = FACE
GOTO 1000
ENDIF
IF(DFACE(FACE) .EQ. 2) THEN
TOPPAR = FACE
GOTO 1000
ENDIF
ENDIF
ENDIF
IF (NSUM .EQ. (3*NCHECK+2)) THEN
TOPDEL = FACE
GOTO 1000
ENDIF
TOPVERT = NODE
GOTO 1000
ENDIF
IF(DNODE(NODE) .EQ. 2) THEN
TOPSER = NODE
GOTO 1000
ENDIF
IF (NSUM .EQ. (3*NCHECK+2)) THEN
TOPWYE = NODE
ENDIF
1000 RETURN
end

SubDerivation {remove, positive}

Object19 is
Attributes
stprob, upprob, loprob : real

Methods
Method 1
begin
IF (SINK1 .EQ. NODE) THEN
DO 10 J = 1,10
UPPROB(J) = POS(EDGE,J)* UPPROB(J)
10 RETURN
end
LOPROB(J) = NEG(EDGE,J) * LOPROB(J)
STPROB(J) = POINT(EDGE,J) * STPROB(J)

10 CONTINUE
ENDIF
end

Method2
begin
   DO 110 J = 1,10
   LOPROB(J) = 1.0
   UPPROB(J) = 1.0
   STPROB(J) = 1.0
110 CONTINUE
end

Method3
begin
   DO 110 J = 1,10
   LOPROB(J) = LOPROB(J) * POS(ARC,J)
   UPPROB(J) = UPPROB(J) * NEG(ARC,J)
   STPROB(J) = STPROB(J) * POINT(ARC,J)
   WRITE(8,174) OPERPROB, LOPROB(J), STPROB(J), UPPROB(J)
174 FORMAT
110 CONTINUE
end

SubDerivation {vertex, main, reduce}

Object20 is
Attributes
term1, term2, term3, term4 : integer

Methods
Method1
begin
   READ(4,*) NTERM, TERM1, TERM2,TERM3,TERM4
end
Method2
begin

NODE = NUM
IF(NODE .EQ. SORE) GOTO 1000
IF(NODE .EQ. TERM1) GOTO 1000
IF(NODE .EQ. TERM2) GOTO 1000
IF(NODE .EQ. TERM3) GOTO 1000
IF(NODE .EQ. TERM4 ) GOTO 1000

1000 RETURN
end

SubDerivation { main, positive}

Object21 is
Attributes
above, below : integer

Methods

Method1
begin

IF(DFACE(FACE) .EQ. 1) THEN
  IF(TOPLOOP .GT. 0) THEN
    ABOVE(TOPLOOP)= FACE
    BELOW(FACE) =TOPLOOP
  ENDFID
ENDIF

IF(DFACE(FACE) .EQ. 2) THEN
  IF(TOPPAR .GT. 0) THEN
    ABOVE(TOPPAR)= FACE
    BELOW(FACE) =TOPPAR
  ENDFID
ENDIF

IF (NSUM .EQ. (3*NCHECK+2)) THEN
  IF (TOPDEL .GT. 0) THEN
    ABOVE(TOPDEL)=FACE
    BELOW(FACE) =TOPDEL
  ENDFID
ENDIF

NODE = NUM
IF(DNODE(NODE) .EQ. 1) THEN
  IF(TOPVERT .GT. 0) THEN
    ABOVE(TOPVERT)=NODE
  ENDFID
BELOW(NODE) = TOPVERT
ENDIF
ENDIF
IF(DNODE(NODE) .EQ. 2) THEN
  IF(TOPSER .GT. 0) THEN
    ABOVE(TOPSER) = NODE
    BELOW(NODE) = TOPSER
  ENDIF
ENDIF
IF(NSUM .EQ. (3*NCHECK+2)) THEN
  IF(TOPWYE .GT. 0) THEN
    ABOVE(TOPWYE) = NODE
    BELOW(NODE) = TOPWYE
  ENDIF
end

SubDerivation {positive}

Object22 is
  Attributes
    sink2 : integer
  Methods
    SubDerivation {}

Object23 is
  Attributes
    oface : integer
  Methods
    SubDerivation {}

Object24 is
  Attributes
    facnum : integer
  Methods
Method 1
begin
    DO 17 K = 1,NF
        READ(4,*) I, DFACE(I)
        FACNUM(K) = I
    17 CONTINUE
end

SubDerivation {main}

Object25 is
Attributes
    nodnum : integer

Methods
Method 1
begin
    DO 16 J = 1,NN
        READ(4,*) I, DNODE(I)
        NODNUM(J) = I
    16 CONTINUE
end

SubDerivation {main}

Object26 is
Attributes
    nterm : integer

Methods
Method 1
begin
    READ(4,*) NTERM, TERM1, TERM2, TERM3, TERM4
end

SubDerivation {main}

Object27 is
Attributes
    sore : integer
Methods

Method 1
begin
READ(4,*) SORE, SINK1, START
PRINT *, 'SOURCE: ', SORE, ' SINK1: ', SINK1
end

SubDerivation {main}

Object 28 is
Attributes
sink1 : integer

Methods

Method 1
begin
IF BNODE(EDGE) .EQ. NODE) THEN
NODE1 = FNODE(EDGE)
ELSE
NODE1 = BNODE(EDGE)
ENDIF
IF (SINK1 .EQ. NODE) THEN
SINK1 = NODE1
WRITE(*, 11) SINK1
11 FORMAT('THE NEW SINK1 NODE IS', 14)
ENDIF
end

Method 2
begin
READ(4,*) SORE, SINK1, START
PRINT *, 'SOURCE: ', SORE, ' SINK1: ', SINK1
end
Method3
begin
    NODE = NUM
    IF (NODE..EQ. SINK1) GOTO 1000
    1000 RETURN
end

SubDerivation {vertex, main, positive}
Vita

Bonnie L. Achee received the bachelor of science degree in Computer Science from Southeastern Louisiana University in 1990, where she graduated magna cum laude. She was a Board of Regents Fellow at Louisiana State University during her graduate studies. She received the degree of Doctor of Philosophy in Computer Science in May 1998. She is a member of the Association for Computing Machinery and the IEEE Computer Society. She is currently employed as an Assistant Professor in the Department of Computer Science at Southeastern Louisiana University.
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