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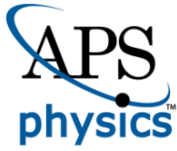
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Antiferromagnetic Order in Pauli Limited Unconventional Superconductors

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We develop a theory of the coexistence of superconductivity (SC) and antiferromagnetism (AFM) in CeCoIn₅. We show that in Pauli-limited nodal superconductors the nesting of the quasi-particle pockets induced by Zeeman pair-breaking leads to incommensurate AFM with the moment normal to the field. We compute the phase diagram and find a first order transition to the normal state at low temperatures, absence of normal state AFM, and coexistence of SC and AFM at high fields, in agreement with experiments. We also predict the existence of a new double- \mathbf{Q} magnetic phase.

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The interplay between antiferromagnetism and unconventional superconductivity is one of the most intensely investigated topics in correlated electron systems. The 115 family of heavy fermion compounds (CeMIn₅ where M=Co,Rh, Ir) exhibits many salient features of this interplay. CeCoIn₅ is a clean layered singlet d -wave superconductor whose upper critical field, H_{c2} , is determined by the Zeeman splitting of the electronic states (Pauli limiting), rather than by the orbital motion of the Cooper pairs. This material has an unusual low-temperature, T , phase at fields just below H_{c2} , separated by a second order transition line from the low field superconductor, and by a first order transition from the normal (N) state ($H \geq H_{c2}$) [1]. Initially this phase was conjectured [1] to be the first realization of the Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) state, where Cooper pairs acquire a finite center of mass momentum to counteract the pair-breaking due to Pauli limiting, and the superconducting order parameter oscillates in real space.

However, experiments present a more complex situation. The high-field N-SC transition becomes first order at higher T than that of the onset of the new phase [1]. Specific heat and resistivity are anomalous just above H_{c2} , consistent with quantum critical behavior due to antiferromagnetic fluctuations [2, 3], yet AFM was not found upon suppression of SC by several means [2, 4–6]. Finally, a series of NMR and neutron scattering measurements with \mathbf{H} parallel to the layers established the existence of static AFM in the high-field phase [7–12]. The ordered moment $\mathbf{m} \perp \mathbf{H}$ is modulated with an essentially field-independent wave-vector $\mathbf{Q}/(2\pi) = (q, q, 0.5)$, ($q \simeq 0.44$). [9, 11]. This unusual phase challenges our understanding of the connection between SC and AFM.

In this Letter we show that the near-perfect nesting of the quasiparticle pockets created by Zeeman pair-breaking near the nodal regions creates the conditions for the antiferromagnetic instability even when the normal state Fermi surface is not nested. This AFM instability is equivalent to equal spin pairing of Bogoliubov quasiparticles within each pocket. We compute the transition temperature both analytically in the weak-coupling limit (WCL) and numerically for a two-dimensional (2D)

model. The resulting coexistence of AFM and SC appears in the low-temperature and high-field region of the phase diagram, while magnetic order does not appear in the normal state. Moreover, the N-SC transition becomes first order at a temperature above that where the magnetic order first appears. These results are in agreement with the experimental observations on CeCoIn₅. The most favorable magnetic state in the WCL is a double- \mathbf{Q} collinear structure at the incommensurate wave-vectors connecting opposite nodes, with $\mathbf{m} \perp \mathbf{H}$, but a single- \mathbf{Q} state may be stabilized in a part of the phase diagram.

Previous theories focused on the field induced AFM and considered single- \mathbf{Q} state only. In some proposals the amplitude modulation of the superconducting order parameter, $\Delta(\mathbf{r})$, is essential and drives a spin density wave (SDW) order that varies on the same length scale [13, 14]. In other theories the SDW instability is not conditional on the oscillatory behavior of $\Delta(\mathbf{r})$ [15–17]. In Refs. [15, 16] the direction of the SDW magnetization was taken parallel to \mathbf{H} , and the phase diagram was obtained numerically for fixed (large) values of interactions in different channels. We find that the longitudinal antiferromagnetic susceptibility is gapped under Zeeman field, but the transverse susceptibility is divergent. Hence AFM with $\mathbf{m} \perp \mathbf{H}$ appears naturally. Landau expansion of the free energy in a model with critical magnetic fluctuations also supports $\mathbf{m} \perp \mathbf{H}$ for nodal superconductors [17]. It was recently suggested [18] that an enhancement of the density of states above the normal state value due to combined effect of vortices and strong Pauli paramagnetism leads to the SDW instability, with no FFLO-like modulation of $\Delta(\mathbf{r})$. In our theory it is the nesting between pockets, and therefore the joint density of states enhancement, that drives the magnetic transition. Finally, we propose the existence of a double- \mathbf{Q} spin structure that differs from previous theories and provides a test of our results.

Since the main Fermi surface sheet of CeCoIn₅ is quasi-cylindrical, we consider a 2D Hamiltonian for a $d_{x^2-y^2}$

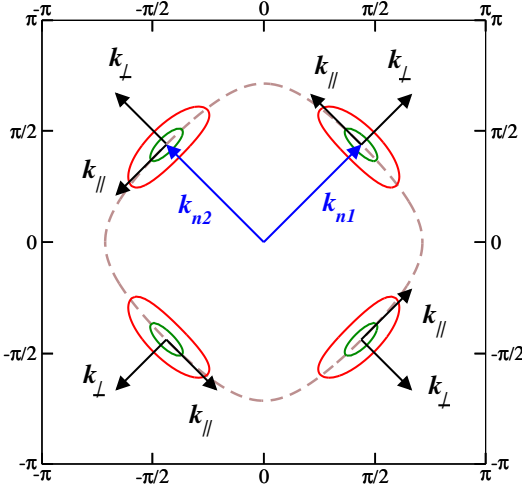


FIG. 1: (Color online) Fermi surface and the nodal pockets generated by Zeeman field for the tight-binding model described in the text with $\Delta_0/t = 0.7$, $h/t = 0.3, 0.7$. $k_{||}$ and k_{\perp} correspond to the directions parallel and perpendicular to the Fermi surface near each pocket.

superconductor with a Zeeman term $h = g\mu_B H$,

$$\mathcal{H}_0 = \sum_{k\sigma} (\varepsilon_k - h\sigma) c_{k\sigma}^\dagger c_{k\sigma} - \sum_{\mathbf{k}} \left(\Delta_{\mathbf{k}} c_{\mathbf{k}\uparrow}^\dagger c_{-\mathbf{k}\downarrow}^\dagger + \text{H.c.} \right).$$

Here $\varepsilon_{\mathbf{k}}$ is the band dispersion and $\Delta_{\mathbf{k}}$ is the $d_{x^2-y^2}$ order parameter. We select the spin quantization axis along \mathbf{H} . A Bogoliubov transformation $\gamma_{\mathbf{k}\uparrow} = u_{\mathbf{k}} c_{\mathbf{k}\uparrow} - v_{\mathbf{k}}^* c_{-\mathbf{k}\downarrow}^\dagger$, $\gamma_{\mathbf{k}\downarrow} = u_{\mathbf{k}} c_{\mathbf{k}\downarrow} + v_{\mathbf{k}}^* c_{-\mathbf{k}\uparrow}^\dagger$ with $2|u_{\mathbf{k}}|^2 = [1 + \varepsilon_{\mathbf{k}}/E_{\mathbf{k}}]$, $2|v_{\mathbf{k}}|^2 = [1 - \varepsilon_{\mathbf{k}}/E_{\mathbf{k}}]$, and $E_{\mathbf{k}} = \sqrt{\varepsilon_{\mathbf{k}}^2 + \Delta_{\mathbf{k}}^2}$ brings the Hamiltonian to the diagonal form

$$\tilde{\mathcal{H}}_0 = \sum_{\mathbf{k}} \left\{ [E_{\mathbf{k}} - h] \gamma_{\mathbf{k}\uparrow}^\dagger \gamma_{\mathbf{k}\uparrow} + [E_{\mathbf{k}} + h] \gamma_{-\mathbf{k}\downarrow}^\dagger \gamma_{-\mathbf{k}\downarrow} \right\}. \quad (1)$$

The first term describes the creation of spin-polarized pockets of Bogoliubov quasiparticles by magnetic field. These pockets are unstable to the formation of AFM, and we first elucidate this instability in the WCL.

At low fields we linearize the dispersion in the near-nodal regions by taking $\varepsilon_{\mathbf{k}} \approx v_F k_{\perp}$ and $\Delta_{\mathbf{k}} \approx v_{\Delta} k_{||}$ with k_{\perp} ($k_{||}$) measured from the node normal (parallel) to the Fermi surface (see Fig. 1) and obtain elliptical Fermi pockets $\sqrt{v_F^2 k_{\perp}^2 + v_{\Delta}^2 k_{||}^2} = h$. For a centrosymmetric system with pairs of nodes at momenta $\pm \mathbf{k}_{ni}$, the low field pockets are perfectly nested at $\mathbf{Q}_i = 2\mathbf{k}_{ni}$ and $\bar{\mathbf{Q}}_i = -2\mathbf{k}_{ni}$ ($i = 1, 2$, see Fig.1), even though the Fermi surface in the normal state is not. This nesting drives the instabilities of the superconducting state.

As 115 materials exhibit strong antiferromagnetic fluctuations, we assume that there is a residual interaction in this channel. We start by considering the simplest AFM with $\mathbf{m} \perp \mathbf{H}$: a single- \mathbf{Q} spiral $\mathbf{m}(\mathbf{r}) = m_{\mathbf{Q}}(\cos \mathbf{Q} \cdot \mathbf{r}, \sin \mathbf{Q} \cdot \mathbf{r}, 0)$, where $\mathbf{Q} \in \pm \mathbf{Q}_i$ is one of

the four wave-vectors that are perfectly nested. The mean field Hamiltonian for this spiral order is

$$\mathcal{H}_{AFM} = -J \sum_{\mathbf{k}} \left[m_{\mathbf{Q}} c_{\mathbf{k}\downarrow}^\dagger c_{\mathbf{k}+\mathbf{Q}\uparrow} + m_{\bar{\mathbf{Q}}}^* c_{\mathbf{k}+\mathbf{Q}\uparrow}^\dagger c_{\mathbf{k}\downarrow} \right], \quad (2)$$

where $m_{\mathbf{Q}} = \sum_{\mathbf{k}} \langle c_{\mathbf{k}\downarrow}^\dagger c_{\mathbf{k}+\mathbf{Q}\uparrow} \rangle / N$, J is the coupling constant, $\langle \dots \rangle$ denotes a thermodynamic average, and N is the number of lattices sites.

Since a Bogoliubov quasiparticle with a given spin at momentum \mathbf{k} combines an electron state with the same spin at \mathbf{k} with a hole with opposite spin at $-\mathbf{k}$, the AFM interaction in the particle-hole channel is manifested as a spin triplet superconducting instability of the Bogoliubov quasiparticles within each pocket. Transforming Eq. (2) into the basis of Bogoliubov states we find

$$c_{\mathbf{k}+\mathbf{Q}\uparrow}^\dagger c_{\mathbf{k}\downarrow} = -u_{\mathbf{k}+\mathbf{Q}} v_{\mathbf{k}}^* \gamma_{\mathbf{k}+\mathbf{Q}\uparrow}^\dagger \gamma_{-\mathbf{k}\uparrow}^\dagger + \text{irr.}$$

Note that we only need to consider the quasiparticles with the spin along the field (occupied states). The terms marked as irrelevant (irr.) involve creation operators with opposite spin, and therefore do not have an expectation value since these excitations are gapped by h . Consider the vicinity of the node $-\mathbf{Q}/2$. We have $\mathbf{k} = -\mathbf{Q}/2 + \mathbf{q}$, so that $\mathbf{k} + \mathbf{Q} = \mathbf{Q}/2 + \mathbf{q}$, and we find

$$c_{\mathbf{k}+\mathbf{Q}\uparrow}^\dagger c_{\mathbf{k}\downarrow} = -u_{\frac{\mathbf{Q}}{2}+\mathbf{q}} v_{-\frac{\mathbf{Q}}{2}+\mathbf{q}}^* \gamma_{\frac{\mathbf{Q}}{2}+\mathbf{q}\uparrow}^\dagger \gamma_{\frac{\mathbf{Q}}{2}-\mathbf{q}\uparrow}^\dagger + \text{irr.},$$

which describes the triplet pairing of ‘‘Bogoliubons’’ within the same pocket. Since $u_{\mathbf{k}+\mathbf{Q}} v_{\mathbf{k}}^* \approx \text{sgn}(k_{||})$ in the linearized approximation for a d -wave gap, we obtain

$$\mathcal{H} = \sum_{\mathbf{q}} \left[\left(E_{-\frac{\mathbf{Q}}{2}+\mathbf{q}} - h \right) \gamma_{-\frac{\mathbf{Q}}{2}+\mathbf{q}\uparrow}^\dagger \gamma_{-\frac{\mathbf{Q}}{2}+\mathbf{q}\uparrow} + J m_{\mathbf{Q}}^* \gamma_{\frac{\mathbf{Q}}{2}+\mathbf{q}\uparrow}^\dagger \gamma_{\frac{\mathbf{Q}}{2}-\mathbf{q}\uparrow}^\dagger \text{sgn}(q_{||}) + \text{H.c.} \right], \quad (3)$$

showing p -wave pairing symmetry. The sum in Eq.(3) runs over wave-vectors \mathbf{q} near the pocket center, i.e. $|\mathbf{q}| \ll \pi/a$. This approximation is valid as long as \mathbf{Q} is far from the commensurate wave vector (π, π) . In that case, only the wave-vectors on the Fermi surface of the pocket centered at $-\mathbf{Q}/2$ satisfy the nesting condition for the transferred momentum \mathbf{Q} (see Fig.2).

The critical temperature in the WCL is

$$T_{\mathbf{Q}} \approx \sqrt{\omega_c h} \exp \left[-\frac{2\pi^2 v_F v_{\Delta}}{J h} \right], \quad (4)$$

where ω_c is the high energy cutoff for the magnetic interaction J . This result is valid for $T_c \ll h \ll \{\omega_c, \Delta_0\}$, and describes the instability of the uniform SC towards the AFM modulation. It is likely that the exponentially small \mathbf{m} at low H is destroyed by the orbital effect (see below). The order parameter that appears at $T_{\mathbf{Q}}$, $\sum_{\mathbf{q}} \text{sgn}(q_{||}) \langle \gamma_{\frac{\mathbf{Q}}{2}+\mathbf{q}\uparrow}^\dagger \gamma_{\frac{\mathbf{Q}}{2}-\mathbf{q}\uparrow}^\dagger \rangle$, has

a staggered triplet superconducting component, $\Delta_Q^t = \sum_q \delta_q^t \langle c_{-Q/2+q\uparrow}^\dagger c_{-Q/2-q\uparrow}^\dagger \rangle$ with $\text{sgn}(\delta_q^t) = \text{sgn}(q_{\parallel})$, in addition to the AFM m_Q [15, 16]. This triplet component is an inevitable companion of Δ_0 and m_Q since the Ginzburg-Landau expansion allows for the invariants of the form $\Delta_Q \cdot m_Q \Delta_0^* - \Delta_Q^* \cdot m_Q \Delta_0$, linear in Δ_Q , where Δ_Q is the vector of three independent components of the triplet superconducting order parameter ($2\Delta_Q^t = \Delta_Q^x + i\Delta_Q^y$). However, we expect Δ_Q^t to be extraordinary fragile with respect to impurity scattering so it cannot be easily observed in CeCoIn₅.

To go beyond WCL, we consider a mean field Hamiltonian with both SC and AFM interactions,

$$\mathcal{H} = \sum_{\mathbf{k}\sigma} \left[(\varepsilon_{\mathbf{k}} - \sigma h) c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma} - \left(\Delta_{\mathbf{k}} c_{\mathbf{k}\uparrow}^\dagger c_{-\mathbf{k}\downarrow}^\dagger + \text{H.c.} \right) \right] \quad (5)$$

$$- J \sum_{\mathbf{k}} \left[m_Q c_{\mathbf{k}\downarrow}^\dagger c_{\mathbf{k}+\mathbf{Q}\uparrow} + \text{H.c.} \right] + \frac{|\Delta_0|^2}{V} + J|m_Q|^2,$$

with a tight-binding dispersion $\varepsilon_{\mathbf{k}} = 2t(\cos k_x + \cos k_y) - \mu$. We fix $\mu/t = 0.749$ which sets the wave vectors connecting the nodal points to $\mathbf{Q} = (\pm 0.88\pi, \pm 0.88\pi)$. The order parameter $\Delta_{\mathbf{k}} = \Delta_0 \eta_{\mathbf{k}}$ with $\eta_{\mathbf{k}} = \cos k_x - \cos k_y$ and $\Delta_0 = V \sum_{\mathbf{k}} \eta_{\mathbf{k}} \langle c_{-\mathbf{k}\downarrow} c_{\mathbf{k}\uparrow} \rangle$. Again we first consider a single- \mathbf{Q} XY magnetic ordering. We diagonalize \mathcal{H} and minimize the free energy to obtain the phase diagram as a function h and T for given interactions J and V . The normal state becomes unstable towards magnetic ordering at $J_c = 3.6t$, so that we choose $J = 3.5t$ to describe a system with strong AFM tendencies. The phase diagram for $V = 3.0t$ in Fig. 3 shows the coexistence of AFM and SC (Q -phase) below $T_Q < T^*$ at high fields as well as the first order N to SC transition at $0 < T_c(h) < T^*$. The latter appears here due to purely Zeeman coupling to the field, dominant at high fields for Pauli-limited CeCoIn₅, but is known to persist in the presence of moderate orbital effects [19]. The phase diagram is qualitatively the same for $0.9J_c \lesssim J < J_c$ and is robust against changes to V and the inclusion of the next-nearest neighbor hopping t' . This strong coupling result confirming the instability analytically found in the WCL, Eq.(4), shows that the phase diagram is ubiquitous for systems such as CeCoIn₅.

The above analysis demonstrates the instability of a Pauli limited d -wave superconductor towards incommensurate AFM. We now determine the most stable magnetic order. If the nodes of the order parameter are located at $(\pm 1/\sqrt{2}, \pm 1/\sqrt{2})k_F$, there are four distinct wave-vectors, $\mathbf{Q}_i = (\pm\sqrt{2}, \pm\sqrt{2})k_F$ that connect the nodal quasiparticle pockets. The most general magnetic structure in the SDW state is $m(\mathbf{r}) \equiv m_x(\mathbf{r}) + im_y(\mathbf{r}) = \sum_{j=1,2} [m_{\mathbf{Q}_j} e^{i\mathbf{Q}_j \cdot \mathbf{r}} + m_{\bar{\mathbf{Q}}_j} e^{i\bar{\mathbf{Q}}_j \cdot \mathbf{r}}]$ (recall the spin z -axis is along \mathbf{H}). As CeCoIn₅ has an easy c -axis (taken as spin x -axis), the state with $m_y = 0$ is energetically more favorable. Now consider each single- \mathbf{Q} term $c_{\mathbf{k}+\mathbf{Q}\uparrow}^\dagger c_{\mathbf{k}\downarrow}$. Recall that we pair spin-up Bogoliubov quasiparticles and

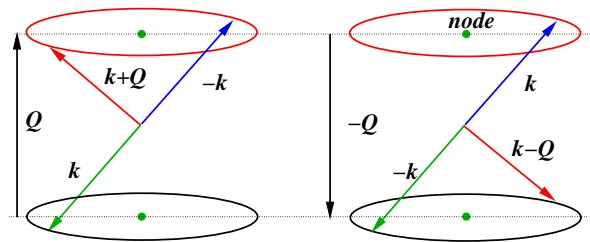


FIG. 2: (Color online) Conditions for pairing of the Fermions at the nodal pockets due to the term $c_{\mathbf{k}+\mathbf{Q}_i\uparrow}^\dagger c_{\mathbf{k}\downarrow}$: a placeholder. Dotted line: Fermi surface, green dots: nodes. Left panel: If \mathbf{k} is in the lower pocket, only the term with $\mathbf{Q}_i = \mathbf{Q}$ satisfies the nesting condition and leads to pairing. Right panel: If \mathbf{k} is in the upper pocket, only $\mathbf{Q}_i = -\mathbf{Q}$ is relevant.

that electron creation (annihilation) operator at \mathbf{k} is a linear combination of the Bogoliubov creation (annihilation) operator with the same momentum and spin, and an annihilation (creation) operator at the opposite spin and momentum. As Fig. 2 shows, for \mathbf{k} , for example, in the pocket centered around $-\mathbf{k}_{n1}$, Eq.(2) produces a logarithmically divergent pairing interaction *only* for $\mathbf{Q} = \mathbf{Q}_1 = 2\mathbf{k}_{n1}$. In contrast, if \mathbf{k} is in the vicinity of \mathbf{k}_{n1} , only $\mathbf{Q} = \bar{\mathbf{Q}}_1 = -2\mathbf{k}_{n1}$ is relevant for the AFM instability. Similar analysis applies to the other pair of pockets. Since \mathbf{Q}_i are far from (π, π) , *in the WCL* the equations for the four Fourier components $m_{\mathbf{Q}_i}$ decouple, look identical, and hence $|m_{\mathbf{Q}_i}| = m_0$ for all \mathbf{Q}_i . The condition $m_y = 0$ immediately yields a double- \mathbf{Q} collinear structure, $m(\mathbf{r}) = m_0[\cos(\mathbf{Q}_1 \cdot \mathbf{r} + \varphi_1) + \cos(\mathbf{Q}_2 \cdot \mathbf{r} + \varphi_2)]$, with $m_{\parallel}|\hat{\mathbf{c}}$ and simultaneous modulation of SDW along the $[110]$ and $[1\bar{1}0]$ directions. Note that the stabilization of this structure is simply due to the counting of the minimal number of independent Fourier components of the order parameter that are needed to fully gap the Fermi pockets of Bogoliubov quasiparticles. The same counting leads to the single- \mathbf{Q} collinear phase of Cr [20].

Beyond WCL, as states away from the Fermi surface participate in AFM, generally single- \mathbf{Q} structures become advantageous [21]. In CeCoIn₅ elastic neutron scattering [9] finds a single- \mathbf{Q} modulation with $\mathbf{Q} \perp \mathbf{H}$ for \mathbf{H} along a nodal direction $[1\bar{1}0]$, and NMR line-shape at $H > 10.2\text{T}$ is consistent with a single- \mathbf{Q} structure [8, 10]. At these high fields the large size of the Bogoliubov pockets leads to an intermediate or strong coupling regime. The first question is whether at lower fields, where pockets are small, our proposed double- \mathbf{Q} structure is realized. NMR measurements of Ref. [10] show an anomalous broadening of the line shape for $9.2\text{T} \lesssim H \lesssim 10.2\text{T}$ and $T = 70\text{mK}$. Moreover, 9.2T is precisely the field at which the amplitude of the ordered moment of the single- \mathbf{Q} structure extrapolates to zero, suggesting that another form of magnetic ordering persists in the $9.2\text{T} \lesssim H \lesssim 10.2\text{T}$ region. The double- \mathbf{Q} structure is a natural candidate for this intermediate phase because

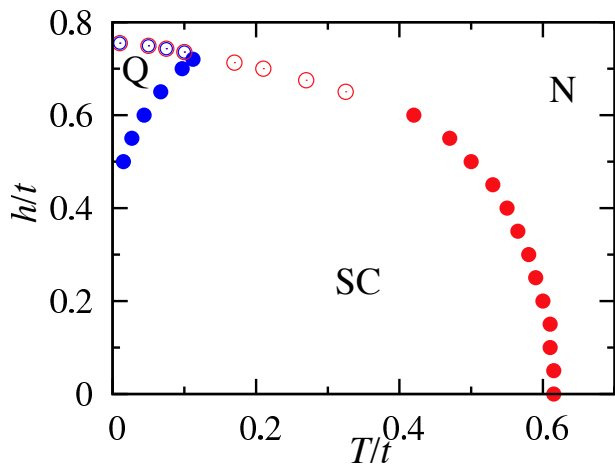


FIG. 3: (Color online) Phase diagram obtained for $V = 3t$ and $J = 3.5t$. Open and filled circles indicate first and second order phase transitions respectively. The red circles are the boundary between the SC and N states, while the blue circles are the boundary for the magnetically ordered phase.

it produces a broad NMR line shape that is consistent with the experimental observation. Detailed neutron and NMR experiments will be able to test this hypothesis. Thermodynamic signatures of the transition from double to single- Q phase are expected to be weak.

For $\mathbf{H} \parallel$ nodes, the orbital coupling suppresses the SDW modulation with $\mathbf{Q} \perp \mathbf{H}$ at low fields. Within the semiclassical approximation the Doppler shift, $\delta E \approx \mathbf{v}_F \cdot \mathbf{p}_s$, where $\mathbf{p}_s \perp \mathbf{H}$ is the momentum of the Cooper pairs, has opposite sign for the two pockets connected by \mathbf{Q} , as $\mathbf{v}_{F1} = -\mathbf{v}_{F2}$. From Eq. (1) this expands one of the pockets and shrinks its counterpart, breaking the nesting condition. For some Fermi surface geometries an additional field-dependent modulation may still allow SDW formation, similar to pnictides [22, 23] and exciton formation [24]. Generically however, AFM is favored when the typical Doppler shift $\delta E_D \sim \Delta_0 \sqrt{H/H_{c2}^{orb}} \geq \mu_B H$, where H_{c2}^{orb} is the orbital critical field. In CeCoIn₅ this gives fields $H \geq H_P^2/H_{c2}^{orb}$, where H_P is the Pauli limiting field, above 20-40% of the observed $H_{c2}(T=0)$. The semiclassical approach is inadequate at high fields [25] where a more detailed analysis is required to determine whether the $\mathbf{Q} \perp \mathbf{H}$ state is stable. In weak coupling at low fields, SDW with $\mathbf{Q} \parallel \mathbf{H}$ may exist since δE vanishes for the quasiparticle pockets around the nodes aligned with the field [26], but T_Q is exponentially small.

Anisotropic spin-spin interactions induced by the spin-orbit coupling may also favor ordering with $\mathbf{Q} \perp \mathbf{H}$, but depend on specific models. An intriguing possibility is that this choice is due to putative FFLO state. In the presence of vortices the FFLO modulation is along the field at a wave vector determined by the field magnitude, and interferes destructively with the AFM at $\mathbf{Q} \parallel \mathbf{H}$ whose wave vector is fixed by the position of the SC

nodes. Hence $\mathbf{Q} \perp \mathbf{H}$ is stabilized. Since generically $T_Q(H)$ that we find differs from the onset of the FFLO modulation, one expects two transitions from the superconducting state, first to a double- Q AFM, followed by the FFLO+single- Q state. Further experiments will distinguish between these scenarios.

To summarize, our theoretical framework describes a generic instability of Pauli-limited unconventional superconductors under Zeeman effect. This instability leads to incommensurate AFM at the wave-vectors connecting opposite nodal points. Our theory describes the existing experiments on CeCoIn₅ and suggests studies to identify the double- Q collinear phase that we find to be favorable in the weak coupling regime, and which may exist in the intermediate field range.

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