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# Flat band magnetism and helical magnetic order in Ni-doped SrCo<sub>2</sub>As<sub>2</sub>

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A series of Sr(Co<sub>1-x</sub>Ni<sub>x</sub>)<sub>2</sub>As<sub>2</sub> single crystals was synthesized allowing a comprehensive phase diagram with respect to field, temperature, and chemical substitution to be established. Our neutron diffraction experiments revealed a helimagnetic order with magnetic moments ferromagnetically (FM) aligned in the *ab* plane and a helimagnetic wavevector of  $q = (0, 0, 0.56)$  for  $x = 0.1$ . The combination of neutron diffraction and angle-resolved photoemission spectroscopy (ARPES) measurements show that the tuning of a flat band with  $d_{x^2-y^2}$  orbital character drives the helimagnetism and indicates the possibility of a quantum order-by-disorder mechanism.

## I. INTRODUCTION

The exploration of materials in proximity to quantum phase transitions is a fruitful area for discovering exotic states of matter due to the strong influence of quantum fluctuations. This idea can be traced to Villain who coined the name *order-by-disorder* when investigating frustrated insulating magnets<sup>1</sup>. The central idea refers to the fact that quantum fluctuations, akin to classical entropic effects, can lift the large degeneracy of ground states and favor a particular order, hence the term *order-by-disorder*<sup>2</sup>. This is considered to be the quantum equivalent to the theme used to explain a variety of phenomena including surface tension and DNA folding, and has been employed to explain unconventional superconductivity<sup>3</sup> and even emergent gravity<sup>4</sup>. There is large recent theoretical interest in itinerant ferromagnets in which quantum fluctuations dominate and drive the system into a variety of novel magnetic states in the vicinity of a quantum critical point<sup>5-7</sup>, such as a helical state driven by ferromagnetic (FM) spin fluctuations. Meanwhile, as an origin of ferromagnetism complementary to that described by Nagaoka<sup>8</sup>, flat-band physics<sup>9</sup> has garnered attention since it provides fertile ground for diverse interaction-driven quantum phases including FM order, a Mott insulating phase<sup>10</sup>, and superconductivity<sup>11</sup>. Therefore, it is interesting to search for helimagnetism associated with a flat-band lying close to the chemical potential in a material close to a quantum critical point.

In the AFe<sub>2</sub>As<sub>2</sub> ( $A = \text{Ca, Sr, Ba}$ ) family of iron pnictides, it is well known that the superconducting electron pairing is attributed to antiferromagnetic (AF) spin fluctuations<sup>12,13</sup>. However, FM spin fluctuations may

also be important to electron pairing<sup>14,15</sup> and were recently observed in Co-substituted compounds by nuclear magnetic resonance (NMR)<sup>16</sup> and neutron scattering experiments<sup>17,18</sup>. Furthermore, electronic structure calculations<sup>19,20</sup> and angle resolved photoemission spectroscopy (ARPES) experiments indicate that ACo<sub>2</sub>As<sub>2</sub><sup>17,21,22</sup> is in proximity to a FM instability due to the existence of a flat band nearby the Fermi level, although these materials remain paramagnetic down to 2 K with AF low energy spin fluctuations<sup>17</sup>. Since chemical substitution can shift the Fermi level relative to the band structure<sup>23</sup>, substitution of Co with Ni will drive the system toward a Van Hove singularity associated with the flat band and efficiently promote the FM instability. Therefore, it is interesting to investigate how AF and FM spin fluctuations evolve in A(Co<sub>1-x</sub>Ni<sub>x</sub>)<sub>2</sub>As<sub>2</sub> and to explore the relevant emergent phenomena.

We successfully synthesized single crystals [Fig.1(a)] of a series of Sr(Co<sub>1-x</sub>Ni<sub>x</sub>)<sub>2</sub>As<sub>2</sub> with a range of Ni concentrations between 0 and 0.6, and carried out systematic magnetic susceptibility,  $\chi$ , and magnetization,  $M$ , measurements. Sr(Co<sub>1-x</sub>Ni<sub>x</sub>)<sub>2</sub>As<sub>2</sub> has a ThCr<sub>2</sub>Si<sub>2</sub>-type body-centered tetragonal crystal structure with no indication of a structural transition [Fig. 1(b)]<sup>24</sup>. Considering both SrCo<sub>2</sub>As<sub>2</sub><sup>17,19</sup> and SrNi<sub>2</sub>As<sub>2</sub><sup>25</sup> are paramagnetic without magnetic order at low temperature, it is surprising that we discovered a helical magnetic order in Sr(Co<sub>0.9</sub>Ni<sub>0.1</sub>)<sub>2</sub>As<sub>2</sub> with a magnetic wave vector  $q = (0, 0, 0.56)$  and transition temperature  $T_c = 28$  K [Fig. 1(c) and 2(c)]. We find that the transition temperature varies systematically with substitution and has maximum value at  $x = 0.1$  from susceptibility measurements [Fig. 2(c)]. Our results suggests that the ground state is he-

limagnetic (HM) with moments lying parallel to the  $ab$  easy plane while rotating with respect to the  $c$ -axis in adjacent layers [Fig. 1(c)]. Measurements of  $M(H)$  with an in-plane magnetic field at low temperatures ( $2 \text{ K} \leq T \leq 4 \text{ K}$ ) demonstrate a two-step transition from HM order first into a partially polarized magnetic (PPM) phase and ultimately into a fully polarized magnetic (FPM) state. Under a field parallel with the  $c$ -axis, the magnetization is linearly dependent on  $H$  prior to saturation at the higher field. Combining neutron diffraction and ARPES experiments, we established a close connection between the magnetic moments and a flat band of the  $d_{x^2-y^2}$  orbital character. Since it was suggested that  $\text{BaCo}_2\text{As}_2$  is a quantum paramagnet near a FM critical point<sup>22,26</sup>, the helimagnetic order observed in Ni-substituted  $\text{SrCo}_2\text{As}_2$  may be induced by quantum fluctuations in the vicinity of the putative quantum critical point<sup>2</sup>.

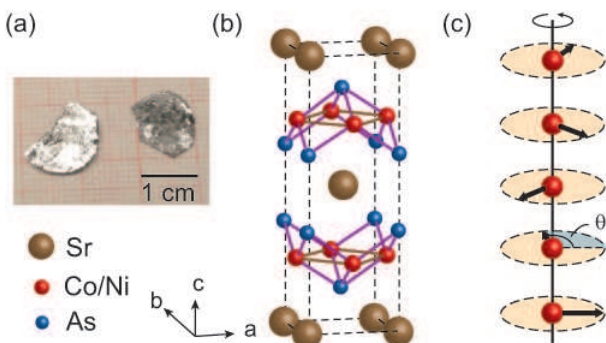


FIG. 1: (a) Single crystals of  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ . (b) Tetragonal structure of  $\text{SrCo}_2\text{As}_2$ . (c) Helical magnetic structure along the  $c$ -axis with a rotation angle  $\theta$  between neighboring layers.

## II. EXPERIMENTAL DETAILS

### A. Sample Growth and Magnetization measurements

Single crystals of  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  were grown from solution using a self-flux method with the ratio  $\text{Sr}:(\text{Co}_{1-x}\text{Ni}_x):\text{As} = 1:5:5$ . The elements were placed in an aluminum oxide crucible and sealed in an evacuated quartz tube. After heating slowly below  $830^\circ\text{C}$ , the mixture was cooked at  $1200^\circ\text{C}$  for 20 hours and then slowly cooled down to  $1050^\circ\text{C}$  at a rate of  $3^\circ\text{C}/\text{h}$  and then down to  $800^\circ\text{C}$  at  $10^\circ\text{C}/\text{h}$ . Single crystals were obtained by cleaning off the flux. The typical crystals were about  $1 \text{ cm}^2$  in size and a few mm in thickness [Fig. 1(a)].

Temperature- and field-dependent dc magnetization measurements were performed on a Quantum Design (QD) Physical Property measurement system (PPMS) in Beijing Normal University and a Magnetic Property Measurement System (MPMS) in Louisiana State University.

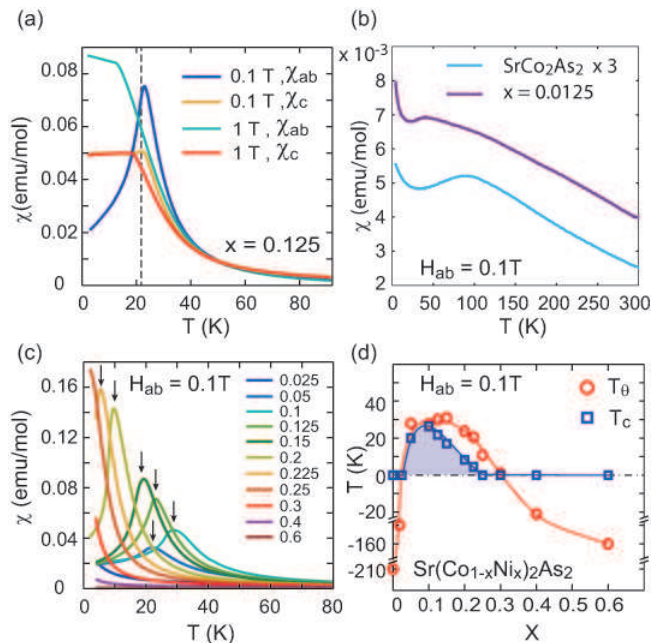


FIG. 2: (a) Magnetic susceptibility,  $\chi$ , in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  with field  $H = 0.1$  and  $1\text{-T}$  parallel and perpendicular to  $c$ -axis for  $x = 0.125$ . (b) and (c)  $\chi(T)$  for crystals with  $0 \leq x \leq 0.6$ . (c) Critical temperature,  $T_c$ , and Weiss temperature  $T_\theta$  vs.  $x$  in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ .

### B. Neutron Diffraction

Neutron powder diffraction (NPD) data for compound  $\text{Sr}(\text{Co}_{0.9}\text{Ni}_{0.1})_2\text{As}_2$  were collected at the NIST Center for Neutron Research on the high resolution powder neutron diffractometer (BT-1) with neutrons of wavelength  $1.5403 \text{ \AA}$  (at 295 K) and  $2.0775 \text{ \AA}$  (at 30 and 5 K) produced by using  $\text{Cu}(311)$  and  $\text{Ge}(311)$  monochromators, respectively. Collimators with horizontal divergences of  $15'$ ,  $20'$  and  $7'$  of arc were used before and after the monochromator and after the sample, respectively. Data were collected in the  $2\theta$  range of  $3\text{-}168^\circ$  with a step size of  $0.05^\circ$ . The structural parameters were refined by Rietveld refinement using the GSAS and EXPGUI programs<sup>27,28</sup>. The atomic neutron scattering factors used in the refinements for Sr, Co, Ni, and As were 0.702, 0.253, 1.03, and  $0.658 \times 10^{-12} \text{ cm}$ , respectively. About 5 grams of  $\text{Sr}(\text{Co}_{0.9}\text{Ni}_{0.1})_2\text{As}_2$  single crystals were grinded into powder for the neutron powder diffraction measurements. Single crystal neutron diffraction measurements were carried out on two instruments at the High Flux Isotope Reactor (HFIR) at Oak Ridge National Laboratory (ORNL), the single crystal diffractometer HB3A and the recently upgraded wide angle neutron diffractometer (WAND2) at the HB-2C beam port. The monochromatic incident beam of wavelength  $1.546 \text{ \AA}$  was used on HB3A diffractometer which is provided by a  $\text{Si}(220)$  monochromator<sup>29</sup>. The detector on HB3A is a two-dimensional (2D) scintillation Anger camera with 1 mm

spatial resolution. WAND2 uses a monochromatic beam with a wavelength of 1.48 Å provided by the Ge(311) monochromator. It is equipped with a 2D position sensitive detector (PSD), which covers the scattering angles of 120° and  $\pm 7.5^\circ$  in the horizontal and vertical directions, respectively. An oscillating radial collimator is used before the PSD<sup>30</sup> On both diffractometers the sample was inserted into a Closed Cycle Refrigerator that provided a temperature range from 4 K to 300 K.

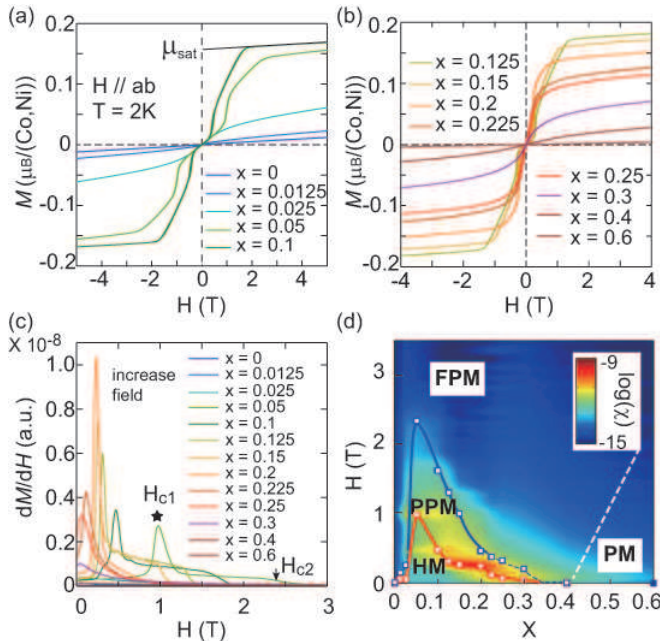


FIG. 3: (a),(b)  $M(H)$  for crystals with  $0 \leq x \leq 0.6$ . (c)  $dM/dH$  vs.  $H$  for  $0 \leq x \leq 0.6$ . (d) Magnetic phase diagram with  $H$  and  $x$ .  $H_{c1}$  and  $H_{c2}$  are defined in frame (c).  $H_{c2}$  is represented as blue dashed curve where it is poorly determined by the data. The white dashed line is a speculative separation (or crossover) between paramagnetic (PM) and field-induced FM states. PPM refers to the partially polarized magnetic state, and FPM means fully polarized magnetic state.

For single crystal diffraction measurements on  $\text{Sr}(\text{Co}_{0.9}\text{Ni}_{0.1})_2\text{As}_2$ , we define the momentum transfer  $\mathbf{Q}$  in three-dimensional reciprocal space in  $\text{Å}^{-1}$  as  $\mathbf{Q} = H\mathbf{a}^* + K\mathbf{b}^* + L\mathbf{c}^*$ , where  $H$ ,  $K$ , and  $L$  are Miller indices and  $\mathbf{a}^* = \hat{\mathbf{a}}2\pi/a$ ,  $\mathbf{b}^* = \hat{\mathbf{b}}2\pi/b$ ,  $\mathbf{c}^* = \hat{\mathbf{c}}2\pi/c$  with  $a = b \approx 3.95 \text{ Å}$ , and  $c = 11.62 \text{ Å}$ .

### C. Angle-resolved Photoemission Spectroscopy (ARPES)

ARPES measurements were performed at the Dreamline beam line of the Shanghai Synchrotron Radiation Facility using a Scienta DA80 analyzer and at the beam line 13U of the National Synchrotron Radiation Laboratory (Hefei) equipped with a Scienta R4000 analyzer. The energy and angular resolutions were set to 15 meV and

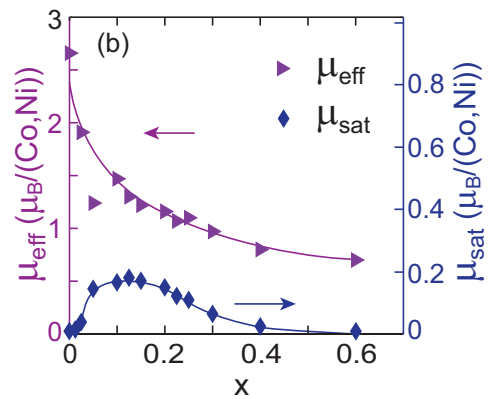


FIG. 4: Effective magnetic moment,  $\mu_{eff}$ , by fits of the C-W law to the magnetic susceptibility above  $T_c$ , and saturated magnetic moment,  $\mu_{sat}$ , vs.  $x$ . The large ratio of  $\mu_{eff}/\mu_{sat}$  reflects the itinerant nature of magnetism.

0.2°, respectively. Samples were cleaved *in situ*, yielding flat mirror-like (001) surfaces. During the measurements, the temperature was kept at 20 K and the pressure was maintained better than  $5 \times 10^{-11}$  Torr.

## III. RESULTS

### A. Magnetization and magnetic susceptibility data

The magnetic susceptibility  $\chi(T)$  measured for  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  with  $x = 0.125$  is shown in Fig. 2(a). We find a clear magnetic phase transition at  $T_c = 22 \text{ K}$ , characterized by a maximum in  $d(\chi \cdot T)/dT$ <sup>31</sup> for  $H = 1 \text{ kOe}$  and  $H$  both parallel and perpendicular to the  $c$ -axis. For  $H = 0.1 \text{ T}$ ,  $\chi(T < T_c)$  displays a strong dependence on the direction of  $H$  relative to the crystalline lattice, exhibiting a behavior typical of AF order. In contrast to the  $A$ -type AF order in  $\text{CaCo}_2\text{As}_2$  where spins are ordered along the  $c$ -axis, the anisotropy of  $\chi(T)$  for  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  clearly indicates that while the system is isotropic at high temperature, the spins are aligned in  $ab$  plane below  $T_c$ <sup>24</sup>, exhibiting the typical behavior of AF magnet with an easy plane. By fitting the high temperature susceptibility (80–200 K) with the Curie-Weiss law [ $\chi(T) \propto (T - T_\theta)^{-1}$ ], we find a positive  $T_\theta$  ( $\approx 28 \text{ K}$  for  $H_{ab}$  and 25K for  $H_c$ )<sup>24</sup>, suggesting that the system is dominated by FM interactions.

In classical molecular-field theory<sup>32</sup>, the parameter  $f \equiv T_\theta/T_c$  is usually found to be smaller than 1 with  $-\infty < f < -1$  for antiferromagnets and 1 for ferromagnets. This is because the real transition (either FM or AF) has to arise before the divergence of  $\chi(q)$  which describes the instability of the system towards a particular magnetic state. Therefore, the divergence of Curie-Weiss susceptibility at  $T_\theta > T_c$  ( $f > 1$ ) reflects that the system is near a FM instability. However, a suppression of the uniform susceptibility [ $\chi(q = 0)$ ] above  $T_c$  indicates



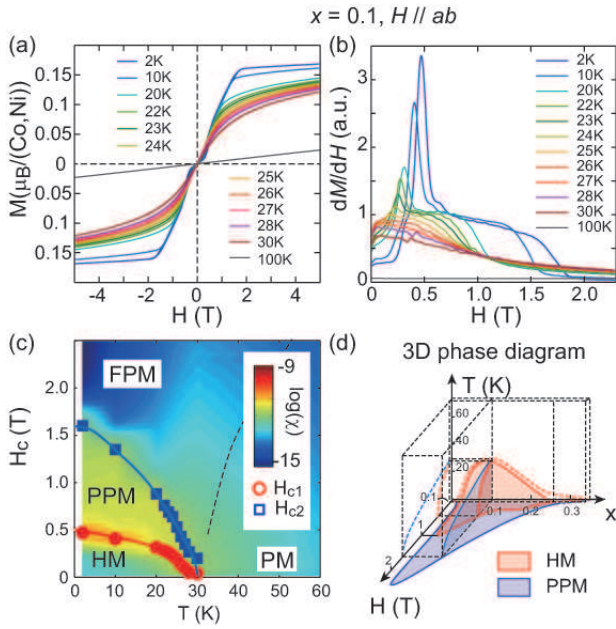


FIG. 5: (a),(b)  $M_{ab}$  and  $dM_{ab}/dH$  vs.  $H$  at temperatures identified in the figures. (c) Phase diagram determined from data in frames (a) and (b). Dashed line is a speculative crossover separating the fully polarized magnetic, FPM, and paramagnetic, PM, phases. PPM denotes the partially polarized magnetic phase. (d) Three dimensional phase diagram combining Fig.2(d), 3(d) and 7(c).

the influence of low dimensionality since a 2D isotropic Heisenberg system cannot exhibit magnetic order above  $T = 0$ . This strongly suggests quantum fluctuations may play a significant role. In addition, the large enhancement of  $\chi_{ab}(T < T_c)$  with in-plane field at  $H = 1$  T suggests the existence of a field-induced meta-magnetic transition.

In order to understand the evolution of this magnetic state with  $x$ , we systematically explore  $\chi(T)$  for  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  single crystals. In Fig. 2(b), we show magnetic susceptibility of stoichiometric  $\text{SrCo}_2\text{As}_2$  and slightly Ni-doped  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  with  $x = 0.0125$ . There is a broad maximum arising around 100 K for  $x = 0$  and 50 K for  $x = 0.0125$ , similar to previous report on  $\text{SrCo}_2\text{As}_2$ <sup>19</sup> in which the maximum in  $\chi(T)$  was attributed to a cross-over from a coherent to an incoherent Fermi liquid state with increasing  $T$ . However, we note that this broad maximum also exists in other itinerant magnetic materials in the proximity to ferromagnetism, such as  $\text{CrGe}$ <sup>33</sup>. The gradual suppression with Ni substitution might suggest its close relationship with the novel magnetic phase observed in compounds with larger Ni substitution. With larger  $x$  as shown in Fig. 2(c), we see that the magnetic transition temperature depends on  $x$  in a systematic way creating a dome-like feature in the  $x$ - $T$  phase diagram with a maximum  $T_c$  at  $x \sim 0.1$  [Fig. 2(d)]. In Fig. 2(d), we summarize  $T_\theta$  by fitting the Curie-Weiss form to  $\chi(T)$  for  $0 \leq x \leq 0.6$ <sup>24</sup>. Curiously,

for Ni concentrations within the dome of magnetic ordering, the dominant interaction, as assessed by  $T_\theta$ , is ferromagnetic ( $T_\theta > 0$ ) with  $f > 1$ , while an AF interaction ( $T_\theta < 0$ ) dominates outside this dome. The concurrence of the HM phase transition and the positive  $T_\theta$  strongly indicates that the magnetic order is driven by FM interactions.

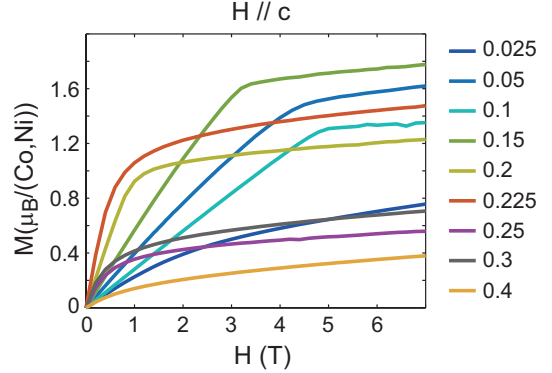


FIG. 6: Magnetization,  $M$ , vs. magnetic field,  $H$  with  $H$  parallel to the  $c$ -axis at a variety of Ni concentrations.

In Figs. 3(a) and (b), we applied a magnetic field along the  $ab$ -plane and measured  $M(H)$  for a series of Ni concentrations. Field-induced meta-magnetic transitions associated with the reorientation of magnetic moments are clearly observed in the magnetically ordered compounds. In Fig. 3(a), for example, at  $x = 0.1$ , the system is in a helical magnetic ground state at low temperatures. The magnetization displays a linear dependence on the in-plane magnetic field at low field [Fig. 3(c)]. As the field increases, a partially polarized magnetic (PPM) intermediate state arises at  $H_{c1} \sim 0.5$  T. This transition is clearly observed in  $\chi(H) \equiv dM/dH$  as a sharp peak which defines the critical field as  $H_{c1}$  [Fig. 3(c)]. The magnetization around  $H_{c1}$  exhibits hysteresis behavior<sup>24</sup> with magnetic field, implying a first-order transition. In the intermediate state, the susceptibility displays a plateau between  $H_{c1}$  and  $H_{c2}$  beyond which the system evolves into a fully polarized magnetic (FPM) state. Furthermore, as the Ni concentration changes, the plateau in  $\chi(H)$  shrinks and disappears for  $x < 0.05$  or  $x \geq 0.2$ , such that the determination of  $H_{c2}$  in these regions is somewhat ambiguous. Therefore, we employed a blue dashed line in the  $x$ - $H$  phase diagram to represent the poorly defined  $H_{c2}$  [Fig. 3(d)]. We have included the magnetic susceptibility ( $\chi \equiv dM/dH$ ) as a color plot (log scale) in Fig. 3(d) to emphasize the clear delineation of magnetic phases.

In Fig. 4, the effective magnetic moment,  $\mu_{eff}$ , estimated from the Curie constant, and the saturated magnetic moment,  $\mu_{sat}$ , according to the high field magnetization, are presented. The magnitude of the effective moment is similar to that for an  $S=1/2$  system while  $\mu_{sat}$  is about one order of magnitude smaller for  $x > 0.05$ . This renders a large Rhodes-Wholfarth ratio,  $\mu_{eff} / \mu_{sat}$ , sug-

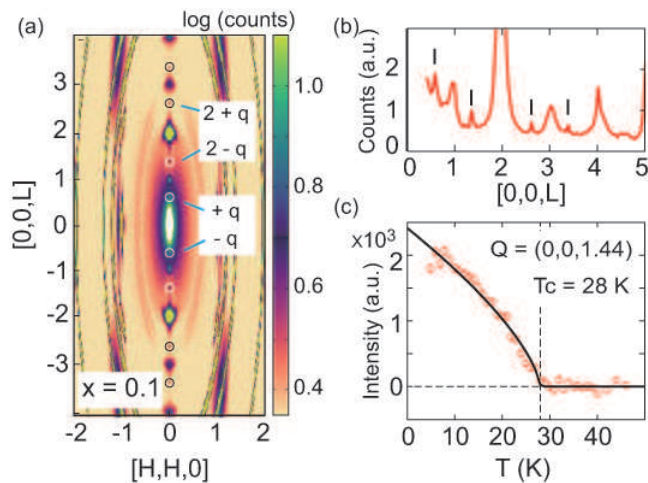


FIG. 7: (a) Neutron diffraction measurements on  $\text{Sr}(\text{Co}_{0.9}\text{Ni}_{0.1})_2\text{As}_2$  in the  $[H, H, L]$  plane<sup>24</sup>. (b) One-dimensional cut along the  $[0, 0, L]$  direction in (a). The intensities at  $(0, 0, L)$  with  $L = \text{odd}$  number are due to double scattering<sup>34</sup>. (c) Temperature dependence of the magnetic peak at  $Q = (0, 0, 1.44)$ .

gesting that the magnetism in this system is itinerant in character.

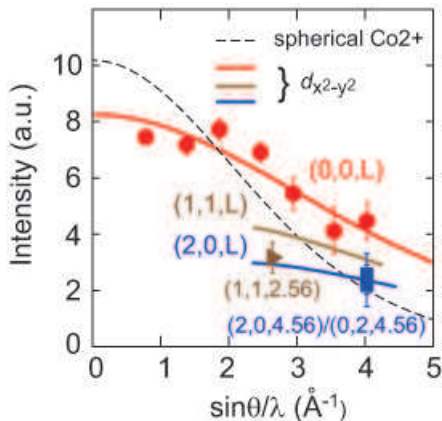


FIG. 8: Integrated intensity of magnetic Bragg peaks. The dashed curve is the magnetic form factor of  $\text{Co}^{2+}$  using a spherical approximation. The solid curves are magnetic form factors for the  $d_{x^2-y^2}$  orbital multiplied with a polarization factor along different measured directions for a helical order. Red, brown and blue are along the  $[0, 0, L]$ ,  $[1, 1, L]$ , and  $[2, 0, L]/[0, 2, L]$  directions, respectively.

In Figs. 5(a) and (b), we investigated the temperature dependence of  $M(H)$  and  $\chi(H)$  for  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  with  $x = 0.1$ . The plateau in  $\chi(H)$  was observed at all temperatures below  $T_c$  [Fig.5(b)]. We note that even in the paramagnetic state, the magnitude at  $T = 30$  K is dramatically enhanced as the system approaches the magnetic transition temperature, in comparison with that at a higher temperature of  $T = 100$  K. Based on these measurements, a  $H$ - $T$  phase diagram for  $x = 0.1$  is

presented in Fig. 5(c) and a schematic three-dimensional ( $H$ - $T$ - $x$ ) phase diagram is shown in Fig. 5(d). In Fig. 6, we plot the magnetization of  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  over a range of  $x$  with field parallel to the  $c$ -axis. The magnetization at low fields has a linear dependence on field, before saturating at higher fields. In summary, our magnetization and susceptibility measurements on  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  are consistent with the magnetic behavior of a system with helical spin order. However, further neutron diffraction measurements are required to determine the magnetic structure of the ground state.

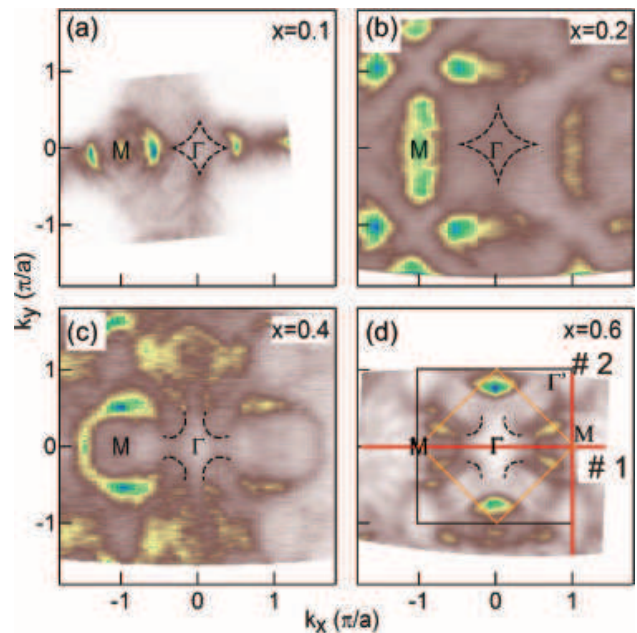


FIG. 9: Plot of the ARPES intensity at  $E_F$  of  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  with  $x = 0.1, 0.2, 0.4, \text{ and } 0.6$ . A complex structure of Fermi surfaces is observed and the topology changes dramatically from  $x=0.1$  to  $x=0.6$  due to the existence of flat band dispersion. The dashed lines curves are guide to the eye.

## B. Neutron diffraction

In order to understand the changes that occur with  $x$  in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ , we probed the magnetic structure at zero field and  $T = 4$  K for  $x = 0.1$  via neutron diffraction experiments. We chose to explore a  $\text{Sr}(\text{Co}_{0.9}\text{Ni}_{0.1})_2\text{As}_2$  single crystal as these samples displayed the highest  $T_c$  with one of the largest  $\mu_{\text{sat}}$  for this series. Figure 7(a) displays the neutron diffraction pattern in the  $[H, H, L]$  scattering plane. Incommensurate peaks at  $(0, 0, n \pm q)$  with  $n$  an even integer and  $q = (0, 0, 0.56)$  are clearly observed in Fig 7(b), manifesting either a planar spiral or sinusoidal magnetic structure. However, a sinusoidal magnetic structure is unlikely in this material since it requires a uniaxial spin anisotropy along either the  $a$  or  $b$  axis and therefore breaks the tetragonal symmetry of the

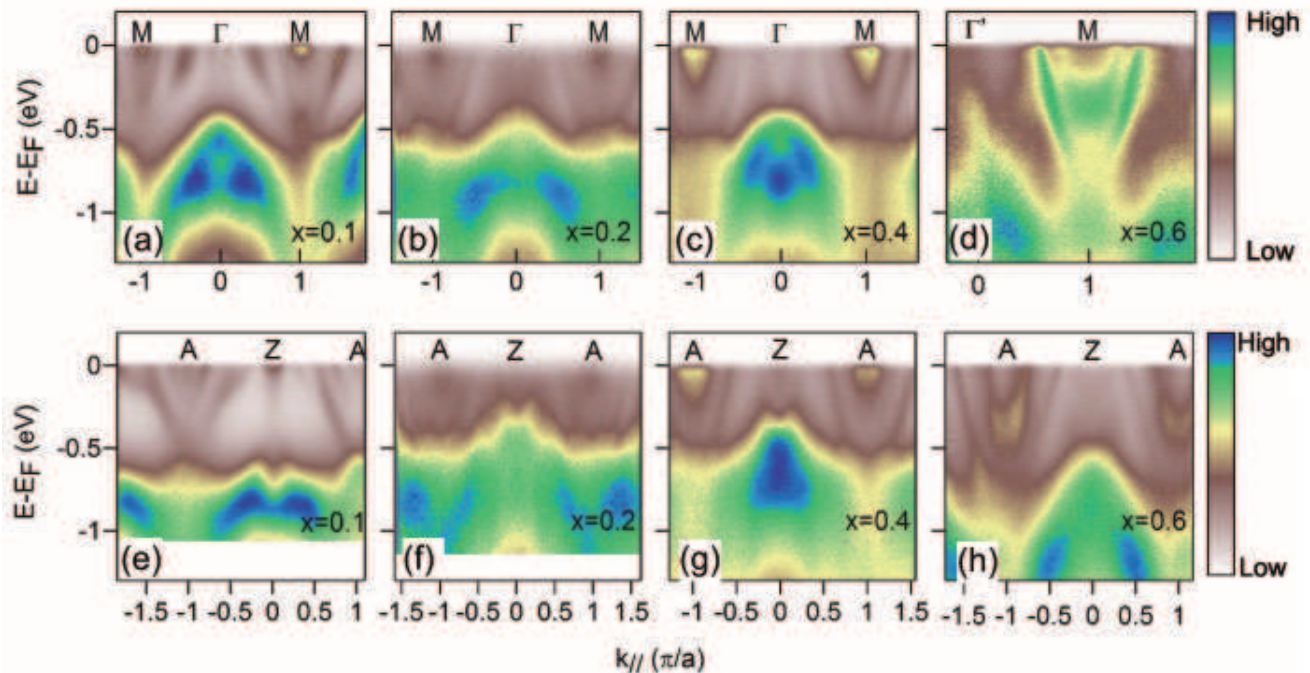


FIG. 10: Intensity plots of the band dispersion along the  $\Gamma$ -M (a-d) and Z-A (e-h) directions from ARPES measurements for  $x = 0.1, 0.2, 0.4,$  and  $0.6$ .

underlying crystalline lattice<sup>24</sup>. This is substantially different from the collinear AF order in iron pnictides<sup>13</sup> or the commensurate A-type AF order in  $\text{CaCo}_2\text{As}_2$ <sup>35</sup>. In  $\text{EuCo}_2\text{As}_2$ <sup>36</sup>, a similar helical order has been observed. However, the magnetic moments are localized on Eu sites with  $S = 7/2$ , in contrast to the itinerant magnetism in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ , implying the underlying physics is significantly different. In addition, the dissimilar spin anisotropy between  $\text{CaCo}_2\text{As}_2$ <sup>37</sup> and  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  suggests a change from an easy-axis to an easy-plane spin anisotropy<sup>38</sup>. Furthermore, the value of  $q$  is close but not equal to  $(0, 0, 0.5)$  indicating a short pitch for the helix, about 4 Co-layers or 2 unit cells, resulting in spins on adjacent Co-layers being nearly perpendicular. This severely constrains the likely exchange interaction responsible for the magnetism. Figure 7(c) demonstrates the  $T$ -dependence of the scattering intensity at  $Q = (0, 0, 1.44)$ . The  $T_c$  of 28 K agrees well with that determined from  $\chi(T)$  in Fig. 2(c). A longitudinal scan along the  $[0, 0, L]$  direction at 4 K (Fig. S4 in Ref.<sup>24</sup>) indicates that the magnetic ordering is long-range within the current instrumental resolution.

In Fig. 8, we show the magnetic intensity from neutron diffraction measurements in comparison with the calculated structure factor for helical order. We employed a  $d_{x^2-y^2}$  magnetic form factor for  $\text{Co}^{2+}$  ions<sup>24,39</sup> and the results (solid lines) are in good agreement with our neutron diffraction measurements. This agreement suggests that the magnetic moments in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  are closely associated with electrons having  $d_{x^2-y^2}$  or-

bit character. The spherical  $\text{Co}^{2+}$  magnetic form factor (dashed curve) is plotted for comparison and is a much poorer representation of our data.

### C. Electronic band structure

In nominally pure  $\text{SrCo}_2\text{As}_2$ , a flat band exists at an energy just above the Fermi level near the  $M$  point of the Brillouin Zone (BZ)<sup>17,20</sup>. Substitution of Ni is expected to raise  $E_F$  so that this flat band is partially occupied resulting in  $E_F$  being closer to a Van Hove singularity. To establish the connection between the helical magnetic phase and this flat band, we carried out ARPES experiments on a series of  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  samples ( $x = 0, 0.1, 0.2, 0.4$  and  $0.6$ ) to map out their electronic structures. We show in Fig. 9 the Fermi surfaces of  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  with  $x = 0.1, 0.2, 0.4, 0.6$  as measured by ARPES. A diamond-shaped electron-like Fermi surface (dashed curve) is observed at the  $\Gamma$  point in the sample with  $x = 0.1$ , similar to that observed in nominally pure  $\text{Sr}(\text{Ba})\text{Co}_2\text{As}_2$ <sup>17,21</sup>. This band is associated with a  $d_{x^2-y^2}$  orbital and has flat dispersion. It is likely responsible for in-plane ferromagnetism and the observed helimagnetic order. We note that as the Ni concentration increases, this Fermi surface opens along the  $\Gamma$ - $M$  direction, and is further separated at  $x = 0.6$ , consistent with the fact that the flat band shifts down below the Fermi level.

In Fig. 10, we display the cuts of ARPES spectra along



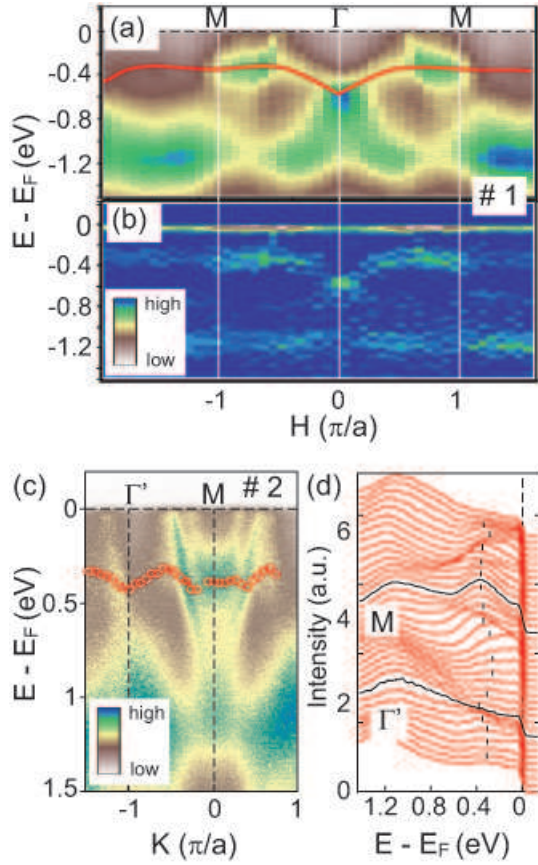


FIG. 11: (a) and (b) ARPES Intensity plot and its second derivative along the cut #1 direction as shown in Fig. 9 (d). (c) and (d) ARPES spectra along the cut #2 direction and its corresponding Energy distribution curve (EDC).

the  $\Gamma$ - $M$  and  $Z$ - $A$  directions for these samples. While there are barely changes in  $x = 0.1, 0.2$  and  $0.4$  samples, the whole band structure suddenly shifts down for  $x = 0.6$ . This shows that the flat band along the  $\Gamma$ - $M$  direction sinks below the  $E_F$  and thus is only observed in ARPES spectra of Fig. 10(d). In order to further prove the existence of the flat band, we made two cuts along both the horizontal and vertical directions labeled as red lines in Fig. 9(d) (for  $x = 0.6$ ) and display these in Fig. 11. Figures 11(a) and (c) are the intensity plots of band dispersion along the cut 1 and cut 2 directions. A nearly flat band dispersion around  $-0.4$  eV with an electron-like band minimum at the  $\Gamma$  point is realized in both cuts. These flat band spectra typically have low intensity in ARPES<sup>40</sup>, but are clearly resolved in the second-derivative plot [Fig.11(b)] and the energy distribution curves (EDCs) [Fig.11(d)].

To investigate the  $x$ -dependence of this flat band, we show the EDC cuts at the  $M$  point for samples with  $0 \leq x \leq 0.6$  in Fig. 12(a). One peak close to  $E_F$  associated with the flat band is identified by the arrows and is degenerate with another electronic band at the  $M$  point<sup>17,20</sup>. The Fermi-Dirac function cuts off ARPES

spectra at  $E_F$  affecting the shape of these peaks. To avoid this effect, we use the symmetrized EDCs to determine whether the band is located below or above the Fermi energy. Similar methods have been applied to determine small superconducting gaps in iron based superconductors<sup>41</sup> [Fig. 12(b)]. A central peak at  $E_F$  manifests that the band is either at or above the Fermi energy and thus gives the lower limit of the band location. We use the value estimated from dynamic mean field theory (DMFT) calculations on pure  $\text{SrCo}_2\text{As}_2$  in previous work<sup>17,20</sup> as the upper limit and the results are summarized in Fig. 12(c). The shading area roughly establishes the evolution of the energy location of the flat band with Ni substitution. It is clear that the band shifts with  $x$  at  $x < 0.4$  much more slowly than at larger  $x$ . This is a manifestation of the large density of states (DOS) of the flat band for electrons filling as it shifts across  $E_F$  ( $0 < x < 0.4$ ). This flat band has  $d_{x^2-y^2}$  orbital character and makes a significant contribution to DOS near the Fermi energy<sup>17</sup>. Our ARPES results for  $0 \leq x \leq 0.6$  confirm that this flat band is partially occupied for the range of  $x$  with helimagnetism, and suggest that the helical magnetic phase is closely associated with this band.

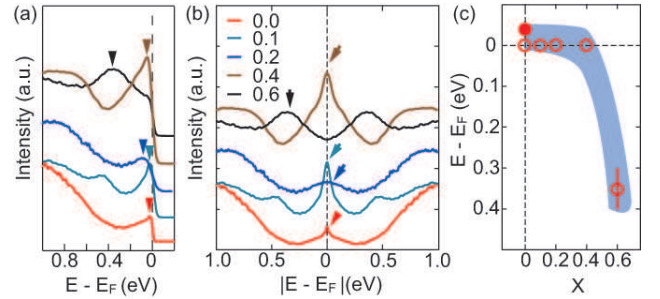


FIG. 12: (a) Energy distribution curves (EDCs) at the  $M$  point for  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  with  $x = 0, 0.1, 0.2, 0.4, 0.6$ . Small peaks close to  $E_F$  were identified as residual spectra from the band above the Fermi level truncated by Fermi-Dirac function. (b) Symmetrized EDCs. The peaks at  $E_F$  in symmetrized EDCs set the lower limit of the energy location of the flat band within the instrumental resolution. (c) Energy location of the flat band determined by ARPES and that from DMFT calculation<sup>20</sup> for  $x = 0$  which we used as the upper limit. The shaded area is a guide to the eye. The evolution of the energy of the flat band with respect to the Fermi level is demonstrated.

#### IV. DISCUSSION AND CONCLUSION

In  $\text{ACo}_2\text{As}_2$  systems, density functional theory (DFT) plus DMFT calculations suggest that FM instabilities are due to a flat band residing near the  $E_F$ . However, experiments show an evolution from AF order in  $\text{CaCo}_2\text{As}_2$ <sup>18,35</sup> to paramagnetism in  $\text{BaCo}_2\text{As}_2$ <sup>22</sup> (or  $\text{Ba}(\text{Fe}_{1/3}\text{Co}_{1/3}\text{Ni}_{1/3})_2\text{As}_2$ <sup>26</sup>) with evidence for a nearby FM critical point<sup>22,26</sup>. This indicates that the magnetism

can be tuned by chemical substitution. In  $\text{SrCo}_2\text{As}_2$ , previous inelastic neutron scattering experiments<sup>17</sup> revealed the coexistence of FM and AF spin fluctuations. It is likely that the fine tuning of these fluctuations by chemical substitution induces the observed magnetic order in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ .

In many helical magnetic systems such as  $\text{MnSi}$ <sup>42-44</sup> or  $\text{Cr}_{1/3}\text{NbSe}_2$ <sup>45,46</sup>, the helical magnetic order is induced by the Dzyaloshinskii-Moriya (DM) interaction<sup>47</sup> arising from the lack of crystalline inversion symmetry. Since  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  has a centro-symmetric crystal structure, the DM interaction is absent. In isostructural  $\text{EuCo}_2\text{As}_2$  where a large magnetic moment exists on the Eu site<sup>32</sup>, the mechanism for helimagnetism is likely distinct from that in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ . Here, a classical Heisenberg model with a frustrated nearest-neighbor (NN)  $J_1$  and next-nearest-neighbor (NNN)  $J_2$  between basal planes can produce helical order<sup>48,49</sup>. Such a mechanism of helical order for centro-symmetric materials has been proposed many years ago by incorporating exchange frustration<sup>50</sup>. However, there are difficulties in applying this model to  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ . First, the effective spin  $S$  derived from  $\mu_{eff} = g\sqrt{S(S+1)}$  is only about  $1/2$ , making the validity of classical Heisenberg model ( $S \rightarrow \infty$ ) questionable. Second, according to the theory, the helical arrangement has a  $q$  given by  $\cos(cq) = -J_1/4J_2$  in which  $c$  is the inter-layer distance. Therefore, the nearly  $90^\circ$  angle between magnetic moments in adjacent layers with  $q \sim \frac{\pi}{2c}$  leads to  $\cos cq \sim \cos(\pi/2) = 0$  and thus an almost vanishing NN exchange coupling  $J_1$  which appears to be unrealistic. Higher order exchange couplings such as  $J_3$  may help stabilize the helical state but the phase space<sup>51</sup> for a stable helix with a rotation of  $\sim \pi/2$  angle between adjacent spins is still limited. Third, the RKKY interaction may be responsible for the evolution of magnetism from  $\text{CaCo}_2\text{As}_2$  to  $\text{BaCo}_2\text{As}_2$ , since the different sizes of intercalated ions can tune the inter-layer Co-Co distance and thus the magnitude of exchange interactions. However, the origin of the helimagnetism along the  $c$  axis is still ambiguous because an unrealistically large  $k_F$  ( $\sim \frac{\pi}{c}$ ) is required to make  $J_1$  nearly zero via the spatial oscillation of the RKKY interaction.

On the other hand, quantum fluctuations in a paramagnet near a FM instability can make significant contributions to the free energy and stabilize unusual magnetic order<sup>2,5,6</sup>. In  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$ , the  $d_{x^2-y^2}$  band is flat along both the in-plane  $\Gamma - M$  and out-of-plane  $\Gamma - Z$

directions. The massive quantum particle-hole excitations can strongly affect the flat band dispersion at the mean-field level and, as a consequence, a helical magnetic order with certain momenta can be induced. However, the presence of flat band requires physics beyond the conventional itinerant spin density wave (SDW) theory with Fermi surfaces nesting, but may be a realization of the *quantum-order-by-disorder* mechanism.

In conclusion, we discovered a novel helical magnetic order in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  and established the phase diagram with systematic studies of the magnetic susceptibility. By combining neutron diffraction and ARPES experiments, we have established a close connection between the  $d_{x^2-y^2}$  flat band and the helical magnetic order. Based on these results, we suggest that the helical magnetic order in  $\text{Sr}(\text{Co}_{1-x}\text{Ni}_x)_2\text{As}_2$  is driven by quantum fluctuations and the system is likely in the vicinity of at least one quantum critical point.

Note added: Recently, a paper studying<sup>52</sup> on the same material as the present work was posted on arXiv. The main experimental results of the two studies are consistent with each other.

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