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Vocal Fold Analysis From High Speed Videoendoscopic Data

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VOCAL FOLD ANALYSIS FROM HIGH SPEED VIDEOENDOSCOPIC DATA

A Dissertation

Submitted to the Graduate Faculty of the Louisiana State University and Agricultural and Mechanical College in partial fulfillment of the requirements for the degree of Doctor of Philosophy

in

The Division of Electrical and Computer Engineering

by

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August 2014
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I would like to dedicate this dissertation to my parents, my husband, and my parents-in-law, for their continuous support and encouragement throughout my entire life.

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ABSTRACT

High speed videoendoscopy (HSV) of the larynx far surpasses the limits of videostroboscopy in evaluating the vocal fold vibratory behavior by providing much higher frame rate. HSV enables the visualization of vocal fold vibratory pattern within an actual glottic cycle. This very detailed information on vocal fold vibratory characteristics could provide valuable information for the assessment of vocal fold vibratory function in disordered voices and the treatments effects of the behavioral, medical and surgical treatment procedures. In this work, we aim at addressing the problem of classifying voice disorders with varying etiology by following four steps described shortly. Our methodology starts with glottis segmentation. Given a HSV data, the contour of the glottal opening area in each frame should be acquired. These contours record the vibration track of the vocal fold. After this, we obtain a reliable glottal axis that is necessary for getting certain vibratory features. The third step is the feature extraction on HSV data. In the last step, we complete the classification based on the features obtained from step 3.

In this study, we first propose a novel glottis segmentation method based on simplified dynamic programming, which proves to be efficient and accurate. In addition, we introduce a new approach for calculating the glottal axis. By comparing the proposed glottal axis determination methods (modified linear regression) against state-of-the-art techniques, we demonstrate that our technique is more reliable. After that, the concentration shifts to feature extraction and classification schemes. Eighteen different features are extracted and their discrimination is evaluated based on principal component analysis. Support vector machine and neural network are implemented to achieve the classification among three different types of vocal folds (normal vocal fold, unilateral vocal fold polyp, and unilateral vocal fold paralysis). The result demonstrates that the classification rates of four different tasks are all above 80%.
CHAPTER 1. INTRODUCTION

Verbal communication that relies on healthy voice is so important to people’s daily life, especially for the professional voice users as singers and teachers. However, the misuse/overuse of voice, the change in laryngeal structure and vocal folds may lead to voice disorders, which can affect the quality of people’s life significantly. Human voice is produced by the vibration of two vocal folds in larynx with help of the airflow from the lungs [1]. Therefore, the evaluation of vocal fold vibratory function has been considered an important component of clinical voice assessment protocol to help with the diagnosis of voice disorders, and plan appropriate treatment strategies (behavioral, surgical or medical) [2]-[3].

1.1 Why High Speed Videoendoscopy is Used

The clinical evaluation of vocal function at the presence of a voice disorder include both direct (laryngoscopy and videostroboscopy) and indirect methods (acoustic and aerodynamic) [4]. Compared with perceptual analysis and the quantitative approaches such as acoustic analysis, only the direct laryngeal imaging (e.g. videostroboscopy) allows determination of etiology of a voice disorder. Currently, videostroboscopy is a gold standard to assess vocal fold vibratory function in a clinic setting [5]-[6]. However, significant vibration details might be overlooked while using the videostroboscopy due to its low recording frame rate (e.g., around 30 frames/second) [7] in the presence of voice disorders that results in irregular vocal fold vibration or short phonation duration. In this situation, high speed videoendoscopy (HSV), with its significantly higher capturing frame rate of 2000 or higher addresses the limitations of videostroboscopy and, could be very helpful to investigate the vocal fold vibratory characteristics within a glottic cycle even the vibration is very irregular and short in duration [2][8]-[9]. Figure 1-1 illustrates the HSV data acquisition. The rigid endoscopy, attached to the high speed
camera, goes through the subject’s mouth and allows visualization of the laryngeal structures and true vocal folds. Then, the vocal fold vibration can be recorded by the camera while the subject produces /i/ sound. An example of a HSV frame can be found from Figure 1-1. This is the data collected from a normal voice. Figure 1-2 shows more examples by demonstrating HSV data from vocal fold vibratory pattern of normal vocal folds, vocal folds with polyp on the left vocal fold pre and post surgery. It can be seen that the view of vocal fold oscillation is very clear in each frame of HSV data. Thus, HSV allows determination of vibratory patterns within the actual glottic cycle along the entire length of the vocal folds in both regular and irregular voices, enabling objective quantification of vocal fold vibratory characteristics.

Substantial research is based on the high speed videoendoscopic data [2][5][7]. For reaching the quantitative analysis of HSV data, different methods are developed. Phonovibrogram (PVG) uses a 2-D plot to demonstrate the vocal fold vibration for the entire video [2]. To analyze the change of vibration along the whole video, videokymography selects vibration amplitude at certain position of vocal fold on each frame and then combine them together [10]. Besides, biomechanical model has also developed to fit the vocal fold vibration [11]. However, to investigate vocal fold function of voice disorders with varying etiology, the vibration characteristics for each type of voice disorders should be considered and analyzed. Therefore, in this work, to reach the goal of vocal fold analysis, we elaborate a series of studies to extract certain features to explore the vibration characteristics of different vocal folds in detail.

1.2 Dissertation Organization

To explore the correlation between the vocal fold vibratory characteristics and a voice disorder (e.g. vocal fold nodules, polyp, and vocal fold paralysis), many features have been investigated in literature [12]-[14]. For example, the vocal fold vibratory amplitude, the fundamental
frequency, the symmetry of left and right vocal fold, and the phase asymmetries are discussed in references [15]-[19]. All those features can be adopted to measure the irregularity of vocal fold vibratory characteristics during voice assessment [20]-[22]. Most of these features are related to the glottal opening area as indicated in Figure 1-1. In other words, to get those features, glottis segmentation is a necessary pre-processing step. Several glottis segmentation methods have been investigated in other research, such as region growing method and active contour method [23]-[25]. In this study, we develop our own glottis segmentation method, which achieves a good balance between efficiency and accuracy.

In addition, some HSV features that describe true vocal fold vibratory functions require the use of glottal axis, which is the projection of the median sagittal plane of the larynx onto the 2D endoscopic imagery (refers to Figure 1-1). For example, phonovibrogram (PVG), an image processing tool developed to analyze HSV data, uses the glottal axis to demonstrate the vocal vibratory patterns in normal voice and pathological voices caused by varying etiology (laryngeal nerve paralysis, functional voice disorder with vocal nodules) [26]. Besides, the glottal axis determination is also important to extract accurate symmetry features, which is one of the most significant measurements for evaluating the vocal fold function. There are two kinds of vocal fold asymmetry: left-right asymmetry and anterior-posterior asymmetry [27]-[28]. Furthermore, the biomechanical models for fitting the observed vocal fold oscillations [11][29] needs the information of glottal axis as well. Several glottal axis determination techniques have been used in earlier studies. Examples include the regression line and the extreme vocal fold endpoint [11][30]. However, the most reliable glottal axis determination technique is yet to be determined. In this study, we propose a new way to obtain the glottal axis and demonstrate its advantage in reliability over state-of-the-art strategies.
Vocal fold vibratory characteristics are very useful to evaluate the vocal fold function. Feature extraction based on HSV data could help to quantify the vocal fold vibratory characteristics and help to establish the relationship between features and voice disorders. Consequently, a reliable feature should be clinically useful to assess the vocal fold function. In this study, eighteen different features that describe the vocal fold vibratory symmetry and regularity have been extracted. Aiming at exploring the relationship of features and voice disorders, we investigate the classification among normal vocal folds and vocal folds pathologies with different etiologies based on the extracted features. Two classification approaches including support vector machine and neural network are applied to achieve the classification on three types of vocal folds (normal vocal fold, unilateral vocal fold polyp, and unilateral vocal fold paralysis).

To summarize, the main contributions of this research are as follows.

- We proposed a new glottis segmentation method based on simplified dynamic programming, which is proved to be both efficient and accurate to obtain the glottal area in each frame of a HSV data.
- We developed a new glottal axis determination technique and explore its capability to differentiate vocal fold of disordered voice from normal vocal fold by comparing with current used glottal axis determination methods.
- We developed several pathological specific features to represent vibration characteristics for each certain type of vocal fold. And then, the classification is achieved based on those features among different vocal folds.

The remaining of this dissertation is organized as follows. We present our exploration on glottis segmentation approach in chapter 2. Chapter 3 elaborates the glottal axis determination
technique and its analysis. In chapter 4, we demonstrate the feature extraction and classification on vocal fold with varying etiology. We finally summarize the studies and present potential works in chapter 5.

![Figure 1-1. An HSV frame obtained from the high speed videoendoscopy](image)

Figure 1-1. An HSV frame obtained from the high speed videoendoscopy

![Figure 1-2. Three different types of vocal folds ((a) normal vocal fold vibratory pattern, (b) vibratory pattern of vocal fold with polyp (pre-surgery), (c) vibratory pattern of vocal fold with polyp (post-surgery))](image)

Figure 1-2. Three different types of vocal folds ((a) normal vocal fold vibratory pattern, (b) vibratory pattern of vocal fold with polyp (pre-surgery), (c) vibratory pattern of vocal fold with polyp (post-surgery))
CHAPTER 2. GLOTTIS SEGMENTATION USING SIMPLIFIED DYNAMIC PROGRAMMING

2.1 Motivation

High speed videoendoscopy (HSV) is widely used for the assessment of vocal fold vibratory behavior in research settings [31]-[32]. However, due to the huge volume of HSV data (2000 frames/second or even higher), a quick and accurate segmentation of glottal opening is highly demanded for objective quantification and analysis of vocal fold vibratory characteristics.

Existing glottis segmentation methods can be divided into three categories. The first one is thresholding methods [33]-[36]. Taking advantage of the fact that pixel intensity in glottal opening are lower than those surrounding glottal opening, these methods choose a threshold to differentiate this intensities difference and achieve segmentation. The second one is the region growing method [23][37]-[38]. Generally, this method requires the manual selection of initial seed points in addition to the threshold selection. The glottis segmentation is reached by adding the adjacent pixels around the initial seed points if these pixels satisfy a homogeneity criterion. A proper homogeneity criterion is critical for accurate segmentation since under- or over-segmentation may easily happen. Lohscheller et al. [23] included manual intervention to obtain proper and flexible glottis segmentation. The last one is the active contour method [24]-[25][39]-[40]. Segmentation using the active contour method is very popular in medical image processing since the foreground and background of medical image is complex. Finding the boundary that minimizes cost function with interior and exterior energy term, the active contour method can produce precise segmentation results. However, active contour introduces much computation cost for searching the best segmentation result.
Referring to an HSV frame in Figure 1-1, our proposed algorithm first tracks the posterior and anterior endpoints of the glottal opening throughout the HSV data, and later extracts the left and right glottal edges in each frame to achieve segmentation. The endpoint tracking is based on the template matching technique. The glottal edge extraction is based on a simplified dynamic programming algorithm. It is obvious that generic edge detection algorithms, such as [41], are not suitable for this task because we have restricted situation where two edges (corresponding to left and right vocal folds) that go through the endpoints need to be extracted. As we will discuss in more detail, the glottal edge extraction problem is converted to a path finding problem.

There is a large volume of literature on path finding. For example, Fischler [42] found a path between a start point and an end point based on the F* algorithm, which adjusts the path array by traversing it based on cost function following two directions. Different types of cost functions, such as the Duda road operator [42] and Sobel-type gradient [42] are used. Other shortest path finding algorithms used in graph theory such as Dijkstra’s algorithm and Bellman-Ford algorithm can also be used to find the path [43]. However, these two algorithms find the shortest path form the single source to all the other vertexes in the graph. It may be time consuming by using these shortest finding algorithms on the glottal edge detection which only the path between two end points needs to be obtained. The A* algorithm, which finds the shortest path between a pair of node, achieve better performance on computation cost by using an cost function as heuristic estimate for the future path cost from the current node to the final goal [44]. Wan [45] implemented the shortest path finding algorithm by using minimum spanning tree and heap sorting to achieve the centerline extraction with computation cost of $O(N\log N)$; however, in our algorithm, the computation cost for getting the glottal edge is $O(N)$. Lie [46] integrated edge detection and dynamic programming to detect the skyline (a single lateral line) across an image. Specifically,
edge detection is applied on image first in their study, then dynamic programming is used to link edges based on certain cost criterion. However, we have stated that both glottal and non-glottal edge segments could be got by simply applying edge detection on HSV image. Those false segments can be very close to the real glottal edge, which brings difficulty on linking the real glottal edge segments.

In our study, line detection is accomplished by a simplified dynamic programming method, which is proved to be a both efficient and accurate segmentation approach.

2.2 Glottis Segmentation Based on Vocal Fold Edges

As shown in Figure 1-1, the glottal opening is bordered with the left and right vocal fold edges extending from a common posterior endpoint to a common anterior endpoint. The proposed segmentation method first finds the posterior and anterior endpoints in each frame of the HSV data to define the region of interest. It is possible that left and right vocal fold edges touch each other inside the glottal opening. To handle such cases, a closed portion determination step is applied to detect such regions. Finally, a dynamic programming based algorithm is employed to extract the left and right vocal fold edges that connect the two endpoints. Figure 2-1 illustrates the flowchart of the entire process.

Figure 2-1. Flow chart of glottis segmentation
2.2.1 Tracking of Posterior and Anterior Endpoints

The posterior and anterior endpoints are defined as the topmost and bottommost points of glottal area in an HSV image. Since vocal fold vibration occurs within the range from posterior to anterior endpoints along the vertical direction, these two endpoints determine the area of interest where the segmentation process will be carried out. The initial positions of the posterior and anterior endpoints are manually selected in the first maximum opening frame. The maximum opening frame is defined as the frame which has the largest glottal area within a cycle. The maximum opening frames are found based on the quick vibratory profile (QVP) [47] prior to computing the glottal area. There are two reasons for using the maximum opening frames to track the endpoints. First, two endpoints are always observable on maximum opening frame, which make the possibility for endpoints tracking; second, implementing endpoints tracking only on maximum opening frames can help to save the computation cost.

Once the endpoints are located in the first maximum opening frame, the endpoints are tracked over the duration of the analysis. The endpoints are assumed to be clearly visible throughout the analysis duration, and the movements of the endpoints are minimal from cycle to cycle. Given the initial positions of the endpoints, template matching technique [41] is used to track the endpoints on a maximum opening frame to the next. Figure 2-2 illustrates the way to get the endpoints for the second maximum opening frame by finding the most matched area of local region within the searching window. The endpoints of the frames between maximum opening frames are obtained by the linear interpolation. Figure 2-3 indicates the posterior and anterior endpoints in each frame within one vibration cycle.
2.2.2 Vocal Fold Edge Detection

This section presents the algorithm of detecting the left and right glottal edges between posterior and anterior endpoints in an HSV frame. Figure 2-4(b) illustrates the gradient curve of one horizontal line from the frame shown in Figure 2-4(a). The absolute gradient value of the pixels which locate on the edges is larger than that of other pixels in the same line. Therefore, the glottal edges are formed by the image pixels which maximizes (the left edge) or minimizes (the right edge) the cumulative horizontal gradient. Denoting the pixel intensity at the point \((x, y)\) by \(I(x, y)\), the horizontal gradient of the pixel is given by:

\[ I_y(x, y) = \frac{\partial I(x,y)}{\partial y} \] .......................... 2.1
Figure 2-4. Gradient curve of one horizontal line of an image. \( I_y \) is the gradient.

Since the left and right glottal edges correspond to the maximum and minimum gradient paths, the cost at a pixel are set to \( I_y(x, y) \) and \(-I_y(x, y)\) for searching right and left glottal edge, respectively.

We could observe that the glottal edge is formed with two smooth curves without any other very irregular curve segment between two endpoints. Therefore, given the region of interest defined by posterior endpoint \((x_p, y_p)\) and anterior endpoint \((x_A, y_A)\), the glottal edge detection problems can be stated as finding the optimal \(\{y_r(x)\}\) and \(\{y_l(x)\}\) for all \(x_p \leq x \leq x_A\), which respectively minimize the cost functions

\[
C_r = \sum_{x=x_p}^{x_A} I_y(x, y_r(x)) \tag{2.2}
\]

\[
C_l = \sum_{x=x_p}^{x_A} -I_y(x, y_l(x)) \tag{2.3}
\]

subject to the constraints

\[
|y_r(x) - y_r(x-1)| \leq 1 \tag{2.4}
\]

\[
|y_l(x) - y_l(x-1)| \leq 1 \tag{2.5}
\]

for all \(x_p \leq x \leq x_A\).
The minimizing solutions can be acquired with the simplified dynamic programming [48]. The algorithm first constructs cumulative energy function, \( E_r \) and \( E_l \), by traversing the individual pixel cost functions \( I_y(x, y) \) and \(-I_y(x, y)\), from the first row (which contains the posterior endpoint) to the last row (with the anterior endpoint). The \( xy \)-th elements of the energy functions are computed by

\[
E_r(x, y) = I_y(x, y) + \min (E_r(x - 1, y - 1), E_r(x - 1, y), E_r(x - 1, y + 1)) \quad 2.6
\]

\[
E_l(x, y) = -I_y(x, y) + \min (E_l(x - 1, y - 1), E_l(x - 1, y), E_l(x - 1, y + 1)) \quad 2.7
\]

with \( E_r \) and \( E_l \) are set to 0 outside the defined range of \( x_p \leq x \leq x_A \) and \( y \). The principle is illustrated in Figure 2-5. Each grid in right image of Figure 2-5 represents a pixel from the left image.

Figure 2-5. Illustration of obtaining the cumulative minimum energy function

After getting the cumulative minimum energy function, the glottal edges are obtained by back tracing the minimum value in each row of \( E_r \) and \( E_l \). Figure 2-6 shows an example of \( I_y \)-value, \( E_r \)-value and the traced right edge. The back tracing begins from the predetermined anterior endpoint \((x_A, y_A)\), and we denote the minimizing solutions as \( y^*_r(x) \) and \( y^*_l(x) \), which are the lateral coordinates of the back-traced vocal fold edges. The back traced most posterior points, \((x_p, y^*_r(x_p))\) and \((x_p, y^*_l(x_p))\), are usually close to the posterior endpoint \((x_p, y_p)\). The glottal
opening area is formed with the detected left and right vocal fold edges and a straight edge which connects the posterior points \((x_p, y_r(x_p))\) and \((x_p, y_l(x_p))\).

![Image](image.png)

Figure 2-6. Original image (left), its \(I_y\)-value (middle) and \(E_r\)-value (right).

Reflection, which is due to the illuminating light source(s), is unavoidable in HSV data acquisition. The gradient-based metric is sensitive to the (bright) reflection of the illuminating light source. With larger intensity value than its neighboring region, reflections near the vocal folds may deviate the optimal paths away from glottal edges. Therefore, the regularization term is included to the cost functions to improve the robustness. An effective regularization strategy to counter this potential issue is to penalize pixel’s intensity when it is not glottal edge pixel. Pixels outside and inside of the glottal opening will be penalized since they have higher and lower intensities than that of glottal edge pixels, respectively. Thus, the cost functions are modified to,

\[
C_r = \sum_{x=x_p}^{x_A} I_y(x, y_r(x)) + \alpha (I(x, y_r(x)) - I_0)^2  
\] 2.8

\[
C_l = \sum_{x=x_p}^{x_A} -I_y(x, y_l(x)) + \alpha (I(x, y_l(x)) - I_0)^2  
\] 2.9

subjected to the constraints \(|y_r(x) - y_r(x-1)| \leq 1\) and \(|y_l(x) - y_l(x-1)| \leq 1\) for all \(x_p \leq x \leq x_A\). The cost functions 2.8 and 2.9 include the regularization term where \(\alpha\) is a non-negative constant and \(I_0\) is the expected vocal fold edge intensity. \(I_0\) is acquired as follows: getting the maximum and minimum \(I_y(x, y)\) at each horizontal line between \(x_p \leq x \leq x_A\); then \(I_0\) is
the mean intensity of corresponding pixels obtained in last step. In this way, we force the path to go through the actual edge and avoid crossing the strong reflection edges.

2.2.3 Closed Portion Determination

The above algorithm performs well for an HSV frame, in which the vocal folds form a single glottal opening area. However, the procedure is more likely to fail if an HSV frame contains multiple glottal area segments due to partial closure of the glottis. Such condition is shown in Figure 2-7(a) in which the left and right edges touch each other between the markers \(d_1\) and \(d_2\). Where the two edges meet, the expected spikes in the horizontal gradient \(I_y\) are likely absent, causing the path finding algorithm to find incorrect edges in that part (as shown in Figure 2-7(b)).

A simple divide-and-conquer approach is employed to address this issue. The vocal fold edges are detected in each glottal open segment, and the edge endpoints in adjacent segments (e.g., \(d_1\) and \(d_2\) in Figure 2-7(a)) are then connected with a straight line. The corresponding segmentation result is shown in Figure 2-7(c).

![Figure 2-7](image_url)

Figure 2-7. (a) Glottal open and closed segments, (b) segmentation without using CPD, (c) segmentation using CPD.
To carry out this multi-segment approach, a preprocessing step, named as closed portion determination is necessary to determine the locations of the glottal closed segments. These segments are identified on the glottal axis,

\[
y_{axis}(x) = \frac{y_A - y_P}{x_A - x_P} (x - x_A) + y_A
\]

For \(x_P \leq x \leq x_A\) (shown as a dashed line in Figure 2-7(a)). Normally, the glottal axis is located inside of the glottal opening and goes through the whole opening. In a frame with multiple glottal open segments, we can find that the pixels on the glottal axis in an open segment have lower intensities (e.g., point \(b\) in Figure 2-7(a)) than the pixels on the glottal axis in a closed segment (e.g., point \(d_2\) in Figure 2-7(a)). For the \(x\)-th horizontal line, the ratio of the maximum intensity and the intensity of the pixel on the glottal axis is used to indicate the closed segment of glottal area,

\[
r(x) = \frac{\max_y I(x,y)}{I(x,y_{axis}(x))}
\]

Using this ratio, the closed segments are found by performing the following test on every horizontal line:

- Calculate the ratio \(r(x)\) for \(x_P \leq x \leq x_A\).
- If \(r(x) > r_t\), where \(r_t\) is a threshold, the \(x\)-th horizontal line belongs to the open segment.
- Otherwise, it belongs to the closed segment.

The threshold \(r_t\) cannot be the same value for every HSV data because the lighting condition, which is highly variable among HSV recordings, highly influences the threshold. Hence, the threshold is dynamically set for every HSV data. Given HSV data, the maximum and minimum opening frames within a cycle can be found based on the quick vibratory profile (QVP) [47] very
easily. Normally, the whole glottal area or the most of glottal area is fully open in maximum opening frame; while it is closed in minimum opening frame. Therefore we randomly choose five maximum and minimum opening frame, and calculate the average value of \( r(x) \) for open and closed segments respectively, denoted by \( r_{\text{open}} \) and \( r_{\text{closed}} \). The threshold \( r_t \) is chosen from the range of \([r_{\text{closed}}, r_{\text{open}}]\) by:

\[
r_t = r_{\text{closed}} + \gamma (r_{\text{open}} - r_{\text{closed}})
\]

where \( 0 < \gamma < 1 \), and \( \gamma = 0.2 \) is used in this study.

### 2.3 Results and Discussion

#### 2.3.1 Endpoints Tracking

To examine the effectiveness of endpoints tracking method, the endpoints of four randomly selected HSV recordings with length of 500 frames are tracked. The tracked endpoint locations are validated against manually selected endpoints at each frame. Note that the endpoints of some intra frames between each two maximum opening frames are invisible, therefore, only the endpoints of maximum opening frames are manually picked; while those of the intra frames are obtained via interpolation. To assess the accuracy of endpoints tracking, we compute the mean distance between manually selected endpoints and tracked endpoints and show them in Table 2-1. The mean distance is the mean value of the distance between two posterior endpoints and the distance between two anterior endpoints for those 500 frames. As can be seen from Table 2-1, the tracking result is accurate with largest difference of 1.71 pixels averaged on 500 frames vibration. Figure 2-8 gives the illustration of the comparison between manually selected endpoints and tracked endpoints at the 500th frame of HSV-4 in Table 2-1.
Table 2-1. Posterior and anterior endpoints tracking error

<table>
<thead>
<tr>
<th>HSV recordings</th>
<th>HSV-1</th>
<th>HSV-2</th>
<th>HSV-3</th>
<th>HSV-4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean Distance</td>
<td>0.61</td>
<td>0.93</td>
<td>1.35</td>
<td>1.71</td>
</tr>
</tbody>
</table>

Figure 2-8. (a) Manually selected endpoints at the 500th frame; (b) automatically tracked endpoints at the 500th frame.

2.3.2 Effect of the Regularization Term

Figure 2-9(a) shows the glottis segmentation result which is affected by the strong reflection. With high cost value, the reflection leads to a faulty edge path both for the left and right vocal fold. Figure 2-9(b) to Figure 2-9(d) illustrates the glottal edge extraction after adding the regularization term to the cost function. The regularized cost function successfully forces the minimum gradient path to follow the glottal edge and to ignore the edge of the nearby reflection. By taking different $\alpha$ value, the segmentation results are different. Figure 2-9(b) still demonstrates some false glottal edge since the $\alpha$ value is too small in this case. When $\alpha$ value is increased to a proper value, the segmentation demonstrates good performance in Figure 2-9(c) and Figure 2-9(d). To search the optimal $\alpha$ value, L-curve method has been used [49]. Based on this study, we get the optimal $\alpha$ as 0.02, which is shown in Figure 2-10.
2.3.3 Glottis Segmentation

Figure 2-11 gives the glottis segmentation result of a HSV data by using the \( \alpha \) value with 0.02. The glottal edge extraction is correct in every frame and not affected by any reflection. Next, the effectiveness of the proposed method is compared to two other segmentation methods. The first one is the fixed-threshold method, which acquires the threshold between foreground and background of image based on the histogram [41]. The second alternate method is the active contour method without edges [50].
Figure 2-12 shows the segmentation results between the fixed-threshold, the active contour method and the proposed method. Figure 2-12(a) indicates the segmentation result based on threshold value as 40. The over-segmentation is shown on the first frame; however, with the same threshold, the under-segmentation, also appears on the third frame. In other words, for the fixed-threshold, it is difficult to find an optimal threshold value that could work well for all the frames within a HSV data. Next, the glottis segmentation results of the active contour method and the proposed method are shown in Figure 2-12(b) and Figure 2-12(c). Although both of them give good and very similar glottal edge in each frame, the proposed method surpasses the active contour by spending less computation time. The proposed method takes 0.04s to process one frame, while the active contour needs 3.11s, with implementation on Matlab. Furthermore, the segmentation on the closed portion of glottal area can be effectively detected with our proposed method, while it may be overlooked when other segmentation schemes are adopted.

Figure 2-11. Glottis segmentation using the regularization term with $\alpha=0.02$. 
2.4 Conclusions

In this study, a glottis segmentation method based on simplified dynamic programming is introduced. The proposed method starts with the pre-processing step of posterior and anterior endpoints tracking and closed portion determination, which are crucial for the remaining segmentation procedure. Then, the simplified dynamic programming is used to accurately follow the paths of glottal edges by employing the horizontal gradient based cost functions. The proposed method is compared to two other commonly used methods: the fixed-threshold segmentation and the active contour algorithm. The proposed method is shown to have the best combination of efficiency and accuracy among the three methods.

Figure 2-12. Comparison of glottis segmentation among (a) the fixed-threshold, (b) the active contour method and (c) the proposed method.
CHAPTER 3. GLOTTAL AXIS DETERMINATION TECHNIQUES

3.1 Background

We have stated that a key step in computing quantitative vocal fold vibratory characteristics is glottal axis determination. Obtaining reliably certain HSV features hinges on consistent and dependable determination of glottal axis both within each HSV data and across different HSV data. The most reliable determination method would be to determine the axis manually on frame by frame or glottic cycle by cycle basis. However, for practical reasons, due to the vast HSV data generated, such manual operation is not feasible, and the axis determination has to be automated. Therefore, an accurate and automatic glottal axis determination technique is a critical requirement in analyses of objective axes-based HSV features.

The existing automatic glottal axis determination methods can be classified into two categories: the anterior-posterior extreme glottal area points based method and linear regression line based method. The first method detects the glottal axis by connecting the most posterior and anterior points within glottal area [11][27][29][51]. One explicit approach to determine the most anterior and posterior points of glottal area is to get the two points which are the vertical extremes of the segmented glottis pixels of vocal fold image [15]. The drawback of this method is that the positions of those two extreme points on distinct frames can vary greatly due to the glottis size. To alleviate this potential problem, Wittenberg in [15] calculated the average values of those two positions over several consecutive frames in a video. However, the use of the posterior extreme point may create problem when arytenoids fold posteriorly during phonation. The other automatic axis determination method is based on linear regression. In this strategy, the glottal axis is defined by the linear regression line of the glottal area pixels [2][23]-[24][30] or of the midpoints of the glottal edges [28].
Considering that some disordered voice with irregular vocal fold shape may lead to the difficulty in finding glottal axis, we propose to integrate the most anterior glottal edge point into linear regression to find the glottal axis, since the most anterior glottal edge point is stable and visible in HSV data. Besides, in this study, we also introduce the principal component analysis (PCA) to determine the glottal axis to make the comparison. In addition, this study presents the performances of the automatic glottal axis determination techniques (both the proposed and existing techniques) in differentiating normal vocal fold vibratory patterns from the vibratory pattern of vocal folds with polyp (pre-surgery). The glottal axis based features are computed and statistically analyzed for each automatic glottal axis determination technique individually.

3.2 Methodology

3.2.1 Subject and HSV Data Acquisition

The study data includes HSV recordings of 13 subjects with vocal fold polyp (both pre- and post-surgery) and 20 subjects with normal vocal fold (10 males and 10 females). All HSV data used in these studies are recorded at 2000 frames per second with KayPENTAX HSV system (Model 9700, Montvale, NJ). Each frame of HSV data is a black-white image, 120 pixels wide by 256 pixels high. For every recording, a segment of 2000 frames is selected from sustained phonation for the study.

3.2.2 Glottal Axis Determination (GAD) Techniques

All the glottal axis determination techniques presented in this study are based on the locations of the glottal edge pixels in each HSV frame. The following mathematical notations are introduced for the proceeding section describing the glottal axis determination techniques. Assuming glottal edge pixels are found for an HSV frame, the edge pixel locations are defined by 

\[ p_k = [x_k \ y_k]^T, \ k = 1, 2, \ldots, K, \]  

where \( x_k \in \{0, 1, \ldots, M - 1\} \) and \( y_k \in \{0, 1, \ldots, N - 1\} \).
represent the vertical and horizontal pixel indices, respectively. The origin of the coordinate is located at the upper left corner of the frame. The set of edge pixels are defined as $\mathcal{P} = \{p_1, p_2, \ldots, p_K\}$. Also, the coordinate points of the edge pixels are given by two vectors: $x = [x_1 \ x_2 \ \ldots \ x_K]^T$ for the $x$-coordinates and $y = [y_1 \ y_2 \ \ldots \ y_K]^T$ for the $y$-coordinates.

The glottal axis is defined as the line between the most posterior and anterior of glottal area. In detail, the location of posterior glottal axis is determined by ensuring the line is passed between the mid-point of vocal processes of the right and left true vocal folds. The location of anterior glottal axis is defined as the most anterior point of the glottal area. However, without any manual guidance, it is hard to correctly and automatically extract the mid-point between vocal processes in each frame of HSV data. Further, the substitution of posteriorly extreme point as the mid-point may create problem when arytenoids fold posteriorly during phonation. Therefore, five automatic axis determination techniques are evaluated in this study, including extreme point technique (EP), linear regression technique (REG), the modified linear regression technique (MREG), principal component analysis technique (PCA), and the modified PCA technique (MPCA). The details of each method are given in the subsections.

In each HSV frame, the glottal axis is defined as a function of the vertical axis $x$. For the $i$-th frame, it is given by:

$$y = m_i x + b_i.$$  \hspace{1cm} 3.1

where $m_i$ is the slope and $b_i$ is the $y$-intercept.

With the assumption that the glottal axis hardly change within one vibration cycle, each GAD technique is applied only on the maximum opening frame of each vibration cycle to get
their axes. Then, linear interpolation is utilized on the axis of maximum opening frames to acquire the axes of the rest frames.

- **Extreme Points (EP) Technique**

  For the maximum opening frame in each vibration cycle, the glottal axis is obtained by connecting the two extreme points along vertical direction. Figure 3-1 gives the illustration of this method. Suppose the extreme points are \( p_{e1} = [x_{e1} \ y_{e1}]^T \in \mathcal{P} \) and \( p_{e2} = [x_{e2} \ y_{e2}]^T \in \mathcal{P} \) in a frame. Then, the slope and \( y \)-intercept of the glottal axis are calculated by

\[
m_{EP} = \frac{y_{e1} - y_{e2}}{x_{e1} - x_{e2}} \quad \cdots \quad 3.2
\]

\[
b_{EP} = y_{e1} - \frac{y_{e1} - y_{e2}}{x_{e1} - x_{e2}} x_{e1} \quad \cdots \quad 3.3
\]

![Figure 3-1. Axis determination method-EP](image)

- **Linear Regression (REG) Technique**

  The glottal axis for each maximum opening frame is given by the linear regression line of glottal edge pixels. The axis is defined by the slope \( m_{REG} \) and the \( y \)-intercept, \( b_{REG} \), which minimize the least square cost functions:

\[
J(m, b) = \| y - (mx + b) \|^2 \quad \cdots \quad 3.4
\]
\{m_{REG}, b_{REG}\} = \arg \min_{m,b} J(m, b)………………………………………………………………………………… 3.5

The \(m_{REG}\) and \(b_{REG}\) can be found from Figure 3-2.

![Axis determination method-REG](image)

Figure 3-2. Axis determination method-REG

- Modified Linear Regression (MREG) Technique

In a laryngeal image, the most anterior glottal area point, \(p_e2\) (i.e., the extreme point of the glottal area at the bottom of the image) is consistently visible, and its pointy feature makes it an easier feature to identify. The MREG method is a hybrid of the EP and REG methods by utilizing the most anterior point and a least squares slope estimate.

The most anterior point is obtained from the vertically lowest pixel \(p_e2\) of \(\mathcal{P}\). This point may be subject to potential inaccuracy resulted from noise. To reduce the effect of noise, the position of the most anterior point, \(p_a = [x_a \ y_a]^T\), is defined as the average of the edge pixels within a three-pixel by three-pixel window centered at \(p_e2\). With \(p_a\), the glottal axis is expressed by

\[y = m(x - x_a) + y_a……………………………………………………………………………………………… 3.6\]

Accordingly, the slope, \(m_{MREG}\), is determined by minimizing the least square cost function:

\[J_{MREG}(m) = \|y - (m(x - x_a) + y_a)\|^2………………………………………………………………………… 3.7\]
Finally, the $y$-intercept is obtained by

$$b_{MREG} = y_a - x_a m_{MREG}.$$  

The illustration of $p_a$, $m_{MREG}$ and $b_{MREG}$ can be found from Figure 3-3.

![Figure 3-3. Axis determination method-MREG](image)

- Principal Component Analysis (PCA) Technique

Principal Component Analysis (PCA) is a mathematical procedure that can convert a set of observations of possibly correlated variables into a set of observations of uncorrelated variables, which are called principal components, without losing significant information [52]. The number of principal components is less than or equal to the number of original variables. Therefore, PCA is mainly used for dimensionality decrease of high-dimensional data. With this idea, the data points of two dimensions can be easily decreased into one dimension by applying PCA. In other words, the two dimensionality dataset can be transferred to a line, which conserves most of information of the original dataset. Corresponding to glottal axis determination, for a frame, all points on the vocal fold edge can be regarded as the original data points. The line obtained from applying PCA on edge pixels could be considered as the glottal axis.
Based on the PCA method, the glottal axis is expected to be in the direction of the first principal component. From Figure 3-4, the first principal component is represented by the eigenvector \( \mathbf{e}_1 \), which corresponds to the largest eigenvalue, of the covariance estimate matrix,

\[
C = (\mathbf{P} - \bar{\mathbf{P}})(\mathbf{P} - \bar{\mathbf{P}})^T
\]

where \( \mathbf{P} = [x\ y]^T \) and \( \bar{\mathbf{P}} \) is the centroid (the average coordinate) of all the glottal edge pixels. Then, all glottal edge pixels can be projected to the direction of the first principal component by

\[
\mathbf{P}' = \bar{\mathbf{P}} + \mathbf{e}_1^T (\mathbf{P} - \bar{\mathbf{P}}) \mathbf{e}_1
\]

Finally, the glottal axis, defined by \( m_{\text{PCA}} \) and \( b_{\text{PCA}} \), can be easily calculated by choosing any two points from \( \mathbf{P}' \).

![Figure 3-4. Axis determination method-PCA](image)

- **Modified Principal Component Analysis (MPCA) Technique**

Although the PCA method works well for vocal folds, which have regular shape, it could not correctly identify the axis for vocal fold with irregular shape, such as vocal fold with polyp. To alleviate this problem, a hybrid approach, similar to the one used in the MREG method, is employed to improve the accuracy of a PCA-based GAD method. The MPCA method also utilizes the most anterior glottal area point from the MREG method.
Since the aim is to find the principal component (direction) which goes through the most anterior glottal area point, the center point $\bar{p}$ in (3.9) is replaced with the most anterior point $p_a$, resulting in an augmented covariance matrix:

$$\tilde{C} = (P - p_a)(P - p_a)^T$$

Then, the eigenvector $\tilde{e}_1$ which corresponds to the largest eigenvalue of $\tilde{C}$ is obtained. The illustration of $\tilde{e}_1$ can be found from Figure 3-5. Thus, all glottal edge pixels can be projected to the direction of the first principal component by

$$\tilde{P}' = p_a + \tilde{e}_1^T (P - p_a)$$

Again, the $m_{MPCA}$ and $b_{MPCA}$, can also be computed by choosing any two points from $\tilde{P}'$.

![Figure 3-5. Axis determination method-MPCA](image)

3.2.3 Features Depending on Glottal Axis

Following features are investigated to evaluate their sensitivities to different axis determination methods: the symmetry between right and left vocal fold amplitudes, asymmetry along the glottal length, asymmetry on the glottal area, and symmetries along horizontal and vertical direction.
The first step in the feature extraction is the motion compensation. HSV data are inevitably affected by the motion of the endoscope. Motion compensation guarantees to place the glottal area at the same position and in the same orientation for every frame. The motion compensation is achieved by the spatial transformation of the video frames. Each point $\mathbf{p} = [x \ y]^T$ in $x - y$ coordinate has been transferred to $u - v$ coordinate,

$$
\begin{bmatrix}
u \\
v \\
1
\end{bmatrix} =
\begin{bmatrix}
cos \theta_k & \sin \theta_k & 0 \\
-\sin \theta_k & \cos \theta_k & 0 \\
\bar{p}_x & \bar{p}_y & 1
\end{bmatrix}
\begin{bmatrix}
x \\
y \\
1
\end{bmatrix}
$$

where $\theta_k = \arctan m_k$ for frame $k$, $\bar{p}_x$ and $\bar{p}_y$ are the $x - y$ coordinate of centroid $\bar{p}$. In the $u - v$ coordinate, the most posterior pixel is located at $(u_1, 0)$ and the most anterior pixel is located at $(u_2, 0)$. The spatial transformation on one frame is illustrated in Figure 3-6. All the features are calculated in the $u - v$ coordinate.

![Figure 3-6. Spatial transformation (x and y are the original coordinate, u and v are the transformed coordinates, $\bar{p}$ is the centroid)](image)

Given a glottal axis, the glottal contour can be divided into left and right glottal edges for each frame in the HSV data. The glottal edge pixels with positive $v$-value belong to the left vocal fold edge, and the glottal edge pixels with negative $v$-value are the right vocal fold edge. Hence,
the glottal edges are represented by the \( v \)-coordinate values of the left and right glottal edge pixels, denoted by \( e_l(u) \) and \( e_r(u) \), respectively.

- Symmetry between right and left vocal fold amplitudes

For each frame, \(|e_l(u)|\) and \(|e_r(u)|\) are also represent the left and right amplitude values from glottal axis to the glottal edges at each vertical point (along the \( u \) axis), which is shown in Figure 3-7.

If the left and right edges are perfectly symmetrical about the glottal axis, \(|e_l(u)| = |e_r(u)|\) for \( u = u_1, u_1 + 1, \ldots, u_2 \). To assess the overall symmetry of the edges about the glottal axis, the difference of the distances is accumulated. The amplitude symmetry is defined as follows:

\[
S = \frac{\sum_{u=u_1}^{u_2} |e_r(u) + e_l(u)|}{A} \tag{3.14}
\]

The sum of the differences is normalized by the glottal area,

\[
A = \sum_{u=u_1}^{u_2} |e_l(u) - e_r(u)| \tag{3.15}
\]

to make the feature comparable among recordings. The range of this feature is from zero to infinite, and zero indicates the perfect symmetry.

Figure 3-7. The distances from glottal axis to left and right glottal edge, (a) is the normal vocal fold and (b) is the vocal fold with polyp (\( u=\)vertical coordinate, \(-e_r(u)=\)right vocal fold amplitude, \( e_l(u)=\)left vocal fold amplitude)
Asymmetry along the glottal length

Asymmetry in length $A_l$ describes the symmetry attribute along the glottal length,

$$A_l = \frac{m_c}{m}$$ \hspace{1cm} 3.16

where $m_c = \sum_{u=u_1}^{u_2} e_l(u) < 0$ or $e_r(u) > 0$ is the length of the part of vocal fold which crosses the glottal axis as illustrated in Figure 3-8(a), and $m = u_2 - u_1$ is the total length of glottal opening. The range of this feature is from zero to one. The smaller the value, the better the symmetry in length is.

Asymmetry on the glottal area

Asymmetry in area $A_a$ represents the symmetry attribute for glottal area,

$$A_a = \frac{A_c}{A}$$ \hspace{1cm} 3.17

where $A_c = A_l + A_r$, $A_l = \sum_{u=u_1}^{u_2} e_l(u)$, when $e_l(u) < 0$; and $A_r = \sum_{u=u_1}^{u_2} e_r(u)$, when $e_r(u) > 0$ is the area of glottal opening which crosses the glottal axis as illustrated in Figure 3-8(b), and $A$ is the area of glottal opening. This feature takes values from zero to one. The smaller the value, the better the symmetry in area is.

Figure 3-8. Asymmetry along the glottal length and asymmetry on glottal area ($m_c$=the length of the part of vocal fold which crosses the glottal axis, $m$=the total length of glottal opening, $A_c$=the area of glottal opening which crosses the glottal axis, $A$=the area of glottal opening)
• Symmetries along horizontal and vertical direction

The last pair of features—symmetries along horizontal ($S_h$) and vertical ($S_v$) directions—are based on the glottal area’s centroid $\bar{p}$. First, the horizontal line $l_h$ and vertical line $l_v$ which cross the centroid are obtained. Then, the distances from the centroid to the four intersected points resulted from the intersection of $l_h$, $l_v$ and glottal edge have been determined. Two features including $S_v$ and $S_h$ have been calculated based on $l_1$, $l_2$, $l_3$ and $l_4$, which are shown in Figure 3-9. In ideal case, the distance $l_1$ and $l_2$ in Figure 3-9 should be the same, and $l_3$ and $l_4$ should also be the same. Therefore, the values of $S_v$ and $S_h$ should be closed to zero for vocal fold with normal voice; however, when comes to vocal fold with polyp, the difference between $l_1$ and $l_2$, $l_3$ and $l_4$ will increase, which, of course, lead to the increase of $S_v$ and $S_h$. $S_v$ and $S_h$ can be acquired by following equations.

$$S_v = \frac{|l_1-l_2|}{l_1+l_2} \tag{3.18}$$

$$S_h = \frac{|l_3-l_4|}{l_3+l_4} \tag{3.19}$$

Figure 3-9. Distances from centroid to other four extreme points ($l_1$ and $l_2$, $l_3$ and $l_4$ are the vertical and horizontal distance from centroid to glottal edge)
3.3 Analysis

3.3.1 Accuracy Analysis

To evaluate the accuracy of automatic determination technique, the glottal axis obtained from each GAD technique is compared with the axis selected by a speech language pathologist (SLP) who has an extensive experience in looking at the endoscopic images of vocal folds. We select 10 vibration cycles from each HSV data and got their glottal axes, which obtained by using six GAD techniques (five automatic and one manual). Then, the mean square error between manual selected glottal axis and each automatic selected axis has been calculated. For one frames of HSV data, given its manually selected glottal axis with slope and intercept as $m_m$ and $b_m$ and automatic glottal axis with $m_a$ and $b_a$. The mean square error will be computed as follows:

$$e = \frac{\sum_{x=x_{e1}}^{x_{e2}} (m_m x + b_m - m_a x - b_a)^2}{x_{e2} - x_{e1}}$$

The mean square error is calculated for every frame within the 10 vibration cycles selected before and the average value is set as the final mean square error for one automatic GAD technique. The assumption is that the smaller the mean square error between axis from manual selection and automatic determination, the more accurate the GAD technique is.

3.3.2 Glottal Axes’ Capability to Differentiate Vocal Fold Vibratory Pattern of Normal and Disordered Voices

In this study, HSV data from 20 subjects with normal vocal fold (10 males and 10 females), and 13 subjects with vocal fold polyp (pre- and post-surgery) have been investigated. First, for each HSV data, 10 vibration cycles from its sustained phonation have been randomly selected. Then all five GAD techniques are applied on those selected cycles. For one GAD technique, the glottal axes of the selected vibration cycles could be obtained and all the symmetry features can
be calculated based on those glottal axes. Only maximum opening frame of each cycle is used while computing the symmetry features. Finally, the average value among those 10 maximum opening frames is computed and set as the final value for each feature of every HSV data. The same feature extraction has been done for the other four GAD techniques.

Consequently, five groups of symmetry features corresponding to five GAD techniques are acquired. Each group includes features extracted from three vibratory patterns of vocal folds (normal vocal fold, vocal folds with polyp of pre- and post-surgery). The five GAD techniques’ capability for differentiating the vocal fold vibratory pattern of normal and disordered voices are compared based on these symmetry features.

The statistical analysis of two-way ANOVA with significant level of 0.05 has been used to identify the features’ stability across different GAD techniques.

The statistical analysis of MANOVA with significant level of 0.05 has been adopted in comparison between normal vocal fold vibratory patterns and the vibratory pattern of vocal folds with polyp (pre-surgery). In addition to \( p \)-value, MANOVA analysis also provides a parameter of group mean distance (\( \text{gmdist} \)) between two groups. In this study, \( \text{gmdist} \) is adopted to represent glottal axis ability to differentiate different vocal folds.

### 3.4 Results

3.4.1 Results on Accuracy Analysis

The result of the mean square error for each GAD technique is shown in Table 3-1. It can be seen that the modified linear regression (MREG) technique gives the best performance on normal vocal fold vibratory patterns, as well as the vibratory pattern of vocal folds with polyp (post-surgery). MPCA shows the most accuracy on the vibratory pattern of vocal fold with polyp (pre-
surgery). After integrating the most anterior point, both the MREG and MPCA demonstrate better accuracy than original REG and PCA, respectively. In addition, as we expected, the GAD technique demonstrates the highest accuracy on normal vocal fold vibratory patterns, compared with the vocal folds with polyp. Not-surprisingly, the accuracy of the glottal axis on post-surgery vocal fold is higher than that of the pre-surgery vocal fold, since the shapes of the pre-surgery vocal folds are more irregular than that of the post-surgery vocal fold.

Table 3-1. Mean square error between the subjective and objective glottal axis determination techniques

<table>
<thead>
<tr>
<th>GAD techniques</th>
<th>Normal Vocal Folds</th>
<th>Pre-Surgery Vocal Folds</th>
<th>Post-Surgery Vocal Folds</th>
</tr>
</thead>
<tbody>
<tr>
<td>Extreme Points (EP)</td>
<td>3.48</td>
<td>12.12</td>
<td>4.48</td>
</tr>
<tr>
<td>Linear Regression (REG)</td>
<td>1.56</td>
<td>16.59</td>
<td>4.68</td>
</tr>
<tr>
<td>Principal Component Analysis (PCA)</td>
<td>1.50</td>
<td>15.00</td>
<td>3.67</td>
</tr>
<tr>
<td>Modified Linear Regression (MREG)</td>
<td>1.39</td>
<td>12.31</td>
<td>3.04</td>
</tr>
<tr>
<td>Modified Principal Component Analysis (MPCA)</td>
<td>1.47</td>
<td>12.17</td>
<td>3.06</td>
</tr>
</tbody>
</table>

3.4.2 Results on Glottal Axes’ Capability to Differentiate Vocal Fold Vibratory Pattern of Normal and Disordered Voices

Table 3-2 shows the result of features’ $p$-values for two elements between normal vocal fold vibratory patterns and the vibratory pattern of vocal folds with polyp (pre-surgery) based on two-way ANOVA. All the features have high GAD $p$-values, which indicate that these features are not affected by different GAD techniques. In addition, all the features’ voice $p$-values with less than 0.01 indicates that each feature is significantly different between normal vocal fold vibratory patterns and the vibratory pattern of vocal folds with polyp (pre-surgery).
Among three vibratory patterns in this study, vibratory pattern of vocal folds with polyp (post-surgery) is a critical one. Even though they look very similar to normal vocal folds, the healing process of vocal folds will vary between the individuals and this will influence the vocal fold vibratory characteristics. Therefore, only vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery) are considered to be the clean datasets. Consequently, the comparison between vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery) is taken to evaluate the discriminative function of each GAD technique. With the result of MANOVA analysis, the \( g_{m\text{dist}} \) gives quantification of the discriminative ability for each GAD techniques. The larger the \( g_{m\text{dist}} \), the stronger the GAD’s ability to differentiate vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery) is. The results of each GAD technique’s ability to differentiate these two vibratory patterns are shown in Table 3-3.

### Table 3-2. Two-way ANOVA for normal vocal fold and vocal fold with polyp (pre-surgery) 
(GAD=glottal axis determination, \( S \)=symmetry, \( A_l \)=asymmetry along glottal length, \( A_a \)=asymmetry on glottal area, \( S_v \)=symmetry in vertical direction, \( S_h \)=symmetry in horizontal direction)

<table>
<thead>
<tr>
<th>Feature</th>
<th>GAD ( p )-value</th>
<th>Voice ( p )-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( S )</td>
<td>0.72</td>
<td>&lt;0.01</td>
</tr>
<tr>
<td>( A_l )</td>
<td>0.99</td>
<td>&lt;0.01</td>
</tr>
<tr>
<td>( A_a )</td>
<td>0.99</td>
<td>&lt;0.01</td>
</tr>
<tr>
<td>( S_v )</td>
<td>0.89</td>
<td>&lt;0.01</td>
</tr>
<tr>
<td>( S_h )</td>
<td>0.99</td>
<td>&lt;0.01</td>
</tr>
</tbody>
</table>

### Table 3-3. MANOVA analysis based on automatic glottal axes (GAD= glottal axis determination, EP=extreme point, REG=linear regression, PCA=principal component analysis, MREG=the modified linear regression, MPCA=the modified PCA, \( g_{m\text{dist}} \)=group mean distance)

<table>
<thead>
<tr>
<th>GAD techniques</th>
<th>( p )-value</th>
<th>( g_{m\text{dist}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>EP</td>
<td>0.04</td>
<td>1.93</td>
</tr>
<tr>
<td>REG</td>
<td>0.01</td>
<td>2.55</td>
</tr>
<tr>
<td>PCA</td>
<td>0.02</td>
<td>2.43</td>
</tr>
<tr>
<td>MREG</td>
<td>&lt;0.01</td>
<td>3.97</td>
</tr>
<tr>
<td>MPCA</td>
<td>&lt;0.01</td>
<td>3.95</td>
</tr>
</tbody>
</table>
3.5 Discussions

The main goal of this study is to find the best glottal axis determination technique. To reach this goal, two evaluation methods are conducted. First we identify and modified five GAD techniques and compared them to subjective determination of glottal axis. It can be found from Table 3-1 that the MREG give the best accuracy on glottal axis detection since it has the smallest error when comparing to the subjective determination result. Second, we develop symmetry features which are dependent on the use of the glottal axis and determine performances of each GAD techniques in differentiating vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery) using these symmetry features. Based on Table 3-3, we can also find that the MREG still demonstrates the best performances with the largest $gmdist$ value, which indicates that MREG makes the largest separation between vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery).

Another goal of this study is to determine if the glottal axis dependent variables such as symmetry features of true vocal fold vibratory patterns are affected by the implementation of different GAD techniques or not. The symmetry features, including the symmetry between right and left vocal fold amplitudes, asymmetry along the glottal length, asymmetry on the glottal area, and symmetries along horizontal and vertical direction, can be affected by two elements in this study. One is different GAD techniques, and the other is the presence or absence of a polyp on vocal fold. Reliable use of symmetry features will depend upon, first their ability to differentiate between true vocal fold with and without polyp and second, not being affected by different GAD techniques. A two-way ANOVA is demonstrated (Table 3-2) that all the symmetry features are not affected by different GAD techniques (with GAD’s $p$-values are larger than 0.05) and could
differentiate vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery) (with voice’s $p$-values are smaller than 0.05).

In addition to $gmdist$, MANOVA analysis also provides canonical variable, which is a linear combination of the mean-centered original features, using coefficients from the eigenvector matrix. This information can be used to demonstrate visualization details on differentiation of vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery). The distribution of the HSV data for these two vibratory patterns following the first two canonical variables based on MREG and EP are shown in Figure 3-10 and Figure 3-11. Corresponding to the result shown in Table 3-3, MREG with the largest $gmdist$ gives a very clear division on these two vibratory patterns; on the contrary, EP with the smallest $gmdist$ shows a poor ability to differentiate these two vibratory patterns. In addition, Figure 3-12 and Figure 3-13 demonstrate the distribution of vibratory patterns of “pre- vs. post- surgery” and “normal vs. post-surgery” vocal fold, respectively. Compared to “normal vs. pre-surgery”, there is more overlap between vibratory patterns of pre- and post-surgery vocal fold. The distribution of vibratory patterns of normal and post-surgery vocal fold has the largest overlap among these three comparisons. From clinical perspective, the overlap between the vibratory patterns of pre and post-surgery vocal fold may indicate the different level of healing of vocal folds in individuals with varying degree of polyp size and type. The more desired overlap between the vibratory patterns of normal and post-surgery vocal fold indicates the vibratory patterns of vocal folds with polyp reaching to more normal vocal fold vibratory patterns found in normal voices after surgery.

In addition, the GAD technique of MREG demonstrated the best performance in differentiating the vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery) in this study with $gmdist$ of 3.97. The MPCA, which has very close mean square error and $gmdist$
with MREG in Table 3-1 and Table 3-3, also shows a very good performance. Both of these two methods take the most anterior glottal area point into account while finding glottal axis. Therefore, it is significant to include the anterior information while calculating the glottal axis.

There are limitations to this study, the subjects of normal vocal folds and vocal folds with polyp are not age and gender matched and effects of these variables should be investigated in future studies. In addition, the vibratory pattern of vocal folds with polyp (pre-surgery) group did not have identical polyp size, place and location which may have contributed to “pre- vs. post-surgery” and “normal vs. pre-surgery” vocal fold vibratory pattern separation.

Figure 3-10. Distribution of normal and pre-surgery data points based on the modified linear regression technique (MREG) ($gm\text{dist}$=group mean distance, $c_1$ and $c_2$ are the first two canonical variables given by MANOVA)

Figure 3-11. Distribution of normal and pre-surgery data points based on the extreme points (EP) ($gm\text{dist}$=group mean distance, $c_1$ and $c_2$ are the first two canonical variables given by MANOVA)
Figure 3-12. Distribution of pre- and post-surgery data points based on the modified linear regression technique (MREG) ($gmdist=group \ mean \ distance$, $c_1$ and $c_2$ are the first two canonical variables given by MANOVA)

Figure 3-13. Distribution of normal and post-surgery data points based on the modified linear regression technique (MREG) ($gmdist=group \ mean \ distance$, $c_1$ and $c_2$ are the first two canonical variables given by MANOVA)

3.6 Conclusions

Glottal axis plays a crucial role to get certain objective quantification of vocal fold vibratory pattern features from HSV data. Connecting the extreme points on vocal fold edge and forming linear regression line based on glottal edge are two normal ways to acquire the glottal axis. Although the linear regression line of glottal edge pixels shows good capability to be the glottal axis, it fails to represent the real axis when comes to some disordered voices, since the shapes of these pathological vocal fold are irregular. Considering the most anterior glottal area point of vocal fold is stable and the glottal axis always goes through this point, we propose to integrate the location of this point while calculating glottal axis. Aiming at investigating the ability of glottal axis
to differentiate different vocal fold vibratory patterns, several symmetry-related features have been extracted to represent vocal fold vibratory characteristics. Axes’ capability on differentiating vibratory patterns has been evaluated based on those features. As we expect, the GAD techniques of MREG and MPCA which integrate the location of the most anterior glottal area point give the best performance on differentiating vibratory patterns of normal vocal folds and vocal folds with polyp (pre-surgery). Besides, the comparison between the automatic GAD techniques and manual glottal axis determination also indicates that the MREG has the highest accuracy while acquiring the glottal axis.
CHAPTER 4. CLASSIFICATION OF VOCAL FOLD VIBRATION IN VOICE DISORDERS WITH VARYING ETIOLOGY

4.1 Background

One of the most important goals of vocal fold analysis is to investigate the vocal fold function for voice disorders with different etiology. The examination of vocal fold vibratory function is one of the essential parts of clinical voice assessment in determining effects of a vocal pathology. The investigation of symmetry and regularity of vocal fold vibration patterns are two important measurements [53]. High speed videoendoscopy with large frame rate makes the observation of irregular vibration feasible. However, the most used technique to evaluate HSV data is the perceptual evaluation of its data. Currently available HSV system with their increased temporal and spatial resolutions allows the use of image processing techniques to quantify HSV data objectively. This enables the quantitative analysis for the symmetry and regularity features of vocal fold vibratory features.

The objective analysis that quantifies the vibration characteristics of vocal fold has been explored for a long time. There are a large body of literatures addressing the features which can be used to do the objective analysis. The most commonly used features are based on the glottal area waveform. For this type of features, we need to calculate the glottal area for each frame at first, and then get the one dimensional glottal area waveform [7]. The oscillation cycle can be determined by choosing the frame from a maximum/minimum glottal opening to the next one. Therefore, the features such as the open quotient which describe the proportion of time the glottis is open during a vibration cycle [54], the glottal insufficiency which captures the relation between the maximum and minimum glottal opening for each cycle [55], and amplitude periodicity that computes a vocal fold’s deflection stability [16] can be extracted from the glottal area waveform.
In addition, similar to extracting features from glottal area waveform, we could also explore features such as lateral peaks, mucosal waves, and medial peaks [10][56] based on videokymography data, which is one dimensional data obtained from a certain position in each frame. However, unless we have an extremely stable vocal fold and high speed camera while collecting the high speed data, getting these features is highly challenging since it is not easy to capture the same position of vocal fold in each frame. On the other hand, some biomechanical model parameters can be used as good objective features too. Specifically, a biomechanical model is investigated to fit vocal fold vibration [11][29]. Besides, the aforementioned PVG parameters can be good features [57]. While most of features are obtained based on the sustained phonation period, the parameters computed from vocal fold onset and offset period can be another type of features [58]. Unlike the sustained phonation period which implies a stable stage, the onset that represents the initiation of phonation and the offset corresponding to the ending of phonation also may convey valuable vibration information. In this study, we explore new features in addition to some traditional features such as symmetry and open quotient [54]; with a particular focus on features that could represent the information within one vibration cycle and the shape of glottal area.

For a vocal fold, we could have a feature vector to demonstrate its oscillation pattern after getting features from its HSV recording. According to this feature vector, classification could be achieved to differentiate healthy and pathological vocal fold. However, some features may give similar values while evaluating two different types of vocal folds. In other word, this feature is not discriminant enough for the purpose of classification. In contrast, it will decrease the efficiency of classification. Therefore, principal component analysis (PCA) is adopted to decrease the dimensionality of feature vectors and get rid of the useless information.
In this study, the HSV data of 60 subjects including normal vocal fold, unilateral vocal fold paralysis and unilateral vocal fold polyp has been used to do the classification. After getting the final feature vector for each HSV data, both the support vector machine (SVM) and neural network have been used to test the classification rate. Different classification tasks have been set and analyzed. The result of this study will be discussed in the following section.

4.2 Data

In this study, we have HSV recording collected from 60 different subjects, including 20 subjects with normal vocal fold, 20 subjects with unilateral vocal fold polyp and 20 subjects with unilateral vocal fold paralysis. All HSV data used in this study is recorded by the same system mentioned in chapter 3. For every recording, a segment of 100 oscillation cycles is selected from sustained phonation for the study.

4.3 Feature Extraction

Finding a salient feature is a key step to achieve satisfying result for classification. A discriminant feature could easily improve the classification rate among different types of vocal folds. In this study, we explore traditional features and also developed new features to test the classification among different types of vocal folds. The features we investigate are discussed as follows.

All the features discussed in this study are calculated based on the locations of the glottal edge pixels in each HSV frame. The same as above chapter, the edge pixel locations are defined by $p_k = [x_k, y_k]^T$, $k = 1, 2, \ldots, K$, where $x_k \in \{0, 1, \ldots, M - 1\}$ and $y_k \in \{0, 1, \ldots, N - 1\}$ represent the vertical and horizontal pixel indices, respectively.

- Maximum opening index difference ($syn_{tr}$)
The synchronization of left and right vocal fold oscillation is an important characteristic to evaluate the vocal fold function. A very directive way to measure this synchronization characteristic is to find whether left and right vocal fold reach its maximum opening at the same time or not, which can be obtained from left and right glottal area waveform. In an HSV frame, depending on the glottal axis, glottal edge could be divided into left and right glottal edge easily. Therefore, we could get the left \( (GA_l) \) and right glottal area waveform \( (GA_r) \) respectively. Maximum opening index \( (maxopenind_l \text{ and } maxopenind_r) \) can be acquired for each glottal area waveform by searching the maximum value in each vibration cycle. Therefore, the synchronization of left and right vocal fold oscillation is depicted by taking the difference of these two indexes.

\[
syn_{lr} = |maxopenind_l - maxopenind_r| \tag{4.1}
\]

Figure 4-1 shows left and right glottal area waveform for normal vocal fold and unilateral vocal fold paralysis. It can be seen that left and right vocal fold achieve their maximum opening at the same time for normal vocal fold, while right vocal fold is two frames later than left vocal fold for unilateral vocal fold paralysis in this case.

![Figure 4-1. Left and right glottal area waveform of (a) normal vocal fold; (b) unilateral vocal fold paralysis](image)
• Oscillation synchronization of left and right glottal edge \((rtiofeqdirc_1, rtiofeqdirc_2, rtiofeqdirc_3)\)

The feature of maximum opening index difference generally illustrates how the synchronization of left and right glottal opening reach their maximum openings for a vocal fold. However, this feature only considers the glottal area in each maximum opening frame. For a vocal fold, the asynchronization may happen from one frame to the next frame, or it may only happen in some certain portion of vocal fold. In this case, the feature of maximum opening index difference will miss this information. Aiming at catching the asynchronization from one frame to the next one, we select three different positions on glottal area first (refers to Figure 4-2), which will guarantee that different portion of vocal fold is tested for the synchronization. Then the displacement of glottal edge from one frame to the next one is calculated for left and right vocal fold respectively. If the left and right vocal folds are synchronization with each other, the displacements should have different signs with one positive and one negative. In other words, if left and right vocal folds are asynchronization, which means one glottal area is opening while the other one is closing, the two displacements will have the same signs. For example, in Figure 4-2, four glottal edge pixels \(\mathbf{p}_1 = [x_1 \ y_1]^T, \mathbf{p}_2 = [x_2 \ y_2]^T, \mathbf{p}_3 = [x_3 \ y_3]^T, \mathbf{p}_4 = [x_4 \ y_4]^T\) are got from two continued frames in the middle position of glottal area. Two displacements can be computed by,

\[
d_1 = y_2 - y_1 \tag{4.2}
\]

\[
d_2 = y_3 - y_4 \tag{4.3}
\]

For exploring the synchronization between these two HSV frames, the sign of \(d_1\) and \(d_2\) is compared at these three positions \((rtiofeqdirc_1, rtiofeqdirc_2, rtiofeqdirc_3)\) respectively.
Figure 4-2. Displacement calculation from one frame to the next one

- Phase difference and energy on maximum opening index ($phase_d$, $E$)

From the first feature, we get the difference of left and right maximum opening index. Based on this information, more details such as phase difference ($phase_d$) and energy ($E$) could be evaluated by taking Fourier transform on maximum opening index.

\[ phase_d = |\text{angle}(\text{fft(maxopenind}_l)) - \text{angle}(\text{fft(maxopenind}_r))| \] .......................... 4.4

\[ E = \sum |\text{fft(syn}_{lr})| \] .......................................................... 4.5

- Open quotient ($Open_q$)

Open quotient [54], which is the proportion of time the glottal area is open during a cycle, can be calculated based on the glottal area waveform.

- Opening and closing phase quotient ($OC_p$)

According to the glottal area waveform, the maximum opening index and minimum opening index could be very easy to obtain. Within one vibration cycle, the opening phase ($O_p$) is defined as the period from a minimum opening to the next maximum opening, while the closing phase ($C_p$) is defined as the period from a maximum opening to the next minimum opening. The ratio
of these two parameters indicates the opening and closing phase quotient. Figure 4-3 demonstrates the opening and closing phase in an oscillation cycle.

\[
OC_p = \frac{O_p}{C_p}
\]

![Graph showing glottal area over time with opening and closing phase annotations.]

Figure 4-3. Opening phase and closing phase of one oscillation cycle

- Symmetry \((S, A_l, A_a)\)

Symmetry is a very significant criterion to evaluate voice. To have the symmetry evaluation for each HSV recording, three measurements including symmetry between right and left vocal fold amplitudes \((S)\), asymmetry along the glottal length \((A_l)\) and asymmetry on the glottal area \((A_a)\) discussed in chapter 3 have been used. Based on these features, we can easily measure symmetry property for each single frame of HSV data.

- Place of polyp \((Polyp\text{pos})\)

The features of symmetry could provide symmetry measurement for each frame of HSV recording; however, these features treat each frame separately, which may miss some information between the HSV frames within one oscillation cycle. Therefore, to save all the vibration details
within one cycle, we color-coded the vibration amplitude for each horizontal position within glottal opening area. Each HSV frame corresponds to one color-coded bar. For example, Figure 4-4(b) is the color-coded result for the HSV frame shown in Figure 4-4(a), and Figure 4-4(c) is the color-coded result for one vibration cycle from minimum opening to the next minimum opening. From this color-coded pattern, the portion of glottal area without vibration can be easily observed. For instance, there is no opening shown in the middle portion of glottal area for the frames before $f_1$ in Figure 4-4(c), which indicates the position of polyp. Therefore, this feature can help to examine the present of vibration area and then to classify the vocal fold with polyp from the normal vocal fold. In detail, for each horizontal position $x_i$, we could get the frame index $f_{x_i}$ when there is glottal opening. Maximum opening frame (refers to Figure 4-4(c)) $f_m$ can be easily acquired by searching the maximal glottal area within this cycle. Thus, the more closed of $f_{x_i}$ and $f_m$, the higher possibility of polyp on this position $x_i$ will be.

Figure 4-4. Color-coded of HSV frame (a) original HSV frame; (b) color-coded of (a); (c) color-coded of HSV frames within one vibration cycle

- Closed pattern of glottal area ($top_{track}$, $bom_{track}$)

Normally, the positions of most top and bottom points in glottal area should be very stable from one vibration cycle to the next one. However, if there is a polyp on vocal fold, the positions
of those two points may be changed, since the glottal area may not completely closed result from the presence of polyp. Therefore, we find the positions of most top and bottom points for each frame within a cycle, \( \mathbf{te} = [te_1 \ te_2 \ \ldots \ te_n]^T \) and \( \mathbf{be} = [be_1 \ be_2 \ \ldots \ be_n]^T \). The feature \( top_{track} \) and \( bom_{track} \) are depicted by the standard deviation of \( \mathbf{te} \) and \( \mathbf{be} \).

- Difference on glottal edges (\( edge_{diff} \))

We have stated that symmetry is a very important criterion for evaluating the vocal fold vibration. Actually, two aspects are included in this symmetry measurement. One is symmetry on the shape of glottal edge, while the other is symmetry of the left and right vocal fold vibration amplitude, which is described by \( S \). Aiming at exploring the symmetry on the shape of glottal edge, we apply Fourier transform on left and right glottal edges respectively. Figure 4-5 gives an example of glottal edges and their Fourier transform result for a vocal fold with polyp.

![Image](image.png)

Figure 4-5. (a) left and right glottal edges of a HSV frame (b) Fourier transform of (a)

- Presence of polyp (\( polyp_{pres} \))

If there is a polyp on a vocal fold, the amplitude of vibration maybe different from the normal vocal fold. Therefore, getting the amplitude value of a vocal fold could help us to identify
the presence of polyp on the vocal fold. In detail, we obtain a curve $a \nu$ which including amplitude values in each horizontal position of glottal area in maximum opening frame. Then we apply polynomial fitting on curve $a \nu$, and get the fitted curve $a \nu_f$. Finally, we count the number of peaks on the fitted curve. For vocal fold with normal voice, it should only have one peak, while it has more than one peak for the vocal fold with polyp or nodule, which can be found in Figure 4-6.

![Figure 4-6. Amplitude and its fitted curve on maximum opening frame of (a) normal vocal fold and (b) vocal fold with polyp](image)

- Curvature of glottal edge ($curva$)

We notice that the shape of glottal edge looks like an ellipse in ideal case, with two sharp turns on the posterior and anterior portions. If there is any tissue change with vocal fold, the shape of glottal edge will be changed, such as vocal fold with polyp. Curvature, which gives a large value for the position with large direction change (like sharp turn) on a curve, could be used to indicate the shape change of vocal fold. Therefore, we calculate the curvature values [59] for each point on the glottal edge, then find the peaks on the curvature curve. We only consider maximum opening frame for this feature, since maximum opening frame provides the best picture for the whole glottal edge. In details, giving the glottal edge pixels on maximum opening
frame, we find the centroid of glottal area first. For each glottal edge pixel \( p(x_i, y_i) \), the value of angle \( \theta_i \) is calculated (refers to Figure 4-7). Then, to make sure edge pixels’ coordinates are in the order of their corresponding angles from 0 to 360, interpolation is applied on angles to sort the coordinate \( x = [x_1 \ x_2 \ \ldots \ x_K]^T \) and \( y = [y_1 \ y_2 \ \ldots \ y_K]^T \). With this information, the curvature is calculated by,

\[
ct(i) = \frac{x_i(i, \sigma)y_i(i, \sigma) - x_i(i, \sigma)y_i(i, \sigma)}{(x_i(i, \sigma)^2 + y_i(i, \sigma)^2)^{3/2}}
\]

\[
X_i(i, \sigma) = \frac{\partial(x \otimes g(i, \sigma))}{\partial i} = x \otimes g_i(i, \sigma)
\]

\[
X_{ii}(i, \sigma) = \frac{\partial^2(x \otimes g(i, \sigma))}{\partial i^2} = x \otimes g_{ii}(i, \sigma)
\]

\[
Y_i(i, \sigma) = \frac{\partial(y \otimes g(i, \sigma))}{\partial i} = y \otimes g_i(i, \sigma)
\]

\[
Y_{ii}(i, \sigma) = \frac{\partial^2(y \otimes g(i, \sigma))}{\partial i^2} = y \otimes g_{ii}(i, \sigma)
\]

![Figure 4-7. Curvature calculation](image)

- Convex hull of glottal edge (\( \text{conv}_{\text{ratio}} \))

Furthermore, aiming at describing the shape of glottal area, the convex hull of glottal area is obtained. Based on Figure 4-8, we can find the convex hull of vocal fold with normal voice and
vocal fold with polyp. Based on this information, the quotient of the glottal area and the convex area is computed. For vocal fold with normal shape, the quotient will be closed to 1.

Figure 4-8. Convex hull of glottal edge of (a) normal vocal fold and (b) vocal fold with polyp

4.4 Feature Evaluation

From the previous section, 18 features are acquired for each HSV recording. In other word, feature extraction provides a feature vector with dimensionality of 18 by 1 for each HSV data. For purpose of classification, it is very important to find features which are discriminant for classifying one type of vocal fold from the others. Therefore, it is necessary to eliminate the less discriminant features. Besides, it could help us to shorten the feature vector and improve the efficiency of classification accordingly.

To decrease the dimensionality of feature space, principal component analysis (PCA) is adopted. In this study, we have 60 different HSV recording, which obtained from 20 subjects with normal vocal fold, 20 subjects of unilateral vocal fold polyp, and 20 subjects of unilateral vocal fold paralysis. After feature extraction, each HSV recording corresponds to a 18*1 feature vector. Thus, the feature space for whole data will be a 18*60 matrix $\mathbf{H} = [h_1 \ h_2 \ \ldots \ h_{60}]$. Given the covariance estimate matrix,
where $\overline{\mathbf{h}}$ is the average of all the column vectors of $\mathbf{H}$, we calculate its eigenvalues

$$
\lambda = [\lambda_1 \ \lambda_2 \ \ldots \ \lambda_{18}]^T
$$

and the corresponding eigenvectors $\mathbf{v} = [v_1 \ v_2 \ \ldots \ v_{18}]^T$. The goal of feature evaluation is to save as much original information as possible while decreasing the dimensionality of feature space. Therefore, eigenvalue, which indicates the proportion of information its corresponding vector saved, is used to guide the number of dimensionality we should keep. Figure 4-9 shows the eigenvalues for 18 eigenvectors. For instance, if each feature vector is decreased to $3*1$, the proportion of original information is saved could be calculated by taking the quotient of the sum of the largest three eigenvalues and the sum of all the eigenvalues,

$$
q = \frac{\sum_{i=1}^{3} \lambda_i}{\sum_{i=1}^{20} \lambda_i}
$$

In this study, 97% of original information is saved by decreasing the feature vector from $18*1$ to $3*1$ and 90.1% of original information is saved by shrinking the feature vector from $18*1$ to $2*1$. Obviously, the first three eigenvalues indicates that most of original information is saved by taking first three dimensions. Using the eigenvectors $\mathbf{v}_{\text{eigen}} = [v_1 \ v_2 \ v_3]^T$ which correspond to the largest three eigenvectors, the new decreased feature is obtained,

$$
\mathbf{h}'_i = \mathbf{v}_{\text{eigen}}(h_i - \overline{\mathbf{h}})
$$

where $i = 1, 2, \ldots 60$. Figure 4-10 provides a distribution of HSV data used in this study when each feature vector is decreased from $18*1$ to $2*1$. 
4.5 Classification

With regard to explore the vocal fold function of voice disorder with varying etiology, classification is the final goal for the vocal fold analysis in this study. Two classification methods have been used to test different types of vocal folds. One is support vector machine (SVM), and the other is neural network.

While the data set we used here has three different types of vocal folds with 20 HSV recordings respectively, 15 HSV data in each type of vocal folds are selected as training set and the rest...
5 of them is used as testing set. To get robust classification result, cross-validation is adopted. Therefore, we take 30 testing trails. Each trial, we randomly choose 15 HSV data from 20 for each type of vocal fold as the training set. The average of 30 classification rate is used as the final classification result for each classification task.

In this study, four different classification tasks are set, including ‘normal vocal folds vs unilateral vocal fold polyp’, ‘normal vocal folds vs unilateral vocal fold paralysis’, ‘unilateral vocal fold paralysis vs unilateral vocal fold polyp’, and ‘normal vocal folds vs unilateral vocal fold polyp vs unilateral vocal fold paralysis’. For the support vector machine approach, linear SVM is used here. When it comes to classify all three types of vocal fold together (‘normal vocal fold vs unilateral vocal fold polyp vs unilateral vocal fold paralysis), multi-SVM is implemented. Specifically, we could build three SVM models, with each model treating one type of vocal fold as one class and the other two types of vocal fold as another class. For instance, model $m_1$ is used to classify normal vocal fold from the other two vocal folds, model $m_2$ is used to classify unilateral vocal fold polyp from the rest two vocal folds, and model $m_3$ is used to classify unilateral vocal fold paralysis from the other two vocal folds. For neural network approach, we train a network with three layers and each layer with 7 nodes.

### 4.6 Result and Discussion

We have stated above that there are four classification tasks in this study, which are noted as follows:

- Classification task 1: normal vocal fold vs unilateral vocal fold polyp.
- Classification task 2: normal vocal fold vs unilateral vocal fold paralysis.
- Classification task 3: unilateral vocal fold paralysis vs unilateral vocal fold polyp.
Classification task 4: normal vocal fold vs unilateral vocal fold polyp vs unilateral vocal fold paralysis.

Table 4-1 lists the classification rate for each task based on two classification approaches, with all the classification rates that we reach are above 80%. It can be seen that SVM provides better performance in classification than that of neural network in this study. One of a possible reason is that we use the network with the same structure for all the classification tasks, which may not be the most appropriate one for each individual task.

Table 4-1. Classification rate for four classification tasks

<table>
<thead>
<tr>
<th>Classification tasks</th>
<th>Classification rate</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>SVM</td>
</tr>
<tr>
<td>Classification task 1</td>
<td>90.3%</td>
</tr>
<tr>
<td>Classification task 2</td>
<td>89.3%</td>
</tr>
<tr>
<td>Classification task 3</td>
<td>95.7%</td>
</tr>
<tr>
<td>Classification task 4</td>
<td>84%</td>
</tr>
</tbody>
</table>

With the comparison among different classification tasks, we notice that the classifications between two types of vocal fold (task 1, 2 and 3) lead to better performance than the classification among all three types of vocal fold (task 4). Therefore, for improving the classification accuracy, instead of merging all vocal folds with varying etiology together, we could treat each pathological vocal fold individually while comparing with normal vocal fold.

According to Table 4-1, for two-classes tasks (task 1, 2 and 3), we find that task 3 yields the best performance with rate up to 95.7%, and followed by task 1 and task 2. This result is reasonable when we compare the shape and oscillation characteristic of these three types of vocal fold. First, for normal vocal fold and unilateral vocal fold paralysis, the shapes of their vocal fold are similar (normal shape with no big tissue change); in other words, if we only observe the maximum opening frame of both these two types of vocal fold, we could not distinguish one from the
other. However, giving the whole vibration cycle, it will be easy for us to differentiate one type of vocal fold from the other since the synchronization of left and right vocal fold for vocal fold paralysis is not as good as normal vocal fold. Therefore, compared with classification task 1 and 3, task 2 gives the lowest accuracy. Second, for normal vocal fold and unilateral vocal fold polyp, the shapes of their vocal fold are different since polyp leads to structure change on vocal fold. Obviously, it will be easier to develop features to catch this shape difference when it comes to classification. Thus, the classification rate of task 1 is higher than that of task 2. Third, for unilateral vocal fold paralysis vs unilateral vocal fold polyp, both the shape difference and oscillation difference can be observed between these two types of vocal fold. Apparently, the classification between them will lead to the highest accuracy comparing with task 1 and 2. Finally, in order to demonstrate more details for classification task 1, Table 4-2 gives which vocal fold is identified when misclassification happens.

Table 4-2. Classification rate for task 1 by using SVM

<table>
<thead>
<tr>
<th></th>
<th>true normal vocal fold</th>
<th>true unilateral vocal fold paralysis</th>
<th>true unilateral vocal fold polyp</th>
<th>classification rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>normal vocal fold</td>
<td>216</td>
<td>9</td>
<td>25</td>
<td>86.4%</td>
</tr>
<tr>
<td>unilateral vocal fold paralysis</td>
<td>27</td>
<td>200</td>
<td>23</td>
<td>80%</td>
</tr>
<tr>
<td>unilateral vocal fold polyp</td>
<td>17</td>
<td>19</td>
<td>214</td>
<td>85.6%</td>
</tr>
</tbody>
</table>

Currently, the research on classification for vocal fold of HSV data is limited in literature. Daniel Voigt in [60] achieved classification between healthy and dysfunctional vocal fold by using PVG as features on HSV data. The average classification rate they reached is 78.5%. In this study, we could reach classification accuracy of 84% among the vocal fold with varying etiology. This difference may result from the different features we use for the classification. Also, another
possibility is that we use different HSV data for the study. Döllinger in [4] investigated the classification on HSV data with different frequency and intensity obtained from one subject with normal vocal fold. The classification accuracy up to 96% is achieved based on PVG features. In this work, we use the HSV data collected from the normal frequency. The classification on different frequency of pathological vocal fold will be a good future work. Most of the classifications are based on the acoustic data instead of HSV data. Linder in [61] reached the classification rate of 80% by using neural network to differentiate healthy and hoarse voice on acoustic data. The acoustical features such as jitter, shimmer, standard deviation of fundamental frequency and the glottal-to-noise excitation ratio are used. Besides, with discriminant analysis, Awan in [62] gives the categorization between healthy and functionally dysphonic voice such as breathy, hoarse and rough with accuracy of 74.6% according to the spectral-based acoustic measures. However, giving the HSV data of the normal and functionally dysphonic voice, we may reach to a better performance on the classification since HSV data providing detailed information of vibratory characteristics of vocal fold. Therefore, the comparison of acoustic feature and HSV feature on the pathological vocal fold can be a new study to investigate.

In addition to reach the classification among vocal fold with different etiology, we also want to explore the discrimination of each single feature. Thus, each single feature is set as input of SVM approach to achieve the classification between “normal vocal fold vs unilateral vocal fold polyp”, “normal vocal fold vs unilateral vocal fold paralysis”, “unilateral vocal fold polyp vs unilateral vocal fold paralysis”. The result is demonstrated in Table 4-2. In this study, in addition to four traditional features ($syn_{tr}, S, Open_q, OC_p$), we develop fourteen pathologically specific features. Based on different purpose, these new developed features can be divided into three groups.
- Features used to differentiate unilateral vocal fold paralysis (paralysis feature): \( \text{phase}_d \), \( E \), \( \text{rtioeqdirc}_1 \), \( \text{rtioeqdirc}_2 \), \( \text{rtioeqdirc}_3 \)

- Features used to differentiate unilateral vocal fold polyp (polyp feature): \( \text{edge}_\text{diff} \), \( \text{Polyp}_{\text{poss}} \), \( \text{Polyp}_{\text{pres}} \), \( \text{conv}_{\text{ratio}} \), \( \text{curva} \), \( \text{top}_{\text{track}} \), \( \text{bom}_{\text{track}} \)

- Features related to symmetry (symmetry feature): \( A_l \), \( A_d \)

From Table 4-2, we set classification rate above 0.7 as the acceptable accuracy rate to investigate each feature’s discriminant capability. First, we could observe that the polyp features such as \( \text{Polyp}_{\text{poss}} \), \( \text{Polyp}_{\text{pres}} \), \( \text{conv}_{\text{ratio}} \) and symmetry feature \( A_l \) demonstrate better performance than the other features when classifying normal vocal fold vibratory features from unilateral vocal fold polyp; the paralysis features including \( \text{phase}_d \), \( E \), \( \text{rtioeqdirc}_2 \) and polyp feature \( \text{conv}_{\text{ratio}} \) provide higher classification rate than the other features while classifying normal vocal fold from unilateral vocal fold paralysis. Therefore, the new derived pathologically specific features of polyp feature and paralysis feature can achieve their goal of differentiating pathological vocal fold from normal vocal fold very well. Besides, we notice that the polyp feature of \( \text{conv}_{\text{ratio}} \) also gives a good result when classifying unilateral vocal fold paralysis from normal vocal folds. A possible reason is that the frequency of phonation for these two groups of vocal fold may different and then result in the large change of vocal fold shape. Second, we also explore the classification between different pathological vocal folds. According to Table 4-2, the polyp features of \( \text{Polyp}_{\text{poss}} \), \( \text{Polyp}_{\text{pres}} \), \( \text{conv}_{\text{ratio}} \) give better result when the classification between unilateral vocal fold polyp and unilateral vocal fold paralysis is performed. Obviously, the new derived polyp features demonstrate better performance than that of paralysis features in this case. The reason is that the unilateral vocal fold polyp also has the synchronization problem since the weight of polyp will lead to asynchronization between two vocal folds during vibration.
Consequently, polyp features provide higher accuracy rate than that of paralysis feature when classifying unilateral vocal fold polyp from unilateral vocal fold paralysis. Therefore, these new developed features can be used to explore the vibratory characteristics of unilateral vocal fold polyp and unilateral vocal fold paralysis.

Table 4-3. Classification rate of each single feature based on SVM approach

<table>
<thead>
<tr>
<th>Features</th>
<th>Normal vs polyp</th>
<th>Normal vs paralysis</th>
<th>Polyp vs paralysis</th>
</tr>
</thead>
<tbody>
<tr>
<td>$syn_{tr}$</td>
<td>0.64</td>
<td>0.70</td>
<td>0.48</td>
</tr>
<tr>
<td>$S$</td>
<td>0.58</td>
<td>0.62</td>
<td>0.56</td>
</tr>
<tr>
<td>$Open_d$</td>
<td>0.69</td>
<td>0.68</td>
<td>0.48</td>
</tr>
<tr>
<td>$OC_p$</td>
<td>0.49</td>
<td>0.68</td>
<td>0.60</td>
</tr>
<tr>
<td>$phase_d$</td>
<td>0.65</td>
<td>0.74</td>
<td>0.58</td>
</tr>
<tr>
<td>$E$</td>
<td>0.67</td>
<td>0.73</td>
<td>0.50</td>
</tr>
<tr>
<td>$rtioeqdir_1$</td>
<td>0.65</td>
<td>0.68</td>
<td>0.55</td>
</tr>
<tr>
<td>$rtioeqdir_2$</td>
<td>0.63</td>
<td>0.78</td>
<td>0.68</td>
</tr>
<tr>
<td>$rtioeqdir_3$</td>
<td>0.69</td>
<td>0.69</td>
<td>0.64</td>
</tr>
<tr>
<td>$edge_{diff}$</td>
<td>0.63</td>
<td>0.59</td>
<td>0.46</td>
</tr>
<tr>
<td>Polyp $pos$</td>
<td>0.72</td>
<td>0.45</td>
<td>0.78</td>
</tr>
<tr>
<td>Polyp $pres$</td>
<td>0.77</td>
<td>0.53</td>
<td>0.81</td>
</tr>
<tr>
<td>conv$_{ratio}$</td>
<td>0.86</td>
<td>0.73</td>
<td>0.75</td>
</tr>
<tr>
<td>curva</td>
<td>0.55</td>
<td>0.59</td>
<td>0.51</td>
</tr>
<tr>
<td>top$_{track}$</td>
<td>0.61</td>
<td>0.46</td>
<td>0.46</td>
</tr>
<tr>
<td>bom$_{track}$</td>
<td>0.58</td>
<td>0.52</td>
<td>0.44</td>
</tr>
<tr>
<td>$A_l$</td>
<td>0.73</td>
<td>0.61</td>
<td>0.49</td>
</tr>
<tr>
<td>$A_R$</td>
<td>0.53</td>
<td>0.59</td>
<td>0.48</td>
</tr>
</tbody>
</table>

4.7 Conclusion

In this study, a method is proposed to achieve the classification between normal vocal fold and vocal fold with varying etiology. Based on glottal segmentation and glottal axis determination techniques, we extract 18 different features from HSV data. To eliminate the less discriminant feature and improve the classification efficiency, feature evaluation is adopted in order to decrease the dimensionality of each feature vector obtained from each HSV data. Then, the decreased feature vector is set as input of classification approaches for the final result. SVM and
neural network are two classification approaches used here. The classification rate of all the different classification tasks designed in this study are above 80%. It shows that SVM provides better performance than that of neural network. In addition, for classification, the two-class tasks demonstrate higher accuracy than that of three-class task. In [60], it is stated that the phonation frequency impacts the measurement of vocal fold vibration. Therefore, it will impose influence on the classification too. In this study, the HSV recordings we used are recorded based on the normal phonation frequency. The frequency should not be a problem. However, for future study, for each subject, we can take the HSV data with different phonation frequency, and then explore the classification among HSV data with different frequency.
CHAPTER 5. SUMMARY AND FUTURE WORK

5.1 Summary

Providing detailed imaging system with high frame rate, high speed videoendoscopy has driven the development of the analysis on HSV data of vocal fold. Many approaches such as Phonovibrogram (PVG) and videokymography give quantitative analysis on vocal fold vibration. However, a sophisticated quantitative analysis on voice disordered with varying etiology is still demanded. This research presents a series of studies addressing this problem.

First, the glottis segmentation, which is a very significant pre-processing step of objective assessment of vocal fold vibration behavior, is explored. We propose a new glottis segmentation approach based on the simplified dynamic programming. The evaluation results demonstrate that our proposed method could give a very good performance on both efficiency and accuracy compared with two kinds of currently used segmentation methods such as the fixed-threshold method and the active contour method.

Second, followed by the segmentation, we illustrate glottal axis determination technique, which is very significant for acquiring some vibratory features. We present five different glottal axis determination techniques including the existing and the proposed ones. Two ways have been used to evaluate those techniques. One is to compare the glottal axis acquired by each technique with the manually selected glottal axis. The other one is to compare their performance on differentiating vocal fold with polyp from normal vocal fold. The glottal axis determination technique using the anterior endpoint information is considered as the best one based on both two evaluation methods.
The third study presented in this research pays attention to the classification among different types of vocal fold. According to the glottal edge and glottal axis obtained from the first two steps, we extract several features for each HSV data. Then, feature evaluation is followed to get the discriminant features. At last, the final goal is reached by inputting the feature vectors to classification approaches of SVM and neural network. The classification rate for all the tasks are above 80%, with highest of 95.7% for the differentiation between unilateral vocal fold paralysis and unilateral vocal fold polyp.

5.2 Future Work

While the research presented in this dissertation focuses on the HSV data obtained from subjects with normal frequency, the HSV data with different range of frequency can be another topic to be investigated. In the near future, for the voice disordered with certain etiology, we could collect its HSV data at three different frequencies such as low, normal and high. Thus, features extracted from these HSV data will be explored for the purpose of classification. As a consequence, we could figure out whether these features will be affected by the change of frequency of phonation.

On the other aspect, in this presented work, the features we extracted are from sustained phonation of each HSV data. However, the voice onset period and voice offset period can be another valuable segment to be explored. The voice onset period which represents voice initiation of the phonation and the voice offset period that demonstrates the ending of the phonation both are very short segments. The vocal fold vibration within these two periods is not as regular as that in the sustained phonation. Whether there is relationship between these irregular vibration periods and certain etiology is yet to be determined. Therefore, feature extraction on voice onset period and voice offset period could be explored and then, the investigation of the vibration
characteristics on these two periods will be acquired based on the classification for voice disor-
dered with varying etiology.
REFERENCES


APPENDIX AUTHOR’S PUBLICATIONS


VITA

Jing Chen was born in 1985, in Huanggang, Hubei, China. She received her Bachelor’s, Master’s degree in Electronics and Information Engineering, Pattern Recognition and Intelligent System from Huazhong University of Science and Technology respectively in June 2007 and March 2010. Since then, she has been enrolled in the Department of Electrical and Computer Engineering at Louisiana State University, Baton Rouge, Louisiana, to pursue her doctorate degree. During this period, she passed her qualify exam in Fall 2011 and general exam in April 2013, respectively. She anticipates graduating with her Doctor of Philosophy degree in Summer 2014.

Jing’s research interests broadly lie in imaging processing, pattern recognition, and vocal fold vibratory behavior analysis on high speed videoendoscopy. She has published a series of papers on these topics in various image processing and voice analysis conferences.